Cache Design

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Oracle Cache

- CPU Cycles = CPU Compute Cycles + Memory Stall Cycles
- **Oracle cache**: a cache that never misses
 - In effect, Memory Stall Cycles == 0
 - o Impossible, since even with infinite capacity, there are still cold misses
 - But useful to set **bounds** on performance
- Real caches may approach performance of oracle caches but can't exceed
- What metric can we use to compare and evaluate real cache designs?
 - AMAT (Average Memory Access Time)



AMAT (Average Memory Access Time)

- AMAT (Average Memory Access Time) is defined as follows:
 - AMAT = hit time + (miss rate × miss penalty)
 - o Hit time: time to get the data from cache when we hit
 - Miss rate: what percentage of cache accesses we miss
 - o Miss penalty: time to get the data from lower memory when we miss
 - Shouldn't it be hit rate × hit time?
 - Hit time is incurred regardless of hit or miss
 - It is more aptly called access time (the time to search for the data)
- Hit time, miss rate, miss penalty are the 3 components of a cache design
 - When evaluating a cache design, we need to consider all 3
 - Cache designs trade-off one for the other
 - E.g. a large cache trade-offs longer hit time for smaller miss rate
 - Whether trade-off is beneficial depends on the resulting AMAT



Cache Design Parameter 1: Number of Levels



AMAT of No-Cache vs. L1 Cache

- For a CPU with no caches:
 - AMAT(none) = DRAM access time

```
Hit! DRAM Memory DRAM access time
```

- For a single-level cache (L1 cache):
 - \circ AMAT(L1) = L1 hit time + (L1 miss rate × DRAM access time)

```
Miss! Hit! L1 Cache L1 hit time

Hit! DRAM Memory L1 miss rate × DRAM access time
```



AMAT of No-Cache vs. L1 Cache

For L1 Cache to be worth it, AMAT(None) > AMAT(L1) needs to be true.

```
    DRAM Memory
    PRAM access time
    PRAM L1 hit time
    DRAM Memory
    L1 miss rate × DRAM access time
```

- AMAT(None) > AMAT(L1)?
- → DRAM access time > L1 hit time + L1 miss rate × DRAM access time
- \rightarrow (1 L1 miss rate) \times DRAM access time > L1 hit time
- → Benefit from reduced DRAM accesses > Penalty from accessing L1
- So, should we add an L1 cache or not?
 - Depends on L1 miss rate, which depends on locality present in software!



AMAT of No-Cache vs. L1 Cache

- For it to be worth it to install an L1 cache:
 (1 L1 miss rate) × DRAM access time > L1 hit time
- Let's assume L1 hit time = 1 cycle and DRAM access time = 100 cycles:
 (1 L1 miss rate) × 100 > 1
 L1 miss rate < 0.99
 → If L1 miss rate can be kept below 99%, worth it to install L1 cache!
- Let's assume L1 hit time = 1 cycle and DRAM access time = 10 cycles:
 (1 L1 miss rate) × 10 > 1
 L1 miss rate < 0.90
 → If L1 miss rate can be kept below 90%, worth it to install L1 cache!
- Let's assume L1 hit time = 1 cycle and DRAM access time = 1 cycle:
 (1 L1 miss rate) × 1 > 1
 L1 miss rate < 0
 - → There is no reason to put in an L1 whatsoever.



AMAT of Only L1 Cache vs. L1 + L2 Cache

- For a single-level cache (L1 cache):
 - \circ AMAT(L1) = L1 hit time + (L1 miss rate × DRAM access time)



- For a multi-level cache (L1, L2 caches):
 - \circ AMAT(L2) = L1 hit time + (L1 miss rate × L1 miss penalty)
 - \circ L1 miss penalty = L2 hit time + (L2 miss rate × DRAM access time)
 - AMAT(L2) = L1 hit time + L1 miss rate × L2 hit time
 + L1 miss rate × L2 miss rate × DRAM access time





AMAT of Only L1 Cache vs. L1 + L2 Cache

For L2 Cache to be worth it, AMAT(L1) > AMAT(L2) needs to be true.

```
L1 Cache

L1 hit time

L1 miss rate × DRAM access time

>?

L1 Cache

L1 hit time

L2 Cache

L1 miss rate × L2 hit time

DRAM Memory

L1 miss rate × L2 miss rate × DRAM access time
```

- AMAT(L1) AMAT(L2)
 - = $(L1 \text{ miss rate} L1 \text{ miss rate} \times L2 \text{ miss rate}) \times DRAM access time$
 - L1 miss rate \times L2 hit time
 - = L1 miss rate \times ((1 L2 miss rate) \times DRAM access time L2 hit time) > 0
- \rightarrow (1 L2 miss rate) \times DRAM access time > L2 hit time
- → Benefit from reduced DRAM accesses > Penalty from accessing L2



Cache Design Parameter 2: Cache Size



Impact of Cache Size (a.k.a. Capacity) on AMAT

- AMAT = hit time + (miss rate × miss penalty)
- Larger caches are good for miss rates
 - More capacity means you can keep around cache blocks for longer
 - Means you can leverage more of the pre-existing temporal locality
 - o If entire working set can fit into the cache, no capacity misses!
- But larger caches are bad for hit times
 - o Longer wires and larger decoders mean longer access time
- Exactly why there are multiple levels of caches
 - o **Frequently** accessed data where hit time is important stays in **L1** cache
 - Rarely accessed data which is part of a larger working set stays in L3



What cache size(s) should I choose?

- How should each cache level be sized?
- That depends on the application
 - Working set sizes of the application at various levels. E.g.:
 - Small set of data accessed very frequently (typically stack variables)
 - Medium set of data accessed often (currently accessed data structure)
 - Large set of data accessed rarely (rest of program data)
 - o Ideally, cache levels and sizes would reflect working set sizes.
- Simulate multiple cache levels and sizes and choose one with lowest AMAT
 - Simulate on the applications that you care about
 - In the end, it must be a compromise (giving best average AMAT)



Cache Design Parameter 3: Cache Block Size



Impact of Cache Block Size on AMAT

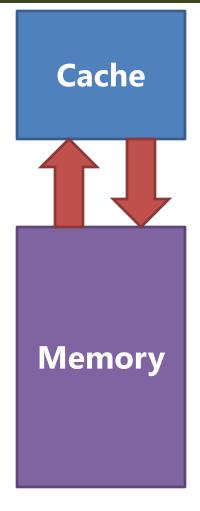
- AMAT = hit time + (miss rate × miss penalty)
- Cache block (a.k.a. cache line)
 - Unit of transfer for cache data (typically 32 or 64 bytes)
 - o If program accesses any byte in cache block, entire block is brought in
 - o Each level of a multi-level cache can have a different cache block size
- Impact of larger cache block size on miss rate
 - Maybe smaller miss rate due to better leveraging of spatial locality
 - Maybe bigger miss rate due to worse leveraging of temporal locality (Bringing in more data at a time may push out other useful data)
- Impact of larger cache block size on miss penalty
 - With a limited bus width, may take multiple transfers for a large block
 - o E.g. DDR 4 DRAM bus width is 8 bytes, so 8 transfers for 64-byte block
 - Could lead to increase in miss penalty



Cache Block Size and Miss Penalty

- On a miss, the data must come from lower memory
- Besides memory access time, there's transfer time
- What things impact how long that takes?
 - The size of the cache block (words/block)
 - The width of the memory bus (words/cycle)
 - The speed of the memory bus (cycles/second)
- So the transfer time will be:

$$\frac{\text{seconds}}{\text{block}} = \frac{1}{\frac{\text{cycles}}{\text{second}} \times \frac{\text{words}}{\text{cycle}}} \times \frac{\text{words}}{\text{block size}}$$
bus speed bus width





What cache block size should I choose?

- Again, that depends on the application
 - How much spatial and temporal locality the application has
- Simulate multiple cache block sizes and choose one with lowest AMAT
 - Simulate on benchmarks that you care about and choose best average
 - You may have to simulate different combinations for multi-level caches



Cache Design Parameter 4: Cache Associativity



Mapping blocks from memory to caches

- Cache size is much smaller compared to the entire memory space
 - Must map all the blocks in memory to limited CPU cache
- Does this sound familiar? Remember branch prediction?
 - Had similar problem of mapping PCs to a limited BHT
 - O What did we do then?
 - We hashed PC to an entry in the BHT
 - On a hash conflict, we replaced old entry with more recent one
- We will use a similar idea with caches
 - Hash memory addresses to entries in cache
 - o On a conflict:
 - Replace old cache block with more recent one
 - Or, chain multiple cache blocks on to same hash entry



Impact of Cache Associativity on AMAT

- Depending on hash function and chaining, a cache is either:
 - Direct-mapped (no chaining allowed)
 - Set-associative (some chaining allowed)
 - Fully-associative (limitless chaining allowed)
- Impact of more associativity on miss rate
 - Smaller miss rate due to less misses due to hash conflicts
 - Misses due to hash conflicts are called conflict misses
 - A third category of misses besides cold and capacity misses
- Impact of more associativity on hit time
 - o Longer hit time due to need to search through long chain



Direct-mapped Caches



Assumptions

- Let's assume for the sake of concise explanations
 - 8-bit memory addresses
 - 4-byte (one word) cache block sizes
- Of course these are not typical values. Typical values are:
 - o 32-bit or 64-bit memory addresses (32-bit or 64-bit CPU)
 - 32-byte or 64-byte cache blocks sizes (for spatial locality)
 - o But too many bits in addresses are going to give you a headache
- According to our assumption, here's a breakdown of address bits

Upper 6 bits: Offset of cache block within main memory

Lower 2 bits: Byte offset within 4-byte cache block

 When I refer to addresses, I will sometimes omit the lower 2 bits (When we talk about cache block transfer, that part is irrelevant)

Direct-mapped Cache Hash Function

• Each memory address maps to **one** cache block

No chaining allowed so no need to search

• Implementing this is relatively simple

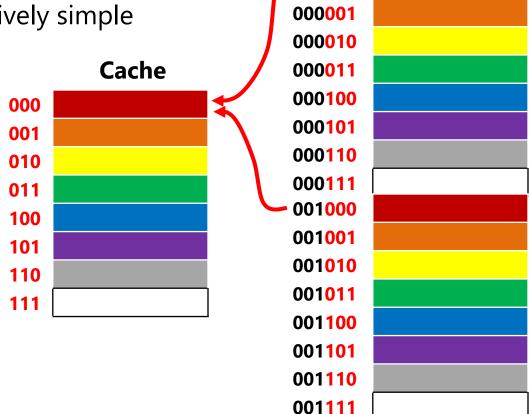
Hash function:

For this 8-entry cache, to find **cache block index**, take the lowest 3 cache block offset bits in address.

But if our program accesses **001000**, then **000000**, how do we tell them apart?

Tags!





000000

Memory

Tags help differentiate between conflicting blocks

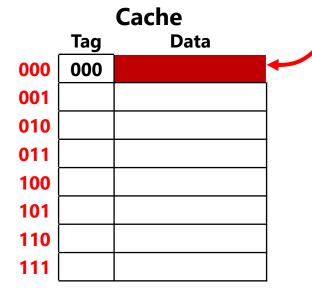
Tag: part of address excluding cache block index Memory On allocation of **001000**: tag = **001** Cache **Data** Tag

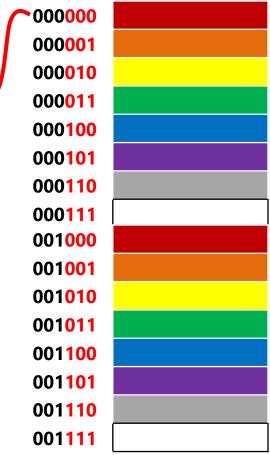


Tags help differentiate between conflicting blocks

Tag: part of address excluding cache block index

- On allocation of **001000**: **tag** = **001**
- On allocation of **000000**: **tag** = **000**





Memory



Valid bit indicates that block contains valid data

Cache

Valid bit: indicates that the block is valid

- Set to 0 initially when cache block is empty
- Set to 1 when a cache block is allocated

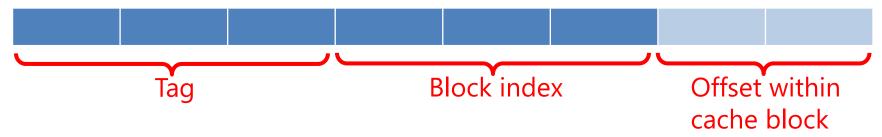
		-44110	
V	Tag	Data	
1	000		4
0			
0			
0			
0			
0			
0			
0			
	1 0 0 0 0 0	1 000 0 0 0 0 0 0	1 000 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0

Cache hit: V == 1 &&
 CacheBlock.Tag == MemoryBlock.Tag



Quiz: Address Bits Breakdown

- Now with the following parameters:
 - 8-bit memory addresses
 - 4-byte cache block sizes
 - 8-block cache
- How would we breakdown the memory address bits?

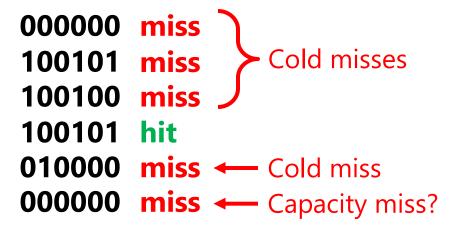


- o First, the correct cache block is accessed using the **block index**
- Then, the tag is compared to the cache block tag
- o If matched, **offset** is used to access specific byte within block



Example: A Direct-mapped Cache

- When the program first starts, we set all the valid bits to 0.
 - Signals all cache lines are empty
- Now let's try a sequence of reads... do these **hit** or **miss?** How do the cache contents change?



	V	Tag	Data
000	1	010	something
001	0		
010	0		
011	0		
100	1	100	something
101	1	100	something
110	0		
111	0		



Conflict Misses

- What should we call 2nd miss on **000000**?
 - Awkward to call it a capacity miss (It's not like capacity was lacking)
 - Let's call it a conflict miss

000000	miss
100101	miss Cold misses
100100	miss J
100101	hit
010000	miss ← Cold miss
000000	miss — Copákictymisss

	V	Tag	Data
000	1	010	something
001	0		
010	0		
011	0		
100	1	100	something
101	1	100	something
110	0		
111	0		



Types of Cache Misses (Revised)

- Besides cold misses and capacity misses, there are conflict misses
- Cold miss (a.k.a. compulsory miss)
 - o Miss suffered when data is accessed for the **first time** by program

• Capacity miss

- Miss on a repeat access suffered due to a lack of capacity
- When the program's working set is larger than can fit in the cache

Conflict miss

- Miss on a repeat access suffered due to a lack of associativity
- Associativity: degree of freedom in associating cache block with an index
- Direct mapped caches have no associativity
 - Since cache blocks are directly mapped to a particular block index



Associative caches



Flexible block placement

- Direct-mapped caches can have lots of conflicts
 - Multiple memory locations "fight" for the same cache line
- Suppose we had a 4-block direct-mapped cache

0 /	As	before,	4-byte	per	cache	block
-----	----	---------	--------	-----	-------	-------

- Memory addresses are 8 bits.
- The following locations are accessed in a loop:
 - 0 0, 16, 32, 48, 0, 16, 32, 48...
 - or 00000000, 00010000, 00100000, 00110000, ...

	V	Tag	Data
00	1	0011	
01	0		
10	0		
11	0		

• What would happen?

- They will all land on the same block index, and all conflict miss!
- Those other 3 blocks are not even getting used!
- What if we used the space to chain conflicting blocks?



Full associativity

Let's make our 4-block cache 4-way set-associative.

V	Tag	D
1	000000	*0

V	Tag	D
1	001100	*48

V	Tag	D
1	000100	*16

V	Tag	D
1	001000	*32

- What's the difference?
 - Now a hashed location can be associated with any of the 4 blocks
 - Analogous to having a hash conflict chain 4-entries long
 - The 4 cache blocks are said to be part of a cache set
 - When set size == cache size, it is said to be fully associative
- Let's do that sequence of reads again: 0, 16, 32, 48, 0, 16, 32, 48...
- Notice tag is now bigger, since there are no block index bits
 - Or set index bits in this context (just one set, so none needed)
- Now cache holds the entire working set: no more misses!



Example: A 2-way Set-Associative Cache

- 16-block 2-way set-associative cache
- Let's try the same stream of accesses as direct-mapped cache
- Yay! 2nd access to **000000** is no longer a conflict miss!

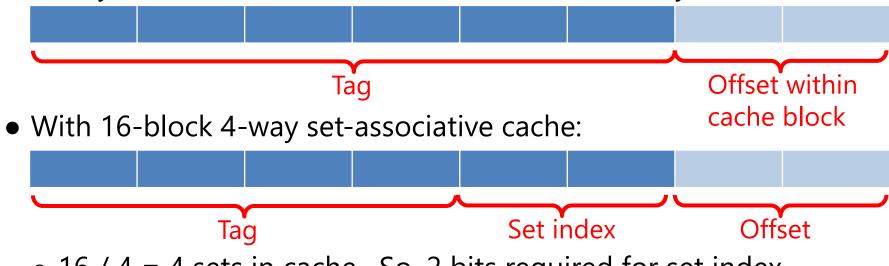
000000	miss
100101	miss
100100	miss
100101	hit
010000	miss
000000	hit

Set	V	Tag	Data	V	Tag	Data
000	1	000	something	1	010	something
001	0			0		
010	0			0		
011	0			0		
100	1	100	something	0		
101	1	100	something	0		
110	0			0		
111	0			0		



Address Bits Breakdown

• A fully associative cache (doesn't matter how many blocks):



- \circ 16 / 4 = 4 sets in cache. So, 2 bits required for set index.
- With 64-block 8-way set-associative cache:



64 / 8 = 8 sets in cache. So, 3 bits required for set index.

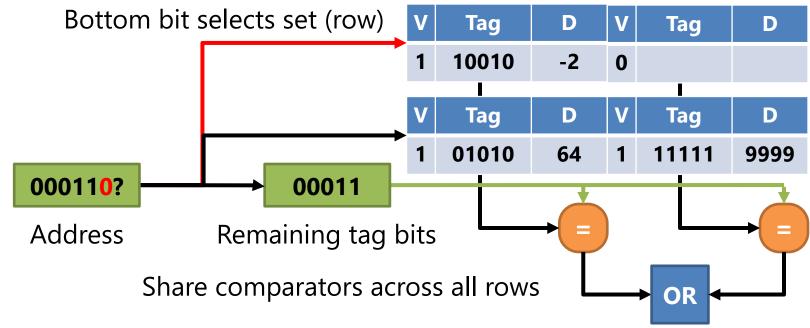
Want More Examples?

- Try out the Cache Visualizer on the course github:
 - https://github.com/wonsunahn/CS1541_Spring2023/tree/main/resources/cache_demo
 - Courtesy of Jarrett Billingsley
- Visualizes cache organization for various parameters
 - Cache block size
 - Number of blocks in cache (capacity)
 - Cache associativity



Associativity is Costly

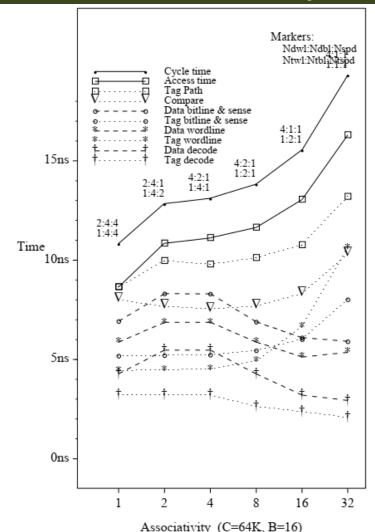
- Associativity requires complex circuitry and may increase hit time
- Full associativity is only used for very small caches
 - And where a cache miss is extremely costly
- Usually caches are 2-, 4-, or maybe 8- way set-associative





Access/cycle time as a function of associativity

Thoziyoor, Shyamkumar & Muralimanohar, Naveen & Ahn, Jung Ho & Jouppi, Norman. (2008). CACTI 5.1.





Cache Design Parameter 5: Cache Replacement Policy



Cache Replacement

• If we have a cache miss and no empty blocks, what then?

V	Tag	D
1	000000	*0

V	Tag	D
1	001100	*48

V	Tag	D
1	000001	*4

V	Tag	D				
1	001000	*32				

- Let's read memory address 4 (**000001**00).
 - O Uh oh. That's a miss. Where do we put it?
- With associative caches, you must have a **replacement scheme**.
 - Which block to evict (kick out) when you're out of empty slots?
- The simplest replacement scheme is **random**.
 - Just pick one. Doesn't matter which.
- What would make more sense?
 - o How about taking temporal locality into account?



LRU (Least-Recently-Used) Replacement

• When you need to evict a block, kick out the oldest one.

V	Tag	D	V	Tag	D	V	Tag	D	V	Tag	D
1	000001	*4	1	001100	*48	1	000100	*16	1	001000	*32
4 reads old			1 read	old		3 reads	old		2 reads	old	

- Our read history looked like 0, 16, 32, 48. How old are the blocks?
- Now we want to read address 4. Which block should we replace?
- But now we must maintain the age of the blocks
 - o Easy to say. How do we keep track of this in hardware?
- Have a saturating counter for each cache block indicating age
 - When accessing a set, increment counter for each block in set
 - On a cache hit, reset counter to 0 (most recently used)



Impact of LRU on AMAT

- AMAT = hit time + (miss rate × miss penalty)
- Impact of LRU on miss rate
 - Smaller miss rate due to better leveraging of temporal locality (Recently used cache lines more likely to be used again)
- Saturating counter for LRU uses bits and adds to amount of metadata
 - o Cache tag, the valid bit, the saturating counter are all metadata
 - o Every bit you spend on metadata is a bit you don't spend on real data
 - Spending many bits on counter may reduce capacity for real data
 - o This may lead to a **larger miss rate**, if LRU is not very effective

