

NUMBER SYSTEM – LOGARITHMS (BASICS → PLACEMENT LEVEL)

1. WHAT IS A LOGARITHM?

A logarithm is the inverse operation of exponentiation. It answers the question: To what power should a base be raised to obtain a given number? Logarithms are frequently asked in placement aptitude to test conceptual clarity.

If $a^x = b$, then $\log_a(b) = x$. Here, 'a' is the base, 'b' is the number, and 'x' is the logarithmic value.

2. BASIC LOGARITHMIC VALUES

- $\log_{10}(1) = 0$
- $\log_{10}(10) = 1$
- $\log_{10}(100) = 2$
- $\log_2(2) = 1$
- $\log_2(8) = 3$

3. LAWS OF LOGARITHMS (MUST REMEMBER)

- Product Law: $\log_a(MN) = \log_a M + \log_a N$
- Quotient Law: $\log_a(M/N) = \log_a M - \log_a N$
- Power Law: $\log_a(M^x) = x \log_a M$
- $\log_a(a) = 1$
- $\log_a(1) = 0$

4. SOLVED EXAMPLES

- Example 1: $\log_{10}(1000) = 3$ because $10^3 = 1000$
- Example 2: $\log_2(16) = 4$ because $2^4 = 16$
- Example 3: $\log_{10}(5 \times 20) = \log_{10}(100) = 2$
- Example 4: $\log_3(27) - \log_3(9) = 3 - 2 = 1$
- Example 5: $\log_2(32) = 5$

5. COMMON MISTAKES TO AVOID

- Using different bases incorrectly
- Forgetting that $\log_a(1) = 0$
- Applying log rules without checking base
- Trying to calculate instead of converting to powers

6. PRACTICE QUESTIONS (HOMEWORK)

- 1. Find the value of $\log_{10}(10000)$
- 2. Find the value of $\log_2(64)$
- 3. Simplify: $\log_{10}(4 \times 25)$
- 4. Evaluate: $\log_3(81) - \log_3(3)$
- 5. Find the value of $\log_5(125)$

7. ANSWERS (FOR SELF-CHECK)

- 1. 4
- 2. 6
- 3. 2
- 4. 3
- 5. 3