

1) Performance Metrics:

a) Iris dataset

Observe the following Confusion matrices for the Iris dataset prediction model, Compute Accuracy, Precision, recall, F1-Score, Sensitivity, Specificity.

Predicted	IRIS-Dataset	Actual		
		Setosa	Versicolor	Virginica
	Setosa	98	42	10
	Versicolor	30	105	15
	Virginica	17	39	102

$$\text{Overall Accuracy} = \frac{TP_{\text{total}}}{\text{Total Samples}} = \frac{98 + 105 + 102}{600}$$

$$= \frac{305}{600} = 0.5083$$

For each class let's treat one class as "Positive" and the other two combined as "Negative" for binary metrics.

1) Setosa

$$TP = 98$$

$$FP = 30 + 17 = 47$$

$$FN = 42 + 10 = 52$$

$$TN = 105 + 15 + 31 + 102 = 253$$

$$\text{Precision} = \frac{98}{98 + 47} = 0.675$$

$$\text{Recall} = \frac{98}{98 + 52} = 0.653$$

$$F1\text{-Score} = \frac{2 \times (0.675 \times 0.653)}{0.675 + 0.653} = 0.664$$

$$\text{Specificity} = \frac{253}{253 + 47} = 0.843$$

2) versicolor

$$\bullet TP = 105$$

$$\bullet FP = 42 + 31 = 73$$

$$\bullet FN = 30 + 15 = 45$$

$$\bullet TN = 98 + 10 + 17 + 102 = 227$$

$$\text{Precision} = 105 / (105 + 73) = 0.59$$

$$\text{Recall} = \frac{105}{105 + 45} = 0.7$$

$$F1\text{-Score} \approx 0.639$$

$$\text{Specificity} = \frac{227}{227 + 73} \approx 0.756$$

3) virginica

$$\bullet TP = 102$$

$$\bullet FP = 10 + 15 = 25$$

$$\bullet FN = 17 + 31 = 48$$

$$\bullet TN = 98 + 42 + 30 + 105 = 275$$

$$\text{Precision} = 102 / (102 + 25) = 0.803$$

$$\text{Recall (Sensitivity)} = 102 / (102 + 48) = 0.68$$

$$\text{F1-Score} \approx 0.736$$

$$\text{Specificity} = 275 / (275 + 25) = 0.916$$

$$\text{overall Accuracy} = 50.83\%$$

2) Construct the Decision Tree for the following Data sets by using the ID3 Algorithm.

a)

SNO	length	Gills	Beak	Teeth	Is
1	3	NO	Yes	Many	Dolphin
2	4	NO	Yes	Many	Yes
3	3	NO	Yes	Few	Yes
4	5	NO	Yes	Many	Yes
5	5	Yes/NO	Yes	Few	Yes
6	5	Yes	Yes	Many	NO
7	4	Yes	Yes	Many	NO
8	5	Yes	NO	Many	NO
9	4	Yes	NO	Many	NO
10	4	NO	Yes	Few	NO

Step 1: Calculate Entropy of the Dataset:

Target Column: Is Dolphin

• Yes: 5 times

• No: 5 times

$$\begin{aligned} \text{Entropy (S)} &= - \sum P_i \log_2(P_i) = - \left(\frac{5}{10} \log_2 \frac{5}{10} + \frac{5}{10} \log_2 \frac{5}{10} \right) \\ &= - 2 \cdot 0.5 \cdot \log_2 0.5 \end{aligned}$$

Step 2: We will now calculate Information Gain (IG) for each attribute and choose the best one.

Attribute: Gills

Gills = Yes \rightarrow [No, No, No, No] \rightarrow 4 instances \rightarrow All NO
 \rightarrow Entropy = 0.

Gills = NO \rightarrow [Yes, Yes, Yes, Yes, Yes, NO] \rightarrow
 6 instances \rightarrow 5 Yes, 1 NO.

$$\text{Entropy} = - \left(\frac{5}{6} \log_2 \frac{5}{6} + \frac{1}{6} \log_2 \frac{1}{6} \right) \approx$$

$$- (0.833 \cdot -0.222) - (0.167 \cdot -2.585)$$

$$\approx 0.65.$$

Weighted Entropy: $\frac{6}{10} \cdot 0.65 + \frac{4}{10} \cdot 0 = 0.39$

$$\text{IG (Gills)} = 1 - 0.39 = 0.61$$

Attribute: Beak

• Beak = Yes \rightarrow 7 values \rightarrow [Yes, Yes, Yes, Yes, Yes, NO, NO] \rightarrow 5 Yes, 2 NO.

$$\text{Entropy} = - (5/7) \log_2 (5/7) - (2/7) \log_2 (2/7)$$

$$\approx 0.863$$

• Beak = NO \rightarrow 3 values \rightarrow All NO \rightarrow Entropy = 0

Weighted entropy:

$$(7/10) \cdot 0.863 + (3/10) \cdot 0 = 0.604$$

$$\text{IG (Beak)} = 1 - 0.604 = 0.396$$

2300030370
• Attribute: teeth

• Menu: [Yes, Yes, Yes, Yes, No, No, No, No] \rightarrow 8 values
4 Yes, 4 No \rightarrow Entropy = 1

• Few: [Yes, Yes] \rightarrow 2 values \rightarrow Both Yes \rightarrow Entropy = 0

Weighted entropy:

$$(8/10) \cdot 1 + (2/10) \cdot 0 = 0.816 (\text{Teeth})$$

$$\left(\frac{1}{5} \text{ pop } \frac{1}{5} + \frac{2}{5} \text{ pop } \frac{2}{5} \right) = 1 - 0.8 = 0.2$$

• Attribute: length

Value: 3, 4, 5

• Length = 3 \rightarrow [Yes] \rightarrow Entropy = 0

• Length = 4 \rightarrow [Yes, No, No] \rightarrow 1 Yes, 2 No \rightarrow Entropy =

• Length = 5 \rightarrow [Yes, Yes, No, No, No, No] \rightarrow 2 Yes, 4 No

\rightarrow Entropy = 0.918

Weighted entropy:

$$(1/10) \cdot 0 + (3/10) \cdot 0.918 + (6/10) \cdot 0.918 \approx 0.918$$

(length)

$$= 1 - 0.918 = 0.082$$

Step 3: Choose

Attribute with Max Information Gain

Wings: 0.61

Beak: 0.396

Teeth: 0.2

length: 0.082

Best split = gills.

step 4: Build Tree Recursively.

Gills \rightarrow Yes \rightarrow All NO \rightarrow Leaf Nodes: NO

Gills \rightarrow NO \rightarrow Subset: $S' = [1, 2, 3, 4, 5, 10]$

Apply ID3 again on this subset of 6 samples.

Subset S' :

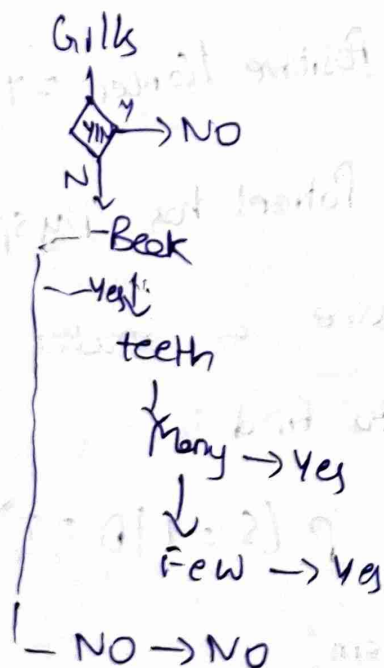
Is Dolphin: Yes (1-5), NO (10) \rightarrow 5 Yes, 1 NO

Entropy = 0.85.

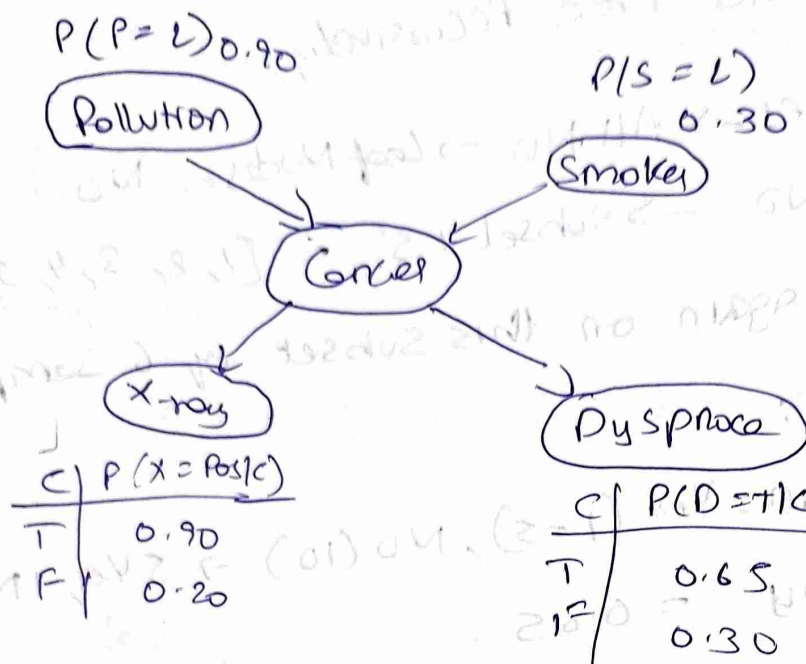
Now, Calculate IG of remaining subsets.

Next split: Beak.

Beak = Yes \rightarrow [1, 2, 3, 4, 5, 10] minus 8 \rightarrow 5 Yes,
1 NO \rightarrow still not pure.



Apply the Bayesian Network technique for the given events and probabilities, answer the following questions.



a) Given that Patient has Cancer, what is the probability they have a positive X-ray?

From the CPT (Conditional Probability Table)

$$P(X=Pos|C=T) = 0.90$$

$$P(X=Positive|Cancer=T) = \boxed{0.90}$$

b) Given that a Patient has Dyspnea, what is the probability they are a Smoker.

We are asked to find:

$$P(S=T|D=T)$$

We use Bayes Theorem:

$$P(S=T|D=T) = \frac{P(D=T|S=T) \cdot P(S=T)}{P(D=T)}$$

2300030370
But D (Dyspnea) depends on Cancer, not directly on Smoker, so we must expand using the full joint distribution:

Compute $P(S=T | D=T)$

We'll compute using marginalization over hidden variables (Pollution and Cancer).

Use:

$$P(S=T | D=T) = \frac{P(S=T \wedge D=T)}{P(D=T)}$$

We'll compute numerator and denominator by summing over all possible values of Pollution and Cancer.

Step 1: List needed probabilities

From diagram:

- $P(P=H) = 0.1$, $P(P=L) = 0.9$
- $P(S=T) = 0.3$, $P(S=F) = 0.7$

From Cancer CPT (middle table), get $P(C=T | P, S)$

- $P(D=T | C=T) = 0.65$, $P(D=T | C=F) = 0.30$

We compute:

$$P(S=T \wedge D=T) = \sum_{P, C} P(P) \cdot P(S=T) \cdot P(C | P, S) \cdot P(D=T | C)$$

For $S=T$ 2300030320

$$|P|C|P(P)|P(C|P, S=T)|P(D=T|C)| \text{ Product } |$$

$$|H|T|O=1$$

$$\text{Sum} = 0.000975 + 0.00855 + 0.005265 +$$

$$0.07857 = 0.09336$$

Now compute $P(D=T)$

Repeat same table for both $S=T$ and $S=F$.

Already got for $S=T \rightarrow 0.09336$.

$$\text{Sum} = 0.00091 + 0.02058 + 0.00041 +$$

$$0.18873 = 0.21063$$

$$\therefore P(S=T | D=T) = \frac{0.09336}{0.09336 + 0.21063} \approx$$

$$\frac{0.09336}{0.30399} \approx 0.307$$

$$P(S=T | D=T) = 0.307$$