

POCHODNE

Funkcja	Pochodna	Uwagi
c	0	c<=>R
x^a	ax^{a-1}	a<=>R
a^x	a^xlna	a>0, x<=>R
e^x	ex	x<=>R
log_ax	1/(xlna)	0<a≠1, x>0
lnx	1/x	x>0
sinx	cosx	x<=>R
cosx	-sinx	x<=>R
tgx	1/cos² x	x≠90
ctgx	-(1/sin² x)	x≠180
arcsinx	1/√(1-x²)	x<=>(-1;1)
arccosx	-(1/√(1-x²))	x<=>(-1;1)
arctg	1/(1+x²)	x<=>R
arctg	-(1/(1+x²))	x<=>R

GRANICE POD. WYRAŻEŃ (x- >0)

lim $(x+1)^{\frac{1}{x}} = e$	<u>x-->(+/-)∞</u>
lim $\frac{\sin x}{x} = 1$	lim $(1+\frac{1}{x})^x = e$
lim $\frac{\operatorname{tg} x}{x} = 1$	lim $(1+\frac{a}{x})^x = e^a$
lim $\frac{\arcsin x}{x} = 1$	
lim $\frac{\operatorname{arctg} x}{x} = 1$	
lim $\frac{e^x - 1}{x} = 1$	
lim $\frac{\ln(x+1)}{x} = 1$	
lim $\frac{a^x - 1}{x} = \ln a$	
lim $\frac{\log_a(1+x)}{x} = \frac{1}{\ln a}$	
Lim $\frac{(x+1)^a - 1}{x} = a$	

<=> - należy.

$\int 0 dx = C$	$\int e^{ax+b} dx = \frac{1}{a} e^{ax+b} + C, a \neq 0$
$\int dx = x + C$	$\int e^x = e^x + C$
$\int x dx = \frac{1}{2} x^2 + C$	$\int \frac{dx}{1+x^2} dx = \arctan x + C$
$\int x^n dx = \frac{1}{n+1} x^{n+1} + C, n \neq -1$	$\int \frac{dx}{1+(ax+b)^2} dx = \frac{1}{a} \arctan(ax+b) + C, a \neq 0$
$\int \frac{1}{x} dx = \ln x + C$	$\int \frac{dx}{a^2+x^2} dx = \frac{1}{a} \arctan \frac{x}{a} + C, a \neq 0$
$\int \frac{1}{x^2} dx = -\frac{1}{x} + C$	$\int \frac{dx}{a^2-x^2} dx = \frac{1}{2a} \ln \left \frac{a+x}{a-x} \right + C, a > 0 \text{ i } x \neq a$
$\int \frac{f'(x)}{f(x)} dx = \ln f(x) + C$	$\int \frac{dx}{ax+b} dx = \frac{1}{a} \ln ax+b + C, a \neq 0$
$\int \sqrt{x} dx = \frac{2}{3} x \sqrt{x} + C$	$\int \frac{dx}{(ax+b)^2} dx = -\frac{1}{a(ax+b)} + C$
$\int \frac{dx}{\sqrt{x}} dx = 2 \sqrt{x} + C$	$\int \frac{1}{\sin^2 x} dx = -\cot x + C$
$\int (ax+b) dx = \frac{a}{2} x^2 + bx + C$	$\int \frac{1}{\cos^2 x} dx = \tan x + C$
$\int (ax+b)^n dx = \frac{1}{a(n+1)} (ax+b)^{n+1} + C, a \neq 0, n \neq -1$	$\int \sin x dx = -\cos x + C$
$\int \sqrt{ax+b} dx = \frac{2}{3a} (ax+b) \sqrt{ax+b} + C, a \neq 0$	$\int \cos x dx = \sin x + C$
$\int \frac{1}{\sqrt{ax+b}} dx = -\frac{2\sqrt{ax+b}}{a} + C, a \neq 0$	$\int \sin(ax+b) dx = -\frac{1}{a} \cos(ax+b) + C, a \neq 0$
$\int \frac{dx}{\sqrt{1-(ax+b)^2}} dx = \frac{1}{a} \arcsin(ax+b) + C, a \neq 0$	$\int \cos(ax+b) dx = \frac{1}{a} \sin(ax+b) + C, a \neq 0$
$\int \frac{dx}{\sqrt{1+(ax+b)^2}} dx = \frac{1}{a} \ln((ax+b) + \sqrt{(ax+b)^2 + 1}), a \neq 0$	$\int \frac{1}{\sin^2(ax+b)} dx = -\frac{1}{a} \cot(ax+b) + C, a \neq 0$
$\int \frac{1}{\sqrt{1-x^2}} dx = \arcsin x + C, a \neq 0$	$\int \frac{1}{\cos^2(ax+b)} dx = \frac{1}{a} \tan(ax+b) + C, a \neq 0$
$\int \frac{1}{\sqrt{1+x^2}} dx = \ln(x + \sqrt{x^2+1}) + C$	$\int \arctg x dx = x \arctg x - \ln \sqrt{x^2+1} + C$
$\int \frac{1}{\sqrt{x^2-1}} dx = \ln x + \sqrt{x^2-1} + C, x > 1$	$\int m^{ax+b} dx = \frac{m^{ax+b}}{a \ln m} + C, m \neq 1 \text{ i } a \neq 0$
$\int \frac{1}{\sqrt{x^2-a^2}} dx = \ln x + \sqrt{x^2-a^2} + C, a \neq 0$	$\int m^x dx = \frac{m^x}{\ln m} + C, m \neq 1 \text{ i } m > 0$
$\int \frac{1}{\sqrt{a^2-x^2}} dx = \arcsin \frac{x}{a} + C, a > 0$	$\int \ln x dx = x \ln x - x + C$