In-EVM Solana State Verification Circuit Description

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1 Introduction

This paper contains a description of the following PLONK-style circuits:

- SHA256 for block headers and transactions hashes verification.
- EdDSA for validators signature verification.
- Poseidon/Reinforce Concrete for state Merkle-tree and proof generation.

2 SHA256 Circuit

Suppose that input data in the 32-bits form, which is already padded to the required size. Checking that chunked input data corresponds to the original data out of this circuit. However, we add the boolean check and range proof.

Range proof that $a < 2^{32}$ Let $a = \{a_0, ..., a_{15}\}$, where a_i is two bits.

	w_1	w_2	w_3	w_4	w_o
j + 0	a_{12}	a_{13}	a_{14}	a_{15}	acc
j + 1	a_8	a_9	a_{10}	a_{11}	acc
j+2	a_4	a_5	a_6	a_7	acc
j+3	a_0	a_1	a_2	a_3	a

Range gate constraints:

$$w_{1,i}(w_{1,i}-1)(w_{1,i}-2)(w_{1,i}-3) + w_{2,i}(w_{2,i}-1)(w_{2,i}-2)(w_{2,i}-3) + w_{3,i}(w_{3,i}-1)(w_{3,i}-2)(w_{3,i}-3) + w_{4,i}(w_{4,i}-1)(w_{4,i}-2)(w_{4,i}-3)$$

$$w_{o,i} = w_{o,i-1} * 4^4 + w_{4,i} * 4^3 + w_{3,i} * 4^2 + w_{2,i} * 4 + w_{1,i}$$

The range proofs are included for each input data block.

The function σ_0 contain sparse mapping subcircuit with base 2. Let a be divided to a_0, a_1, a_2, a_3 8 bits-chunks. The values a'_0, a'_1, a'_2, a'_3 are in sparse form, and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 NORMALIZE2: Read a'_i to a_i
- 2. **SHA-256 8ROT3 32**: Read a'_1 to r_1
- 3. SHA-256 8ROT2 32: Read a'_4 to r_2
- 4. **SHA-256 8SHR3 32**: Read a'_0 to r_3

	w_1	w_2	w_3	w_4	w_o
j + 0	a_0	a_1	a_2	a_3	a
j + 1	a_0'	a'_1	a_2'	a_3'	acc
j+2	r1	r_2	r_3		σ_0

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + w_{2,j} * 2^8 + w_{3,j} * 2^{8*2} + w_{4,j} * 2^{8*3}$$

$$w_{o,j+1} = w_{2,j+1} * 4^{8-7} + w_{3,j+1} * 4^{8*2-7} + w_{4,j+1} * 4^{8*3-7} + w_{1,j+1} * 4^{8*2-2} + w_{2,j+1} * 4^{8*3-2} + w_{4,j+1} * 4^{8-2} + w_{2,j+1} * 4^{8-3} + w_{3,j+1} * 4^{8*2-3} + w_{4,j+1} * 4^{8^3-3}$$

$$w_{o,j+2} = w_{0,j+1} + w_{1,j+2} + w_{2,j+2} + w_{3,j+2}$$
 7 plookup constraints

The function σ_1 contain sparse mapping subcircuit with base 2. Let a be divided to a_0, a_1, a_2, a_3 8 bits-chunks. The values a'_0, a'_1, a'_2, a'_3 are in sparse form and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 NORMALIZE2: Read a_i to a'_i
- 2. **SHA-256 8ROT1 32**: Read a'_2 to r_1
- 3. **SHA-256 8ROT3 32**: Read a'_2 to r_2
- 4. **SHA-256 8ROT2 32**: Read a'_1 to r_3

	$ w_1 $	w_2	w_3	w_4	w_o
j + 0	a_0	a_1	a_2	a_3	a
j + 1	a_0'	a'_1	a_2'	a_3'	acc
j + 2	r1	r_2	r_3		σ_1

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + w_{2,j} * 2^8 + w_{3,j} * 2^{8*2} + w_{4,j} * 2^{8*3}$$

$$w_{o,j+1} = w_{1,j+1} * 4^{8*2-1} + w_{2,j+1} * 4^{8*3-1} + w_{4,j+1} * 4^{8-1} + w_{1,j+1} * 4^{8*2-3} + w_{2,j+1} * 4^{8*3-3} + w_{4,j+1} * 4^{8-3} + w_{1,j+1} * 4^{8^3-2} + w_{3,j+1} * 4^{8-2} + w_{4,j+1} * 4^{8^2-2}$$

$$w_{o,j+2} = w_{0,j+1} + w_{1,j+2} + w_{2,j+2} + w_{3,j+2}$$
 7 plookup constraints

The sparse values σ_0 and σ_1 have to be normalized. The final addition requires one add gate. We use **SHA256 NORMALIZE2**

Normalize gate constraints:

$$w_{o,j-1}=w_{4,j}*4^8*3+w_{3,j}*4^8*2+w_{2,j}*4^8+w_{1,j}$$

$$w_{o,j+1}=w_{4,j+1}*256^3+w_{3,j+1}*256^2+w_{2,j+1}*256+w_{1,j+1}$$
4 plookup constraints

The Σ_0 function—contain sparse mapping subcircuit with base 2. Let a be divided to a_0, a_1, a_2, a_3 8 bits-chunks. The values a'_0, a'_1, a'_2, a'_3 are in sparse form, and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 NORMALIZE2: Read a_i to a'_i
- 2. **SHA-256 8ROT2 32**: Read a'_0 to r_1
- 3. **SHA-256 8ROT5 32**: Read a'_1 to r_2
- 4. **SHA-256 8ROT6 32**: Read a'_2 to r_3

	w_1	w_2	w_3	w_4	w_o
j + 0	a_0	a_1	a_2	a_3	a
j + 1	a_0'	a'_1	a_2'	a_3'	\mathbf{a}'
j + 2	r1	r_2	r_3		Σ_0

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + w_{2,j} * 2^8 + w_{3,j} * 2^{8*2} + w_{4,j} * 2^{8*3}$$

$$w_{o,j+1} = w_{1,j+1} + w_{2,j+1} * 4^8 + w_{3,j+1} * 4^{8*2} + w_{4,j+1} * 4^{8*3}$$

$$w_{o,j+2} = w_{2,j+1} * 4^{8-2} + w_{3,j+1} * 4^{8*2-2} + w_{4,j+1} * 4^{8*3-2} + w_{1,j+1} * 4^{8*3-5} + w_{3,j+1} * 4^{8-5} + w_{4,j+1} * 4^{8*2-5} + w_{1,j+1} * 4^{8*2-6} + w_{2,j+1} * 4^{8*3-6} + w_{4,j+1} * 4^{8-6} + w_{1,j+2} + w_{2,j+2} + w_{3,j+2}$$
 7 plookup constraints

The Σ_1 function—contain sparse mapping subcircuit with base 2. Let a be divided to a_0, a_1, a_2, a_3 8 bits-chunks. The values a'_0, a'_1, a'_2, a'_3 are in sparse form, and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 NORMALIZE7: Read a_i to a'_i
- 2. **SHA-256 8ROT6 32**: Read a'_0 to r_1
- 3. **SHA-256 8ROT3 32**: Read a'_1 to r_2
- 4. **SHA-256 8ROT1 32**: Read a'_3 to r_3

	$ w_1 $	w_2	w_3	w_4	w_o
j+0	a_0	a_1	a_2	a_3	a
j + 1	a_0'	a'_1	a_2'	a_3'	a'
j+2	r1	r_2	r_3		Σ_1

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + w_{2,j} * 2^8 + w_{3,j} * 2^{8*2} + w_{4,j} * 2^{8*3}$$

$$w_{o,j+1} = w_{1,j+1} + w_{2,j+1} * 7^8 + w_{3,j+1} * 7^{8*2} + w_{4,j+1} * 7^{8*3}$$

$$w_{o,j+2} = w_{2,j+1} * 7^{8-6} + w_{3,j+1} * 7^{8*2-6} + w_{7,j+1} * 4^{8*3-6} + w_{1,j+1} * 7^{8*3-3} + w_{3,j+1} * 7^{8-3} + w_{4,j+1} * 7^{8*2-3} + w_{1,j+1} * 7^{8-1} + w_{2,j+1} * 7^{8*2-1} + w_{3,j+1} * 7^{8*3-1} + w_{1,j+2} + w_{2,j+2} + w_{3,j+2}$$
 7 plookup constraints

The sparse values Σ_0 and Σ_1 have to be normalized. We use **SHA256 NORMALIZE7**

	w_1	w_2	w_3	w_4	w_o
j+0	a'_0	a_1'	a_2'	a_3'	
j + 1	a_0	a_1	a_2	a_3	Σ_i

Normalize gate constraints:

The Maj function contain sparse mapping subcircuit with base 2 for a, b, c. Let a; b; c be divided to $a_0, a_1, a_2, a_3; b_0, b_1, b_2, b_3; c_0, c_1, c_2, c_3$ 8 bits-chunks. The values a'_0, a'_1, a'_2, a'_3 are in sparse form, and a' is a sparse a. Similarly for b and b. Note, that a we already have in the sparse from b0 in the circuit. The variables b and b0 were represented in sparse form in the previous rounds or it is public inputs.

	w_1	w_2	w_3	w_4	w_o
j - k	a'_0	a_1'	a_2'	a_3'	a'
 j - l	b_0'	b_1'	b_2'	b_3' b'	
j - t	c_0'	c_1'	c_2'	c_3'	c'
j + 0	a'	b'	c'		maj

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + w_{2,j} + w_{3,j}$$

The sparse values maj have to be normalized. We use **SHA256 MAJ NORMALIZE2**

	$ w_1 $	w_2	w_3	w_4	w_o
j + 0	a'_0	a'_1	a_2'	a_3'	
j + 1	a_0	a_1	a_2	a_3	maj

Normalize gate constraints:

$$w_{o,i} = w_{4,i} * 256^3 + w_{3,i} * 256^2 + w_{2,i} * 8 + w_{1,i}$$

The final addition requires one add gate.

The Ch function contain sparse mapping subcircuit with base 2 for e, f, g. Let e; f; g be divided to $e_0, e_1, e_2, e_3; f_0, f_1, f_2, f_3; g_0, g_1, g_2, g_3$ 8 bits-chunks. The values e'_0, e'_1, e'_2, e'_3 are in sparse form, and e' is a sparse e. Similarly for b and c. Note, that e we already have in the sparse from Σ_0 in the circuit. The variables f and g were represented in sparse form in the previous rounds or it is public inputs.

	w_1	w_2	w_3	w_4	w_o
j - k	a_0'	a_1'	a_2'	a_3'	a'
j - l	b'_0	b'_1	b_2'	b_3' b'	
j - t	c'_0	c_1'	c_2'	c_3'	c'
j + 0	a'	b'	c'		ch

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + 2 * w_{2,j} + 3 * w_{3,j}$$

The sparse values ch have to be normalized. We use **SHA256 CH NORMALIZE7**

	w_1	w_2	w_3	w_4	w_o
j + 0	a_0'	a_1'	a_2'	a_3'	
j + 1	a_0	a_1	a_2	a_3	ch

Normalize gate constraints:

$$w_{o,i} = w_{4,i} * 256^3 + w_{3,i} * 256^2 + w_{2,i} * 8 + w_{1,i}$$

The final addition requires one add gate.

The updating of variables for new rounds costs 10 add gates.

Producing the final hash value costs two add gates.

2.1 SHA-512

SHA-512 uses the similar logical functions as in refsha256 which operates on 64-bits words. Thus each input uses the same range proof which extended to 64-bits.

Range proof that $a < 2^{64}$ Let $a = \{a_0, ..., a_{32}\}$, where a_i is two bits.

	w_1	w_2	w_3	w_4	w_o
j + 0	a_{29}	a_{30}	a_{31}	a_{32}	acc
j + 1	a_{25}	a_{26}	a_{27}	a_{28}	acc
j + 6	a_4	a_5	a_6	a_7	acc
j + 7	a_0	a_1	a_2	a_3	a

Range gate constraints:

$$w_{1,i}(w_{1,i}-1)(w_{1,i}-2)(w_{1,i}-3) + w_{2,i}(w_{2,i}-1)(w_{2,i}-2)(w_{2,i}-3) + w_{3,i}(w_{3,i}-1)(w_{3,i}-2)(w_{3,i}-3) + w_{4,i}(w_{4,i}-1)(w_{4,i}-2)(w_{4,i}-3)$$

$$w_{o,i} = w_{o,i-1} * 4^4 + w_{4,i} * 4^3 + w_{3,i} * 4^2 + w_{2,i} * 4 + w_{1,i}$$

The range proofs are included for each input data block.

The function σ_0 contain sparse mapping subcircuit with base 2. Let a be divided to $a_0, a_1, a_2, ..., a_7$ 8 bits-chunks. The values $a'_0, a'_1, a'_2, ..., a'_7$ are in sparse form, and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 NORMALIZE2: Read a_i to a'_i
- 2. **SHA-256 8ROT1 64**: Read a'_0 to r_1
- 3. SHA-256 8SHR7 64: Read a'_0 to r_3

	$ w_1 $	w_2	w_3	w_4	w_o
j + 0	a_0	a_1	a_2	a_3	a_4
j + 1	a_0'	a_1'	a_2'	a_3'	a
j+2	a_5	a_6	a_7	a_4'	σ_0
j + 3	a_5'	a_6'	a_7'	r_1	r_2

Sparse map gate constraints:

$$w_{o,j+1} = w_{1,j} + w_{2,j} * 2^8 + w_{3,j} * 2^{8*2} + w_{4,j} * 2^{8*3} + w_{o,j} * 2^{8*4} + w_{1,j+2} * 2^{8*5} + w_{2,j+2} * 2^{8*6} + w_{3,j+2} * 2^{8*7} \\ w_{o,j+2} = w_{2,j+1} * 4^{8-1} + w_{3,j+1} * 4^{8*2-1} + w_{4,j+1} * 4^{8*3-1} + w_{4,j+2} * 4^{8*4-1} + w_{1,j+3} * 4^{8*5-1} + w_{2,j+3} * 4^{8*6-1} + w_{3,j+3} * 4^{8*7-1} + w_{1,j+1} * 4^{8*7} + w_{2,j+1} + w_{3,j+1} * 4^8 + w_{4,j+1} * 4^{8*2} + w_{4,j+2} * 4^{8*3} + w_{1,j+3} * 4^{8*4} + w_{2,j+3} * 4^{8*5} + w_{3,j+3} * 4^{8*6} + w_{2,j+1} * 4^{8-7} + w_{3,j+1} * 4^{8*2-7} + w_{4,j+1} * 4^{8*3-7} + w_{4,j+2} * 4^{8*4-7} + w_{4,j+3} * 4^{8*5-7} + w_{2,j+3} * 4^{8*5-7} + w_{2,j+3} * 4^{8*6-7} + w_{3,j+3} * 4^{8*7-7} + w_{4,j+3} + w_{0,j+3} \\ 10 \text{ plookup constraints}$$

The function σ_1 contain sparse mapping subcircuit with base 2. Let a be divided to $a_0, a_1, a_2, ..., a_7$ 8 bits-chunks. The values $a'_0, a'_1, a'_2, ..., a'_7$ are in sparse form, and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 NORMALIZE2: Read a_i to a'_i
- 2. **SHA-256 8ROT3 64**: Read a'_2 to r_1
- 3. **SHA-256 8ROT5 SHR6 64**: Read $a'_7 + a'_0$ to r_2

	w_1	w_2	w_3	w_4	w_o
j + 0	a_0	a_1	a_2	a_3	a_4
j + 1	a_0'	a'_1	a_2'	a_3'	a
j + 2	a_5	a_6	a_7	a_4'	σ_1
j+3	a_5'	a_6'	a_7'	r_1	r_2

Sparse map gate constraints:

$$w_{o,j+1} = w_{1,j} + w_{2,j} * 2^8 + w_{3,j} * 2^{8*2} + w_{4,j} * 2^{8*3} + w_{o,j} * 2^{8*4} + w_{1,j+2} * 2^{8*5} + w_{2,j+2} * 2^{8*6} + w_{3,j+2} * 2^{8*7} \\ w_{o,j+2} = w_{1,j+1} * 4^{64-19} + w_{2,j+1} * 4^{64+(8-19)} + w_{4,j+1} * 4^{8*3-19} + w_{4,j+2} * 4^{8*4-19} + w_{1,j+3} * 4^{8*5-19} + w_{2,j+3} * 4^{8*6-19} + w_{3,j+3} * 4^{8*7-19} + w_{1,j+1} * 4^{64-61} + w_{2,j+1} * 4^{64+(8-61)} + w_{3,j+1} * 4^{64+(8*2-61)} + w_{4,j+2} * 4^{64+(8*4-61)} + w_{1,j+3} * 4^{64+(8*5-61)} + w_{2,j+3} * 4^{64+(8*6-61)} + w_{2,j+1} * 4^{8-6} + w_{3,j+1} * 4^{8*2-6} + w_{4,j+2} * 4^{8*4-6} + w_{1,j+3} * 4^{8*5-6} + w_{2,j+3} * 4^{8*6-6} + w_{3,j+3} * 4^{8*7-6} + w_{4,j+3} + w_{o,j+3} \\ 10 \text{ plookup constraints}$$

The sparse values σ_0 and σ_1 have to be normalized. The final addition requires one add gate. Note, that a' already initialized in the row j-2. We use **SHA256 NORMALIZE2**

	w_1	w_2	w_3	w_4	w_o
j + 0	a'_0	a'_1	a_2'	a_3'	acc
j + 1	a_0	a_1	a_2	a_3	0
j + 2	a_4'	a_5'	a_6'	a_7'	σ_i
j + 3	a_4	a_5	a_6	a_7	

Normalize gate constraints:

$$w_{o,j+1} = \\ w_{4,j+1} * 256^3 + w_{3,j+1} * 256^2 + w_{2,j+1} * 256 + w_{1,j+1} + w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7 \\ w_{o,j} = w_{o,j-2} - (w_{4,j} * 256^3 + w_{3,j} * 256^2 + w_{2,j} * 256 + w_{1,j}) \\ w_{o,j+1} = w_{o,j} - (w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7) \\ 8 \text{ plookup constraints}$$

The Σ_0 function—contain sparse mapping subcircuit with base 2. Let a be divided to a_0, a_1, a_2, a_3 7-bits chunks and a_4, a_5, a_6, a_7 9 bits-chunks. The values $a'_0, a'_1, a'_2, ..., a'_7$ are in sparse form, and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 9NORMALIZE2: Read a_i to a'_i
- 2. SHA-256 7NORMALIZE2: Read a_i to a'_i
- 3. **SHA-256 9ROT6 32**: Read a'_4 to r_2
- 4. **SHA-256 9ROT2 32**: Read a'_5 to r_3

	$ w_1 $	$ w_2 $	w_3	w_4	w_o
j + 0	a_0	a_1	a_2	a_3	a_4
j + 1	a_0'	a_1'	a_2'	a_3'	a
j+2	a_5	a_6	a_7	a_4'	Σ_0
j+3	a_5'	a_6'	a_7'	r_1	r_2

Sparse map gate constraints:

$$w_{o,j+1} = \\ w_{1,j} + w_{2,j} * 2^7 + w_{3,j} * 2^{7*2} + w_{4,j} * 2^{7*3} + w_{o,j} * 2^{7*4} + w_{1,j+2} * 2^{7*4+9} + w_{2,j+2} * 2^{7*4+9*2} + w_{3,j+2} * 2^{7*4+9*3} \\ w_{o,j+2} = w_{4,j+2} + w_{1,j+3} * 4^9 + w_{2,j+3} * 4^{9*2} + w_{3,j+3} * 4^{9*3} + w_{1,j+1} * 4^{9*4} + w_{2,j+1} * 4^{9*4+7} + w_{3,j+1} * 4^{9*4+7*2} + w_{4,j+1} * 4^{9*4+7*3} + w_{1,j+1} * 4^{64-34} + w_{2,j+1} * 4^{64+(7-34)} + w_{3,j+1} * 4^{64+(7*2-34)} + w_{4,j+1} * 4^{64+(7*3-34)} + w_{1,j+3} * 4^{64+(7*4+9-34)} + w_{2,j+3} * 4^{64+(7*4+9*2-34)} + w_{3,j+3} * 4^{64+(7*4+9*3-34)} + w_{1,j+1} * 4^{64+(7*3-39)} + w_{4,j+1} * 4^{64+(7*3-39)} + w_{4,j+2} * 4^{64+(7*4-39)} + w_{2,j+3} * 4^{64+(7*4+9*2-39)} + w_{3,j+3} * 4^{64+(7*4+9*3-39)} + w_{4,j+3} + w_{o,j+3} \\ 10 \text{ plookup constraints}$$

The Σ_1 function—contain sparse mapping subcircuit with base 2. Let a be divided to a_0, a_1, a_2, a_3 7-bits chunks and a_4, a_5, a_6, a_7 9 bits-chunks. The values $a'_0, a'_1, a'_2, ..., a'_7$ are in sparse form, and a' is a sparse a. We need the following lookup tables:

- 1. SHA-256 9NORMALIZE2: Read a_i to a'_i
- 2. SHA-256 7NORMALIZE2: Read a_i to a'_i
- 3. **SHA-256 7ROT4 32**: Read a'_2 to r_2
- 4. SHA-256 9ROT4 32: Read a_5' to r_3

	$ w_1 $	w_2	w_3	w_4	w_o
j + 0	a_0	a_1	a_2	a_3	a_4
j + 1	a_0'	a'_1	a_2'	a_3'	a
j + 2	a_5	a_6	a_7	a_4'	Σ_0
j+3	a_5'	a_6'	a_7'	r_1	r_2

Sparse map gate constraints:

$$w_{o,j+1} = \\ w_{1,j} + w_{2,j} * 2^7 + w_{3,j} * 2^{7*2} + w_{4,j} * 2^{7*3} + w_{o,j} * 2^{7*4} + w_{1,j+2} * 2^{7*4+9} + w_{2,j+2} * 2^{7*4+9*2} + w_{3,j+2} * 2^{7*4+9*3} \\ w_{o,j+2} = w_{3,j+1} + w_{4,j+1} * 7^7 + w_{4,j+2} * 7^{7*2} + w_{1,j+3} * 7^{7*2+9} + w_{2,j+3} * 7^{7*2+9*2} + w_{3,j+3} * 7^{9*3+7*2} + \\ w_{1,j+1} * 7^{9*4+7*2} + w_{2,j+1} * 7^{9*4+7*3} + w_{1,j+1} * 7^{64-18} + w_{2,j+1} * 7^{64+(7-18)} + w_{4,j+1} * 7^{64+(7*4-18)} + \\ + w_{4,j+2} * 7^{64+(7*4+9-18)} + w_{1,j+3} * 7^{64+(7*4+9*2-18)} + w_{2,j+3} * 7^{64+(7*4+9*3-18)} + w_{3,j+3} * \\ 7^{64+(7*4+9*-18)} + w_{1,j+1} * 7^{64-41} + w_{2,j+1} * 7^{64+(7-41)} + w_{3,j+1} * 7^{64+(7*2-41)} + w_{4,j+1} * 7^{64+(7*3-41)} + \\ w_{4,j+2} * 7^{64+(7*3+9-41)} + w_{2,j+3} * 7^{64+(7*3+9*2-41)} + w_{3,j+3} * 7^{64+(7*3+9*3-41)} + w_{4,j+3} + w_{o,j+3} \\ 10 \text{ plookup constraints}$$

The sparse values Σ_0 and Σ_1 have to be normalized. We use **SHA256 NORMALIZE7** Note, that a' already initialized in the row j-2.

		w_1	w_2	w_3	w_4	w_o
j	+ 0	a'_0	a_1'	a_2'	a_3'	a'
j	+ 1	a_0	a_1	a_2	a_3	acc
j	+ 2	a_4'	a_5'	a_6'	a_7'	σ_i
j	+ 3	a_4	a_5	a_6	a_7	

Normalize gate constraints:

$$w_{o,j+1} = \\ w_{4,j+1} * 256^3 + w_{3,j+1} * 256^2 + w_{2,j+1} * 256 + w_{1,j+1} + w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7 \\ w_{o,j} = w_{1,j-3} + w_{2,j-3} * 4^7 + w_{3,j-3} * 4^{7*2} + + w_{4,j-3} * 4^{7*3} + w_{4,j-2} * 4^{7*4} + w_{1,j-1} * 7^{7*4+9} + w_{2,j-1} * 7^{7*4+9*2} + w_{2,j-1} * 7^{7*4+9*3} \text{ for maj or ch function. for } \Sigma_1 \text{ replace } 4 \text{ with } 7 \\ w_{o,j} = w_{o,j-2} - (w_{4,j} * 256^3 + w_{3,j} * 256^2 + w_{2,j} * 256 + w_{1,j}) \\ w_{o,j+1} = w_{o,j} - (w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7) \\ 8 \text{ plookup constraints}$$

The Maj function contain sparse mapping subcircuit with base 2 for a, b, c. Note, that the sparse chunks of a we already have in Σ_0 in the circuit. The variables b and c were represented in sparse chunks in the previous rounds or it is public inputs.

	w_1	w_2	w_3	w_4	w_o
j	a'	b'	c'		maj

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + w_{2,j} + w_{3,j}$$

The sparse values maj have to be normalized. We use **SHA256 MAJ NORMALIZE2** Note, that maj already initialized in the row j-1.

	w_1	w_2	w_3	w_4	w_o
j + 0	a_0'	a'_1	a_2'	a_3'	acc
j + 1	a_0	a_1	a_2	a_3	0
j+2	a_4'	a_5'	a_6'	a_7'	maj
j+3	a_4	a_5	a_6	a_7	

Normalize gate constraints:

$$w_{o,j+1} = \\ w_{4,j+1} * 256^3 + w_{3,j+1} * 256^2 + w_{2,j+1} * 256 + w_{1,j+1} + w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7 \\ w_{o,j} = w_{o,j-1} - (w_{4,j} * 256^3 + w_{3,j} * 256^2 + w_{2,j} * 256 + w_{1,j}) \\ w_{o,j+1} = w_{o,j} - (w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7) \\ 8 \text{ plookup constraints}$$

The final addition requires one add gate.

The Ch function contain sparse mapping subcircuit with base 2 for e, f, g. Note, that e we already have in the sparse from Σ_1 in the circuit. The variables f and g were represented in sparse form in the previous rounds or it is public inputs.

Sparse map gate constraints:

$$w_{o,j} = w_{1,j} + 2 * w_{2,j} + 3 * w_{3,j}$$

The sparse values ch have to be normalized. Note, that ch already initialized in the row j-1. We use **SHA256 CH NORMALIZE7**

	w_1	w_2	w_3	w_4	w_o
j + 0	a'_0	a_1'	a_2'	a_3'	acc
j + 1	a_0	a_1	a_2	a_3	0
j + 2	a_4'	a_5'	a_6'	a_7'	ch
j+3	a_4	a_5	a_6	a_7	

Normalize gate constraints:

$$w_{o,j+1} = \\ w_{4,j+1} * 256^3 + w_{3,j+1} * 256^2 + w_{2,j+1} * 256 + w_{1,j+1} + w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7 \\ w_{o,j} = w_{o,j-1} - (w_{4,j} * 256^3 + w_{3,j} * 256^2 + w_{2,j} * 256 + w_{1,j}) \\ w_{o,j+1} = w_{o,j} - (w_{1,j+3} * 256^4 + w_{2,j+3} * 256^5 + w_{3,j+3} * 256^6 + w_{4,j+4} * 256^7) \\ 8 \text{ plookup constraints}$$

The final addition requires one add gate.

The updating of variables for new rounds costs 10 add gates.

Producing the final hash value costs two add gates.

3 Poseidon Circuit

WIP

For now, there are two SNARK-friendly hash function candidates: Poseidon¹ and Reinforce Concrete².

4 Merkle Tree Circuit

Merkle Tree generation for set $\{H_{B_{n_1}},...,H_{B_{n_2}}\}$. Let $k = \lceil \log(n_2 - n_1) \rceil$

- 1. $n = n_2 n_1$
- $2. \ 2^k = n$
- 3. for i from 0 to n-1:
 - 3.1 $T_i = H_i$ // just notation for simplicity, not a real part of the circuit
- 4. for i from 0 to k-1:
 - 4.1 for j from 0 to (n-1)/2:

4.1.1
$$T'_i = hash(T_{2\cdot i}, T_{2\cdot i+1})$$
. // see Section 3

- $4.2 \ n = \frac{n}{2}$
- 4.3 for j from 0 to n-1:
 - 4.3.1 $T_i = T'_i$. // just notation for simplicity, not a real part of the circuit

5 Ed25519 Circuit

To verify a signature (R, s) on message M using public key A and a generator B do:

- 1. Prove that s in the defined range.
- 2. k = SHA-512(data||R||A||M) //See section 2.1
- 3. 8sB? = ?8R + 8kA //See section 5.1

5.1 The Arithmetic of Elliptic Curves

Variable-base scalar multiplication circuit per bit b:

- 1. $b^2 = b$
- 2. $(y_1)(2b-1)=(y_2)$
- 3. $(x_2 x_3)(\lambda_1) = (y_2 y_3)$
- 4. $(B\lambda_1)(\lambda_1) = (A + x_3 + x_2 + x_4)$
- 5. $(x_3 x_4)(\lambda_1 + \lambda_2) = (2y_3)$
- 6. $(B\lambda_2)(\lambda_2) = (A + x_4 + x_3 + x_5)$
- 7. $(x_3 x_5)(\lambda_2) = (y_5 + y_3)$

EC Point Addition circuit:

1.
$$(x_2-x_1)(y_3+y_1)-(y_1-y_2)(x_1-x_3)$$

2.
$$(x_1 + x_2 + x_3)(x_1 - x_3)(x_1 - x_3) - (y_3 + y_1)(y_3 + y_1)$$

¹https://www.poseidon-hash.info

²https://www.rc-hash.info

6 The Correct Validator Set Proof Circuit

WIP

7 Bringing it all together

Let bank-hashes of proving block set be $\{H_{B_{n_1}},...,H_{B_{n_2}}\}$. The last confirmed block is H_{B_L} . Each positively confirmed block is signed by M validators.

Denote by block_data the data that is included in the bank hash other than the bank hash of the parent block.

- 1. $H_{B_{n_1}} = H_{B_L} // H_{B_L}$ is a public input
- 2. Validator set constraints. // see Section 6
- 3. for *i* from $n_1 + 1$ to $n_2 + 32$:
 - 3.1 $H_{B_i} = \text{sha256(block_data}||H_{B_{i-1}})$ // see Section 2
- 4. for j from 0 to M:
 - 4.1 Ed25519 constraints for $H_{B_{n_2+32}}$ // see Section 5
- 5. Merkle tree constraints for the set $\{H_{B_{n_1}},...,H_{B_{n_2}}\}$ // see Section 4

References