

Fermi function/Occupation Probability

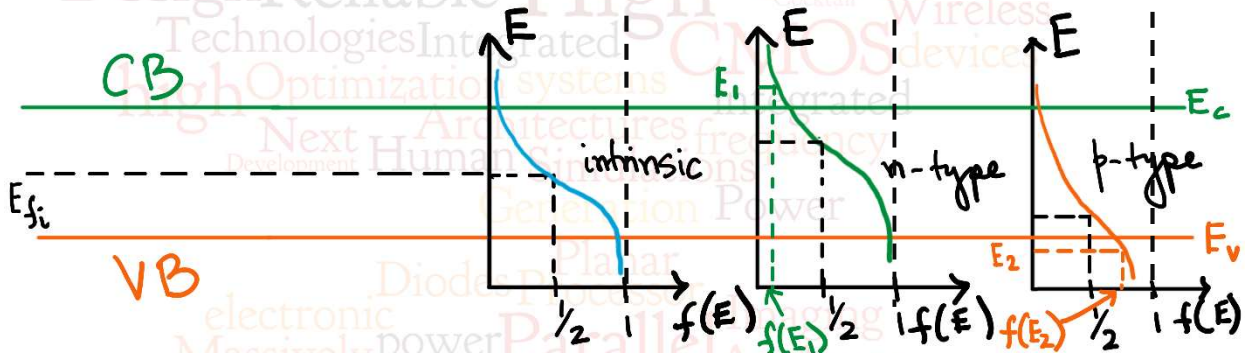
$$f(E) = \frac{1}{1 + e^{\frac{E-E_F}{kT}}}$$

$$f(E_F) = \frac{1}{2}$$

• The function $f(E)$, is also known as **OCCUPATION PROBABILITY**

$$n = \int \rho(E) f(E) dE$$

$$p = \int \rho(E) [1 - f(E)] dE$$



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Carrier Concentration

$$f(E) = \frac{1}{1 + e^{\frac{E-E_F}{kT}}}$$

$$n = \int_{E_c}^{\infty} \rho(E) f(E) dE$$

$$g_C(E)_{3D} = \frac{1}{2\pi^2} \left(\frac{2m_e^*}{\hbar^2} \right)^{3/2} (E - E_c)^{1/2}$$

$$n = N_C^{3D} \frac{2}{\sqrt{\pi}} \mathcal{F}_{1/2}(\eta_C)$$

Effective CB Density of States

Effective VB Density of States

$$p = N_V^{3D} \frac{2}{\sqrt{\pi}} \mathcal{F}_{1/2}(\eta_V)$$

Rigorously correct expression for Carrier Concentration

Defining,

$$N_C^{3D} = 2 \left(\frac{m_e^* kT}{2\pi \hbar^2} \right)^{3/2}$$

$$N_V^{3D} = 2 \left(\frac{m_h^* kT}{2\pi \hbar^2} \right)^{3/2}$$

Effective density of states at 300 K

Semiconductor	$N_C(\text{cm}^{-3})$	$N_V(\text{cm}^{-3})$
Ge	1.03×10^{19}	5.35×10^{18}
Si	3.23×10^{19}	1.83×10^{19}
GaAs	4.21×10^{17}	9.52×10^{18}

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