

Tensor Layouts

Array/Vector (1D)

Logical view

| | | | | | | |
|---|---|---|---|---|----|----|
| 1 | 2 | 3 | 5 | 8 | 13 | 21 |
|---|---|---|---|---|----|----|

Shape: $[7]$

Stride: $[1]$

Physical view

| | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|
| 1 | 2 | 3 | 5 | 8 | 13 | 21 |
| 100 | 102 | 104 | 106 | 108 | 110 | 112 |

In C, we get a pointer to the location in memory where the pointer starts and we use it to access all the rest of the elements

Matrix (2D)

Logical view

| | | |
|---|---|----|
| 1 | 2 | 3 |
| 5 | 8 | 13 |

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Shape: $[2, 3]$

Stride: $[3, 1]$

Note: This is known as a row-major layout.

Physical view

| | | | | | |
|----|----|----|----|----|----|
| 1 | 2 | 3 | 5 | 8 | 13 |
| 62 | 64 | 66 | 68 | 70 | 72 |

To go from one row to the next, we need to skip three elements

Matrix (2D) - Reshape

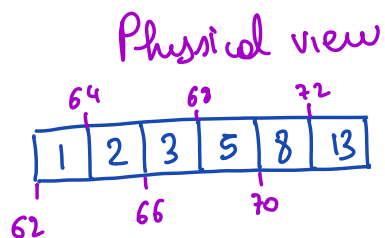
| | | |
|---|---|----|
| 1 | 2 | 3 |
| 5 | 8 | 13 |

⇒

| | |
|---|----|
| 1 | 2 |
| 3 | 5 |
| 8 | 13 |

Shape: $[2, 3]$
Stride: $[3, 1]$

Shape: $[3, 2]$
Stride: $[2, 1]$



Note: physical arrangement does not change!

Matrix (2D) - Transpose

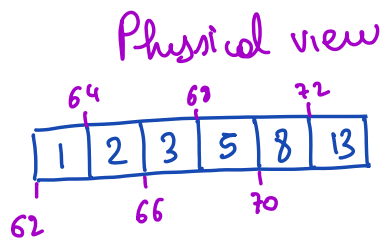
| | | |
|---|---|----|
| 1 | 2 | 3 |
| 5 | 8 | 13 |

⇒

| | |
|---|----|
| 1 | 5 |
| 2 | 8 |
| 3 | 13 |

Shape: $[2, 3]$
Stride: $[3, 1]$

Shape: $[3, 2]$
Stride: $[1, 3]$



↑
To transpose along two dimensions, we need to swap the shape and stride of the two dimensions ... and that's it!

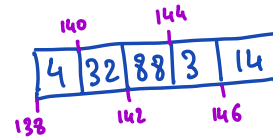
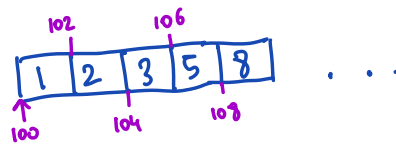
Note: after transposing, the tensor is no longer "contiguous".
that's why in PyTorch you can't "view" but you need to "reshape".

Tensor (3D)

| | | |
|----|----|----|
| 1 | 2 | 3 |
| 5 | 8 | 13 |
| 21 | 34 | 55 |
| 9 | 11 | 13 |

| | | |
|----|----|----|
| 72 | 42 | 2 |
| 31 | 1 | 92 |
| 7 | 4 | 32 |
| 88 | 3 | 14 |

Physical view:



Shape: $[2, 4, 3]$

Stride: $[12, 3, 1]$

$$\text{Stride} = \begin{cases} \text{Stride}[i] = \prod_{j=i+1}^N \text{shape}[j] \\ \text{Stride}[N] = 1 \end{cases}$$