

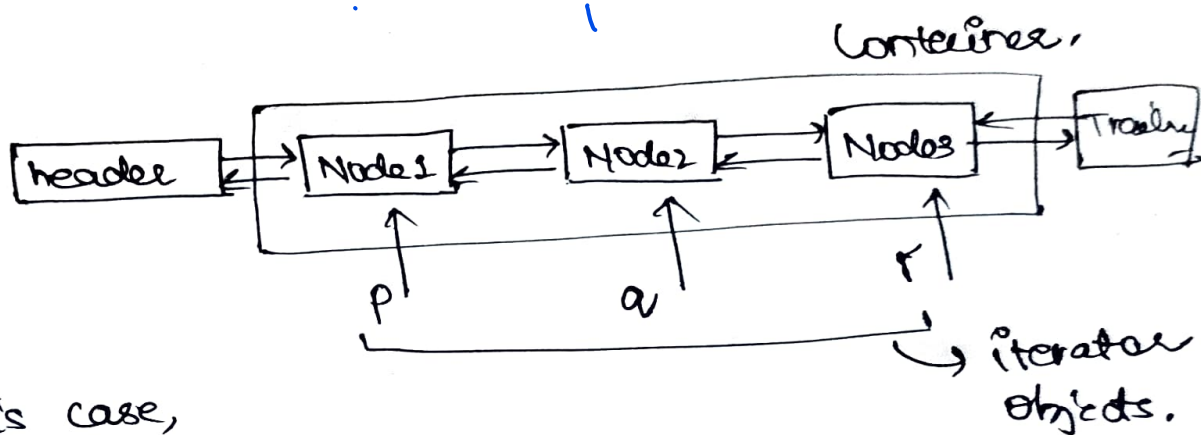
Sequences using DLL :

We have iterator (extension of position class) class which has

*p (dereferencing)

++p (next)

--p (previous)



In this case,

If we have following operation,

atIndex(int i)

= iterator
↳ Begin with $p = \text{begin}()$

For ($j=0; j < i; j++$) $++p$;

return p;

}

ex what is ~~atIndex~~ (1)?

~~iterator p = Node1~~ ~~p~~

~~For ($j=0; j < 1; j++$)~~

so, it returns q,

j	p
0	p
1	q
2	r

Clearly, $O(n)$

```

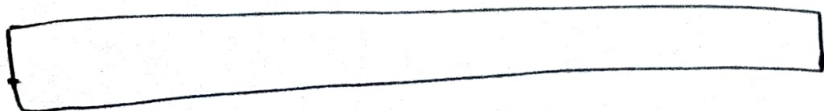
indexOf( Iterator p ) {
    Iterator q = begin();
    int j = 0;
    while (q != p) {
        ++q; ++j;
    }
    return j;
}

```

CA Find `indexOf(r)` .

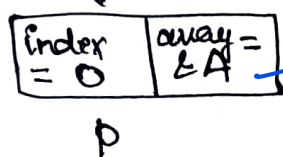
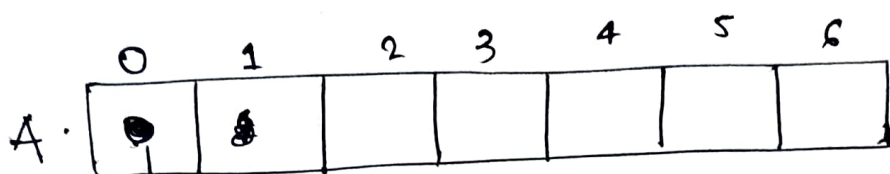
Start with $q' = p$ (true for $q' == r$)
 Set $j = 0$.
 Check if $q' == r$? $\xrightarrow{\text{Yes}}$ return j (index)
 \downarrow (No for $q' == p$ / $q' == q$)
 Increment q' and j time
 clearly $O(n)$ complexity.

What if we implemented sequences with an array?



Implementing Sequence with array.

```
position class {  
    index(i)  
    reference to array (say A)  
}
```



Need to be
some other array
which stores
element?

$*p = A[\text{index}]$

But what is position of p?

No way to reference.

If insertion/deletion occurs,

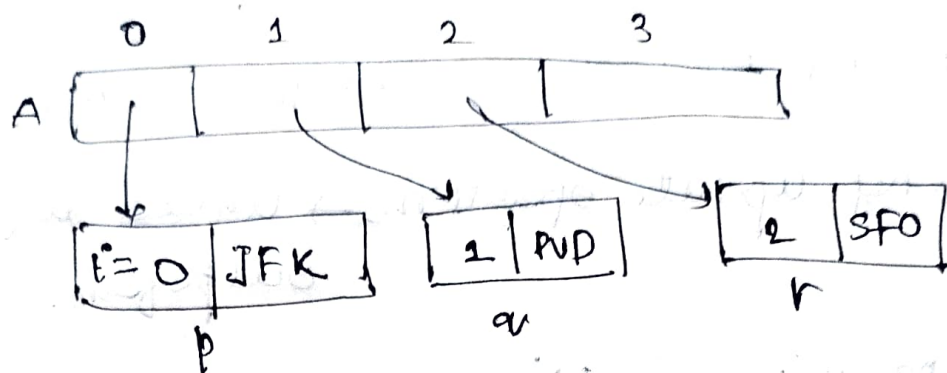
pos. rank changed not positions ✓

If there is no reference to position
how to update position? ✓

New approach.

```
position {  
    index i  
    element e  
}
```

so, $*p = e$



Now, accessing index of position object is $O(1)$

ex. Index of p ?

return $p.index = 0$ $O(1)$

and ~~position~~ which position is at index 2?

~~just iterate over array~~

~~and~~ return $A[2]$ $O(1)$

But while inserting / deleting -
position need to be updated

so, $O(n)$ time in worst case.

What if array is circular?

→ Insert front would take $O(1)$
Back

Comparison.

Array-based Implementation \rightarrow rank based access

Equal on all other access like insert & del.

Regarding update operations \rightarrow linked list outperforms.

Array require $O(N)$

\hookrightarrow size of array

Linked list - $O(n)$

\hookrightarrow no of ~~nodes~~ nodes.