

例13: 求 $L^{-1}\left[\frac{2s^2 + 3s + 3}{s^4 + 10s^3 + 36s^2 + 54s + 27}\right]$

解: 令 $F(s) = \frac{2s^2 + 3s + 3}{s^4 + 10s^3 + 36s^2 + 54s + 27} = \frac{2s^2 + 3s + 3}{(s+3)^3(s+1)}$

$$= \frac{r_1}{[s - (-3)]^3} + \frac{r_2}{[s - (-3)]^2} + \frac{r_3}{[s - (-3)]} + \frac{c_1}{[s - (-1)]}$$

$$r_1 = \left. \frac{2s^2 + 3s + 3}{s+1} \right|_{s=-3} = -6 \quad r_2 = \left. \frac{d\left[\frac{2s^2 + 3s + 3}{s+1}\right]}{ds} \right|_{s=-3} = \frac{3}{2};$$

$$r_3 = \frac{1}{2!} \times \left. \frac{d^2\left[\frac{2s^2 + 3s + 3}{s+1}\right]}{ds^2} \right|_{s=-3} = -\frac{1}{4} \quad c_1 = \frac{1}{4}$$

$$r_i = \frac{1}{(i-1)!} \cdot \left. \frac{d^{i-1}[F(s)(s-p)^r]}{ds^{i-1}} \right|_{s=p} \quad (i=1 \sim r)$$