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MODULE *P2PBroadcast*

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The specification caputurs the *DAG* base reliable broadcast to disseminate shares over a peer to peer network.

The broadcast enables nodes to know which nodes have revceived the message by using implicit acknowledgements. The broadcast is not a *BFT* broadcast. We depend on the higher layers to provide that.

Does this open this broadcast to a *DDoS* attack? Yes, and our argument remains that *p2p* network can resist *DDoS* attacks by other means.

First pass - We assume no processes failures or messages lost.

EXTENDS *Naturals, Sequences*

CONSTANT

*Proc*,      Set of processes  
*Data*,  
*Nbrs*

VARIABLES

*sent\_by*,      Set of messages sent by processes to their neighbours  
*recv\_by*      Set of messages received by processes

*vars*  $\triangleq$   $\langle sent\_by, recv\_by \rangle$

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*Message*  $\triangleq$   $[from : Proc, data : Data]$

*Init*  $\triangleq$   
 $\wedge sent\_by = [m \in Message \mapsto \{\}]$   
 $\wedge recv\_by = [m \in Message \mapsto \{\}]$

*TypeInvariant*  $\triangleq$   
 $\wedge sent\_by \in [Message \rightarrow \text{SUBSET } Proc]$   
 $\wedge recv\_by \in [Message \rightarrow \text{SUBSET } Proc]$

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*SendTo*(*m*, *p*) – send message *m* to neighbour *p*

Sending to self is required as then the message is in the recv list as well.

*SendTo*(*m*, *p*)  $\triangleq$   
 $\wedge m.from \notin sent\_by[m]$       Don't send again - we can add decay here  
 $\wedge \langle m.from, p \rangle \in Nbrs$       Send only to neighbours  
 $\wedge sent\_by' = [sent\_by \text{ EXCEPT } ![m] = @ \cup \{p\}]$   
 $\wedge \text{UNCHANGED } \langle recv\_by \rangle$

*RecvAt*(*m*, *q*) – receive message *m* at *q*. This can be received from forwards

*RecvAt*(*m*, *q*)  $\triangleq$   
 $\wedge \exists p \in Proc : p \in sent\_by[m]$       Some process has sent the message  
 $\wedge q \notin recv\_by[m]$       Not already received by *q*

$$\wedge \text{recv\_by}' = [\text{recv\_by} \text{ EXCEPT } ![m] = @ \cup \{q\}] \\ \wedge \text{UNCHANGED } \langle \text{sent\_by} \rangle$$

*Forward*( $m, p, q$ ) – forward message  $m$  from  $p$  to  $q$

Enabling condition –  $m$  has been sent by some process,  $q$  has received the message,  $q$  is not the sender

Effect –  $p$  forwards the message  $m$  to its nbrs

$$\begin{aligned} \text{Forward}(m, p, q) &\triangleq \\ &\wedge \exists r \in \text{Proc} : r \in \text{sent\_by}[m] \quad \text{Some process has sent the message} \\ &\wedge p \neq q \quad \text{Don't forward to self} \\ &\wedge \langle p, q \rangle \in \text{Nbrs} \quad \text{Forward only to neighbour} \\ &\wedge p \in \text{recv\_by}[m] \quad p \text{ has received } m \\ &\wedge \text{sent\_by}' = [\text{sent\_by} \text{ EXCEPT } ![m] = @ \cup \{q\}] \\ &\wedge \text{UNCHANGED } \langle \text{recv\_by} \rangle \end{aligned}$$

$$\begin{aligned} \text{Next} &\triangleq \exists p \in \text{Proc}, q \in \text{Proc}, m \in \text{Message} : \\ &\vee \text{SendTo}(m, p) \\ &\vee \text{RecvAt}(m, p) \\ &\vee \text{Forward}(m, p, q) \end{aligned}$$

$$\begin{aligned} \text{Spec} &\triangleq \wedge \text{Init} \\ &\wedge \Box [\text{Next}]_{\text{vars}} \end{aligned}$$

Liveness specifies that if a message is enabled to be received at  $p$ , it is eventually received at  $p$ .

$$\text{Liveness} \triangleq \forall p \in \text{Proc} : \forall m \in \text{Message} : \text{WF}_{\text{vars}}(\text{RecvAt}(m, p))$$

$$\text{FairSpec} \triangleq \text{Spec} \wedge \text{Liveness}$$

THEOREM  $\text{Spec} \Rightarrow \Box \text{TypeInvariant}$

\ \* Modification History  
\ \* Last modified Sun Mar 12 07:33:11 CET 2023 by kulpreet  
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