

Beyond Tit-for-Tat Proposal - Melt

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Abstract

Beyond Tit-for-tat: Set up a repeated prisoner's dilemma computer tournament, in which strategies compete against each other. Write a report on your findings.

1. Introduction

The phrase horses for courses alludes to the fact that a racehorse performs best on a racecourse to which it is specifically suited. More generally this idiom is used to express that certain tools and strategies are better suited over others depending on the task or situations at hand. In the context of the repeated prisoners' dilemma, the strategy of tit-for-tat, where one mimics their opponent's previous move, reigns supreme and is best suited over others for the situation at hand¹.

The question this paper aims to answer is as to which situations is tit-for-tat not the dominant strategy. To do this we have to venture down two potential avenues. The first is the adjustment of pay-off values within games, and the second is adjusting pay-off values from games. Consider a standard prisoners' dilemma pay-off table:

| Player 1 / Player 2 | C (Cooperate) | D (Defect) |
|---------------------|---------------|------------|
| C (Cooperate) | (R, R) | (S, T) |
| D (Defect) | (T, S) | (P, P) |

Table 1.1: Prisoner's Dilemma Payoff Matrix with R , P , S , and T Outcomes

Adjusting the values of R (Reward for mutual cooperation), P (Punishment for mutual defection), S (Sucker's pay-off for cooperating while the other defects), and T (Temptation to defect when the other cooperates) is an example of within game pay-off adjustments. These adjustments might produce a new dominant strategy and our analysis aims to find if it does.

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¹The tic-for-tat strategy is the dominant strategy in Axelrod (1980)

From-game adjustments are a bit different and it considers the utility a player gets from the payoffs of its opponent.

| Player 1 / Player 2 | C (Cooperate) | D (Defect) |
|---------------------|------------------------------|------------------------------|
| C (Cooperate) | $(R(1-p) + Rp, R(1-p) + Rp)$ | $(S(1-p) + Tp, T(1-p) + Sp)$ |
| D (Defect) | $(T(1-p) + Sp, S(1-p) + Tp)$ | $(P(1-p) + Pp, P(1-p) + Pp)$ |

Table 1.2: Prisoner's Dilemma Payoff Matrix

The level p here is adapted from Charness & Rabin (2002) who created a utility function that captures various social preferences. In essence, p is how much you care about your opponent's pay-offs as well as your own. In standard prisoners' dilemma games, this is 0 and thus people are purely self-interested. If we let our pay-offs be $R = 3$, $T = 5$, $S = 0$, and $P = 3$, then this situation in strategic form would look like:

| Player 1 / Player 2 | C (Cooperate) | D (Defect) |
|---------------------|---------------|------------|
| C (Cooperate) | (3, 3) | (0, 5) |
| D (Defect) | (5, 0) | (1, 1) |

Table 1.3: Prisoner's Dilemma Payoff Matrix for $p = 0$ (Self-interested person)

However we can adjust the value of p for people who are partially considerate of other people's outcomes, or we can make people egalitarian who care just as much for others as they do for themselves.

| Player 1 / Player 2 | C (Cooperate) | D (Defect) |
|---------------------|---------------|------------|
| C (Cooperate) | (3, 3) | (1, 4) |
| D (Defect) | (4, 1) | (1, 1) |

Table 1.4: Prisoner's Dilemma Payoff Matrix for $p = 0.2$ (Partially considers others' outcomes)

| Player 1 / Player 2 | C (Cooperate) | D (Defect) |
|---------------------|---------------|------------|
| C (Cooperate) | (3, 3) | (2.5, 2.5) |
| D (Defect) | (2.5, 2.5) | (1, 1) |

Table 1.5: Prisoner's Dilemma Payoff Matrix for $p = 0.5$ (Egalitarian person)

p could also take a negative value, which indicates a person is status-seeking and actively wants to bring down their opponent.

| Player 1 / Player 2 | C (Cooperate) | D (Defect) |
|---------------------|---------------|------------|
| C (Cooperate) | (3.6, 3.6) | (−1, 6) |
| D (Defect) | (6, −1) | (0.8, 0.8) |

Table 1.6: Prisoner’s Dilemma Payoff Matrix for $p = -0.2$ (Negative influence by others’ outcomes)

It would be interesting to see under which values of p the dominant strategy changes.

2. Literature Review

We aim to do a short literature review and provide insight from the following sources: Lange & Baylor (2007), Farrell & Ware (1989), Kreps, Milgrom, Roberts & Wilson (1982), Romero & Rosokha (2018), Bó & Fréchette (2019), Breitmoser (2015), Gaudesi, Piccolo, Squillero & Tonda (2016), García & Veelen (2018), Embrey, Fréchette & Yuksel (2018).

Most importantly we aim to structure our output in tables similar to Axelrod (1980).

3. Game Construction

Notes: There are 25 strategies. Each strategy plays everyone else and itself once for 200 rounds. How each variable fairs against each other is recorded

1. Always Strategies:
 - Always Cooperate
 - Always Defect
2. Tit for Tat Variants:
 - Tit for Tat
 - Tit for Two Tats
 - Tit for Tat with Forgiveness
 - Tit for Tat with Randomization
3. Win-Stay/Lose-Switch Strategies:

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- Pavlov
4. Punishment-Based Strategies:
- Grim Trigger
 - Bully
 - Retaliatory Defector
5. Adaptive/Adjusting Strategies:
- Adaptive Defector
 - Adaptive Peacekeeper
 - Probing Adjuster
 - Forgiving Tester
 - Prober
 - Cautious Rebuilder
6. Gradient/Probability-Based Strategies:
- Progressive Cooperator (Gradually increases cooperation)
 - Diminishing Cooperator (Gradually decreases cooperation)
 - Bounded Gradient (Probability based on the opponent's entire history)
 - Recent Gradient (Probability based on recent actions of the opponent)
7. Random Strategies:
- Random 10%
 - Random 25%
 - Random 50%
 - Random 75%
 - Random 90%

4. Game Results

Talk about game results for a single p-value being 0. Talk about how probing adjuster won. Yet without Adaptive/Adjusting Strategies, then Grim-trigger won. Game results are mostly based on what strategies are in

Table 4.1: Tournament Payoff Matrix for $p=0$

| | Payoff Against Other Strategies | | | | | | | | | | | | | | | | | | | | | | | | | Total | Rank |
|--------------------------------|---------------------------------|-----|-----|------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|------|-----|-----|-----|-----|------|------|-------|------|-------|------|-------|------|
| | AC | AD | TfT | Tf2T | TfTF | TfTR | P | G/T | B | RD | ADe | APe | PA | FT | P | CR | PC | DC | BG | RG | R0.1 | R0.25 | R0.5 | R0.75 | R0.9 | | |
| Always Cooperate | 600 | 0 | 600 | 600 | 600 | 600 | 600 | 600 | 147 | 600 | 600 | 501 | 3 | 453 | 600 | 483 | 291 | 261 | 600 | 600 | 69 | 156 | 300 | 420 | 519 | 10803 | 24 |
| Always Defect | 1000 | 200 | 204 | 208 | 276 | 204 | 204 | 204 | 396 | 992 | 204 | 212 | 208 | 212 | 1000 | 212 | 664 | 600 | 204 | 1000 | 276 | 392 | 648 | 792 | 896 | 11408 | 20 |
| Tit for Tat | 600 | 199 | 600 | 600 | 600 | 600 | 600 | 600 | 346 | 600 | 600 | 567 | 399 | 551 | 600 | 561 | 441 | 426 | 600 | 600 | 250 | 344 | 432 | 531 | 580 | 12827 | 4 |
| Tit for Two Tats | 600 | 198 | 600 | 600 | 600 | 600 | 600 | 600 | 296 | 600 | 600 | 501 | 298 | 453 | 600 | 483 | 372 | 370 | 600 | 600 | 244 | 288 | 394 | 480 | 548 | 12125 | 15 |
| Tit for Tat with Forgiveness | 600 | 183 | 600 | 600 | 600 | 600 | 600 | 600 | 322 | 600 | 600 | 561 | 370 | 539 | 600 | 553 | 408 | 411 | 600 | 600 | 249 | 321 | 403 | 527 | 571 | 12618 | 8 |
| Tit for Tat with Randomisation | 600 | 199 | 600 | 600 | 600 | 600 | 600 | 600 | 346 | 600 | 600 | 567 | 399 | 551 | 600 | 561 | 422 | 436 | 600 | 600 | 252 | 357 | 478 | 542 | 577 | 12887 | 2 |
| Pavlov | 600 | 199 | 600 | 600 | 600 | 600 | 600 | 600 | 346 | 600 | 600 | 567 | 399 | 551 | 600 | 561 | 453 | 434 | 600 | 600 | 243 | 325 | 442 | 519 | 582 | 12821 | 5 |
| Grim/Trigger | 600 | 199 | 600 | 600 | 600 | 600 | 600 | 600 | 395 | 600 | 600 | 223 | 205 | 219 | 600 | 221 | 607 | 575 | 600 | 600 | 263 | 399 | 551 | 823 | 933 | 12813 | 6 |
| Bully | 902 | 151 | 351 | 551 | 399 | 351 | 351 | 155 | 298 | 894 | 155 | 683 | 355 | 751 | 902 | 631 | 533 | 554 | 348 | 902 | 230 | 319 | 556 | 700 | 847 | 12869 | 3 |
| Retaliatory Defector | 600 | 2 | 600 | 600 | 600 | 600 | 600 | 600 | 149 | 600 | 600 | 505 | 9 | 457 | 600 | 487 | 263 | 283 | 600 | 600 | 74 | 122 | 319 | 463 | 541 | 10874 | 23 |
| Adaptive Defector | 600 | 199 | 600 | 600 | 600 | 600 | 600 | 600 | 395 | 600 | 600 | 501 | 205 | 453 | 600 | 483 | 448 | 420 | 600 | 600 | 276 | 387 | 457 | 487 | 548 | 12459 | 10 |
| Adaptive Peacekeep | 666 | 197 | 567 | 666 | 576 | 567 | 567 | 213 | 263 | 660 | 666 | 534 | 256 | 503 | 666 | 543 | 418 | 400 | 572 | 666 | 223 | 285 | 393 | 483 | 600 | 12150 | 14 |
| Probing Adjuster | 998 | 198 | 404 | 553 | 436 | 404 | 404 | 205 | 345 | 989 | 205 | 591 | 400 | 557 | 998 | 643 | 587 | 544 | 325 | 998 | 264 | 369 | 549 | 719 | 890 | 13575 | 1 |
| Forgiving Tester | 698 | 197 | 551 | 698 | 563 | 551 | 551 | 209 | 246 | 692 | 698 | 583 | 297 | 502 | 698 | 572 | 452 | 431 | 565 | 698 | 239 | 275 | 393 | 543 | 631 | 12533 | 9 |
| Prober | 600 | 0 | 600 | 600 | 600 | 600 | 600 | 600 | 147 | 600 | 600 | 501 | 3 | 453 | 600 | 483 | 324 | 303 | 600 | 600 | 63 | 156 | 318 | 492 | 540 | 10983 | 21 |
| Cautious Rebuilder | 678 | 197 | 561 | 678 | 576 | 561 | 561 | 211 | 276 | 672 | 678 | 573 | 238 | 522 | 678 | 522 | 413 | 385 | 554 | 678 | 229 | 270 | 402 | 541 | 641 | 12295 | 11 |
| Progressive Cooperator | 798 | 102 | 439 | 557 | 484 | 417 | 414 | 105 | 271 | 794 | 444 | 546 | 203 | 503 | 790 | 504 | 417 | 467 | 289 | 798 | 159 | 247 | 506 | 658 | 742 | 11654 | 18 |
| Deminishing Cooperator | 784 | 109 | 438 | 536 | 454 | 432 | 447 | 141 | 263 | 799 | 410 | 543 | 235 | 487 | 818 | 522 | 499 | 431 | 619 | 798 | 176 | 262 | 435 | 653 | 715 | 12006 | 16 |
| Bounded Gradient | 600 | 199 | 600 | 600 | 600 | 600 | 600 | 600 | 342 | 600 | 600 | 564 | 245 | 520 | 600 | 545 | 513 | 325 | 600 | 600 | 273 | 374 | 442 | 540 | 566 | 12648 | 7 |
| Recent Gradient | 600 | 0 | 600 | 600 | 600 | 600 | 600 | 600 | 147 | 600 | 600 | 501 | 3 | 453 | 600 | 483 | 285 | 312 | 600 | 600 | 84 | 150 | 291 | 462 | 549 | 10920 | 22 |
| Random 10% | 960 | 184 | 255 | 340 | 354 | 251 | 267 | 182 | 381 | 966 | 184 | 325 | 266 | 375 | 938 | 351 | 589 | 560 | 242 | 976 | 238 | 381 | 542 | 812 | 882 | 11801 | 17 |
| Random 25% | 886 | 149 | 367 | 452 | 415 | 353 | 354 | 156 | 329 | 900 | 233 | 533 | 314 | 406 | 900 | 508 | 553 | 498 | 353 | 904 | 216 | 364 | 564 | 695 | 809 | 12211 | 13 |
| Random 50% | 794 | 100 | 428 | 654 | 497 | 460 | 469 | 105 | 260 | 803 | 480 | 634 | 259 | 576 | 806 | 565 | 427 | 467 | 448 | 806 | 188 | 257 | 445 | 625 | 710 | 12263 | 12 |
| Random 75% | 714 | 59 | 538 | 656 | 538 | 525 | 536 | 77 | 217 | 692 | 643 | 609 | 151 | 536 | 726 | 574 | 377 | 358 | 530 | 704 | 107 | 224 | 325 | 532 | 660 | 11608 | 19 |
| Random 90% | 630 | 21 | 570 | 634 | 581 | 572 | 577 | 64 | 169 | 628 | 631 | 541 | 94 | 471 | 620 | 517 | 319 | 324 | 555 | 634 | 76 | 147 | 329 | 460 | 591 | 10755 | 25 |

4.1. Social preferences

Above was all to do with a single p-value.

Below is all the outcomes for when social preferences vary. We see that

Table 4.2: Strategy Rankings Across Different p Values

| Strategy | p Values | | | | | | | | | | | | |
|---------------------------------------|----------|-------|----|------|-----|------|-----|------|-----|------|-----|------|-----|
| | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.15 | 0.2 | 0.25 | 0.3 | 0.35 | 0.4 | 0.45 | 0.5 |
| Always Cooperate | 25 | 24 | 25 | 22 | 19 | 19 | 14 | 10 | 4 | 4 | 4 | 1 | 3 |
| Always Defect | 15 | 18 | 20 | 25 | 25 | 25 | 25 | 25 | 25 | 25 | 25 | 25 | 25 |
| Tit for Tat | 5 | 4 | 3 | 3 | 3 | 1 | 2 | 4 | 5 | 8 | 8 | 11 | 9 |
| Tit for Two Tats | 18 | 16 | 15 | 13 | 11 | 7 | 6 | 5 | 9 | 6 | 6 | 6 | 6 |
| Tit for Tat with Forgiveness | 10 | 8 | 7 | 5 | 4 | 4 | 4 | 3 | 6 | 7 | 7 | 7 | 8 |
| Tit for Tat with Randomisation | 4 | 6 | 5 | 4 | 1 | 2 | 1 | 2 | 7 | 9 | 10 | 8 | 11 |
| Pavlov | 6 | 5 | 2 | 2 | 2 | 3 | 3 | 1 | 8 | 10 | 9 | 9 | 10 |
| Grim/Trigger | 3 | 3 | 4 | 7 | 9 | 9 | 15 | 18 | 18 | 18 | 19 | 19 | 20 |
| Bully | 2 | 2 | 8 | 8 | 10 | 15 | 20 | 21 | 22 | 21 | 21 | 21 | 21 |
| Retaliatory Defector | 23 | 21 | 22 | 20 | 17 | 16 | 10 | 9 | 1 | 3 | 2 | 3 | 4 |
| Adaptive Defector | 12 | 10 | 11 | 9 | 7 | 8 | 7 | 11 | 13 | 13 | 13 | 13 | 14 |
| Adaptive Peacekeep | 17 | 14 | 13 | 14 | 13 | 10 | 12 | 13 | 15 | 14 | 14 | 14 | 13 |
| Probing Adjuster | 1 | 1 | 1 | 1 | 5 | 12 | 19 | 20 | 21 | 22 | 22 | 22 | 22 |
| Forgiving Tester | 9 | 9 | 9 | 10 | 8 | 6 | 8 | 12 | 14 | 15 | 15 | 16 | 16 |
| Prober | 21 | 22 | 24 | 24 | 21 | 17 | 13 | 8 | 3 | 1 | 1 | 2 | 1 |
| Cautious Rebuilder | 14 | 12 | 12 | 12 | 12 | 11 | 9 | 16 | 16 | 16 | 16 | 15 | 15 |
| Progressive Cooperator | 19 | 20 | 17 | 18 | 23 | 22 | 22 | 22 | 20 | 20 | 20 | 20 | 19 |
| Deminishing Cooperator | 16 | 17 | 16 | 15 | 16 | 20 | 21 | 19 | 19 | 19 | 18 | 18 | 18 |
| Bounded Gradient | 8 | 7 | 6 | 6 | 6 | 5 | 5 | 6 | 10 | 11 | 12 | 12 | 12 |
| Recent Gradient | 22 | 25 | 23 | 21 | 18 | 18 | 11 | 7 | 2 | 2 | 3 | 4 | 2 |
| Random 10% | 11 | 15 | 18 | 19 | 24 | 24 | 24 | 24 | 24 | 24 | 24 | 24 | 24 |
| Random 25% | 7 | 13 | 14 | 16 | 19 | 23 | 23 | 23 | 23 | 23 | 23 | 23 | 23 |
| Random 50% | 13 | 11 | 10 | 11 | 14 | 13 | 18 | 17 | 17 | 17 | 17 | 17 | 17 |
| Random 75% | 20 | 19 | 19 | 17 | 15 | 14 | 16 | 15 | 12 | 12 | 11 | 10 | 7 |
| Random 90% | 24 | 23 | 21 | 23 | 22 | 21 | 17 | 14 | 11 | 5 | 5 | 5 | 5 |

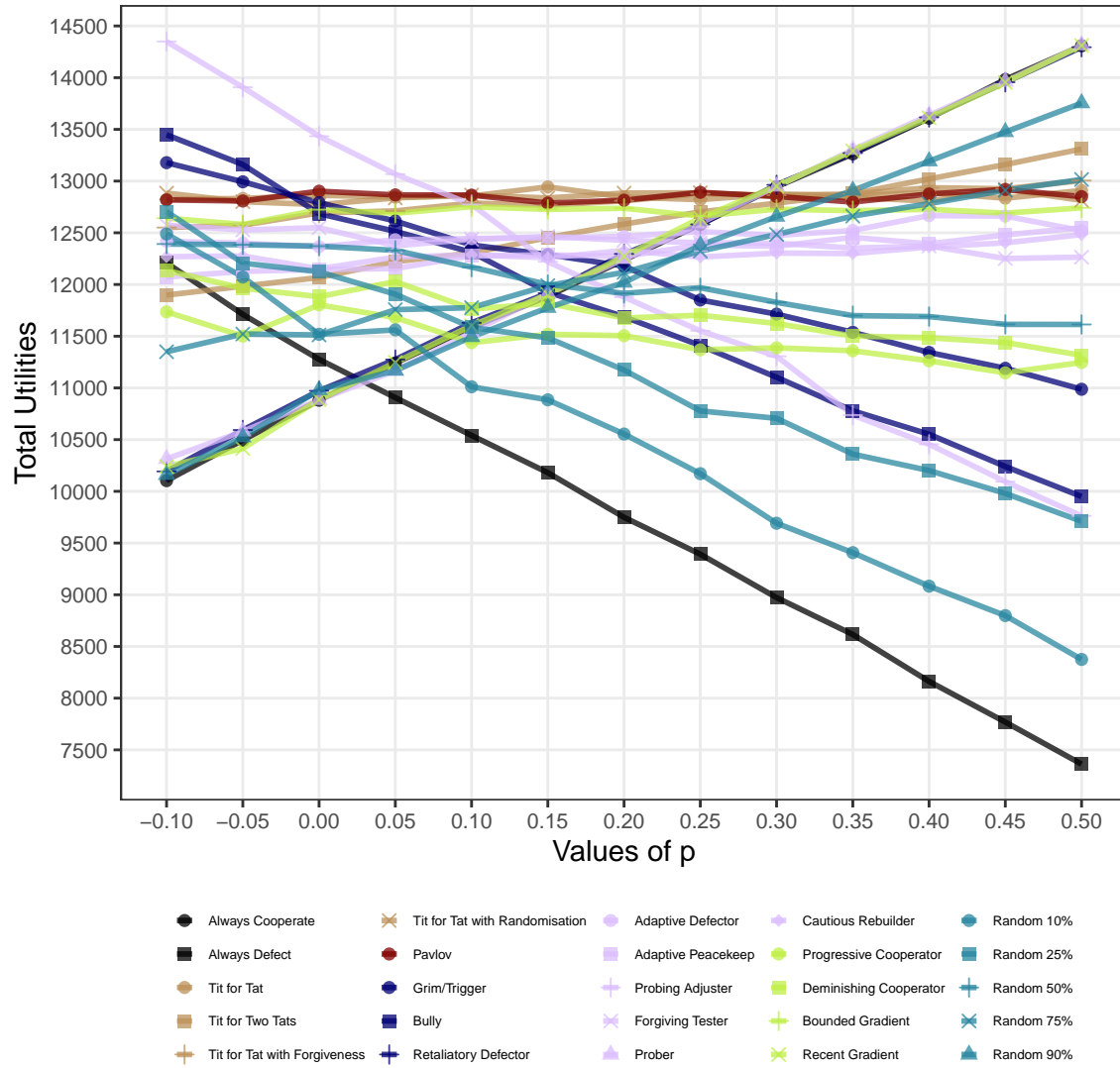


Figure 4.1: Strategies' Total Utilities for Different Strategies Across p

Table 4.3: Strategy Values Across Different p Values

| Strategy | p Values | | | | | | | | | | | | |
|---------------------------------------|----------|----------|-------|----------|---------|----------|-------|----------|---------|----------|-------|----------|---------|
| | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.15 | 0.2 | 0.25 | 0.3 | 0.35 | 0.4 | 0.45 | 0.5 |
| Always Cooperate | 10103.5 | 10495.5 | 10881 | 11240.75 | 11585 | 11886 | 12238 | 12579.75 | 12945 | 13262.5 | 13608 | 13982.25 | 14308 |
| Always Defect | 12209 | 11710.75 | 11276 | 10906.25 | 10540.5 | 10180.5 | 9749 | 9391.75 | 8972.5 | 8615.75 | 8162 | 7768.5 | 7362.5 |
| Tit for Tat | 12824 | 12832 | 12863 | 12844.5 | 12856 | 12943.5 | 12845 | 12820.5 | 12875.5 | 12856.25 | 12891 | 12834.75 | 12908.5 |
| Tit for Two Tats | 11897.5 | 11983.5 | 12067 | 12221.25 | 12304 | 12453.5 | 12584 | 12701.5 | 12786.5 | 12878.25 | 13021 | 13159.75 | 13310.5 |
| Tit for Tat with Forgiveness | 12551 | 12573.75 | 12692 | 12711.5 | 12787.5 | 12766 | 12809 | 12878 | 12863.5 | 12874.5 | 12936 | 12926 | 13004.5 |
| Tit for Tat with Randomisation | 12883.5 | 12801.25 | 12772 | 12837.25 | 12864.5 | 12836.5 | 12884 | 12886.75 | 12854 | 12843.25 | 12806 | 12920.5 | 12813.5 |
| Pavlov | 12818 | 12807.5 | 12902 | 12866.5 | 12864 | 12787.25 | 12815 | 12891.5 | 12851 | 12797.25 | 12875 | 12919.5 | 12849.5 |
| Grim/Trigger | 13178 | 12993 | 12791 | 12613.75 | 12382 | 12289.25 | 12178 | 11850.25 | 11713.5 | 11537.75 | 11343 | 11189.75 | 10987 |
| Bully | 13447.5 | 13160 | 12685 | 12513.75 | 12312 | 11926.25 | 11688 | 11410 | 11103 | 10778.75 | 10552 | 10240.25 | 9950 |
| Retaliatory Defector | 10192.5 | 10593 | 10972 | 11274.25 | 11629.5 | 11915.75 | 12296 | 12581 | 12963.5 | 13270.25 | 13616 | 13955.5 | 14294.5 |
| Adaptive Defector | 12417.5 | 12400.25 | 12365 | 12433 | 12444.5 | 12452 | 12465 | 12511.5 | 12474.5 | 12522.75 | 12666 | 12661.75 | 12520.5 |
| Adaptive Peacekeep | 12071.5 | 12127 | 12145 | 12154.5 | 12277 | 12286.75 | 12271 | 12382 | 12370 | 12455.5 | 12393 | 12479.75 | 12549 |
| Probing Adjuster | 14349.5 | 13907 | 13434 | 13067 | 12773.5 | 12220.5 | 11878 | 11552.25 | 11306 | 10737.25 | 10455 | 10093.5 | 9762.5 |
| Forgiving Tester | 12574 | 12528 | 12549 | 12374.5 | 12437 | 12464.5 | 12427 | 12404 | 12399.5 | 12352.25 | 12372 | 12251.25 | 12264.5 |
| Prober | 10313.5 | 10580 | 10884 | 11166.5 | 11537.5 | 11910.75 | 12248 | 12593.75 | 12948 | 13302.5 | 13637 | 13962 | 14313.5 |
| Cautious Rebuilder | 12268.5 | 12276.25 | 12152 | 12263.5 | 12287 | 12258.25 | 12329 | 12265.5 | 12303.5 | 12299 | 12363 | 12403 | 12482.5 |
| Progressive Cooperator | 11735.5 | 11501.25 | 11803 | 11680.25 | 11437.5 | 11518.25 | 11505 | 11369 | 11387.5 | 11359.5 | 11262 | 11146.25 | 11245.5 |
| Deminishing Cooperator | 12135 | 11963.25 | 11882 | 12028 | 11763.5 | 11817 | 11676 | 11703 | 11622.5 | 11501.75 | 11485 | 11439 | 11315.5 |
| Bounded Gradient | 12641.5 | 12580.75 | 12724 | 12688.75 | 12752.5 | 12726.5 | 12737 | 12661.25 | 12728.5 | 12713.75 | 12727 | 12690 | 12741.5 |
| Recent Gradient | 10240 | 10414.25 | 10887 | 11246.25 | 11602.5 | 11904 | 12272 | 12642.75 | 12951 | 13291.25 | 13613 | 13953.75 | 14311 |
| Random 10% | 12488 | 12072.5 | 11518 | 11561 | 11011 | 10884.75 | 10554 | 10170.75 | 9691.5 | 9407 | 9083 | 8798.25 | 8374.5 |
| Random 25% | 12705.5 | 12206.75 | 12123 | 11906 | 11585 | 11484 | 11173 | 10777.75 | 10706 | 10359.75 | 10201 | 9980.25 | 9710 |
| Random 50% | 12391.5 | 12384.25 | 12371 | 12330.25 | 12168 | 12000 | 11914 | 11968.5 | 11827.5 | 11699.25 | 11690 | 11614.5 | 11613.5 |
| Random 75% | 11350 | 11521 | 11512 | 11756.75 | 11776 | 11989.25 | 12117 | 12323 | 12484 | 12661.25 | 12782 | 12911 | 13015.5 |
| Random 90% | 10159.5 | 10523.5 | 10980 | 11167.75 | 11493 | 11775.25 | 12019 | 12379.75 | 12656.5 | 12909.5 | 13192 | 13475 | 13753.5 |

5. Conclusion

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