

# NUMBER SYSTEM – LOGARITHMS (BASICS → PLACEMENT LEVEL)

## 1. WHAT IS A LOGARITHM?

A logarithm is the inverse operation of exponentiation. It answers the question: To what power should a base be raised to obtain a given number? Logarithms are frequently asked in placement aptitude to test conceptual clarity.

If  $a^x = b$ , then  $\log_a(b) = x$ . Here, 'a' is the base, 'b' is the number, and 'x' is the logarithmic value.

## 2. BASIC LOGARITHMIC VALUES

- $\log_{10}(1) = 0$
- $\log_{10}(10) = 1$
- $\log_{10}(100) = 2$
- $\log_{10}(2) = 1$
- $\log_{10}(8) = 3$

## 3. LAWS OF LOGARITHMS (MUST REMEMBER)

- Product Law:  $\log_a(MN) = \log_a M + \log_a N$
- Quotient Law:  $\log_a(M/N) = \log_a M - \log_a N$
- Power Law:  $\log_a(M^n) = n \log_a M$
- $\log_a(a) = 1$
- $\log_a(1) = 0$

## 4. SOLVED EXAMPLES

- Example 1:  $\log_{10}(1000) = 3$  because  $10^3 = 1000$
- Example 2:  $\log_2(16) = 4$  because  $2^4 = 16$
- Example 3:  $\log_{10}(5 \times 20) = \log_{10}(100) = 2$
- Example 4:  $\log_{10}(27) - \log_{10}(9) = 3 - 2 = 1$
- Example 5:  $\log_{10}(32) = 5$

## 5. COMMON MISTAKES TO AVOID

- Using different bases incorrectly
- Forgetting that  $\log_a(1) = 0$
- Applying log rules without checking base
- Trying to calculate instead of converting to powers

## **6. PRACTICE QUESTIONS (HOMEWORK)**

- 1. Find the value of  $\log_{10}(10000)$
- 2. Find the value of  $\log_2(64)$
- 3. Simplify:  $\log_{10}(4 \times 25)$
- 4. Evaluate:  $\log_3(81) - \log_3(3)$
- 5. Find the value of  $\log_5(125)$

## **7. ANSWERS (FOR SELF-CHECK)**

- 1. 4
- 2. 6
- 3. 2
- 4. 3
- 5. 3