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Marks 14.00/15.00

Grade 3.73 out of 4.00 (93%)

Question 1

Correct


Mark 1.00 out of 1.00

Let $g(t) = x(t) + \alpha x(-t)$ where $x(t) = \beta e^{-t}u(t)$ and the Laplace transform of $g(t)$ is

$$G(s) = \frac{s}{s^2 - 1}, \quad -1 < \operatorname{Re}\{s\} < 1$$

The values of the constants α and β are

Select one:

- ☐ a. $\alpha = 1, \beta = \frac{1}{2}$
- ☐ b. $\alpha = -1, \beta = -\frac{1}{2}$
- ☒ c. $\alpha = -1, \beta = \frac{1}{2}$
-  ☐ d. $\alpha = 1, \beta = -\frac{1}{2}$
- ☐ e. Incomplete question or none of the options is correct.

Your answer is correct.

The correct answer is: $\alpha = -1, \beta = \frac{1}{2}$

Question 2

Correct


Mark 1.00 out of 1.00

Consider the signal

$$x[n] = \begin{cases} \left(\frac{1}{3}\right)^n \cos\left(\frac{\pi}{4}n\right) & n \leq 0 \\ 0 & n > 0 \end{cases}$$

The poles and ROC for $X(z)$ are given by

Select one:

- ☐ a. poles at $z = \frac{1}{3}e^{\pm j\frac{\pi}{2}}$, ROC: $|z| < \frac{1}{3}$
- ☐ b. poles at $z = \frac{1}{3}e^{\pm j\frac{\pi}{4}}$, ROC: $|z| > \frac{1}{3}$
- ☐ c. poles at $z = \frac{1}{3}e^{\pm j\frac{\pi}{2}}$, ROC: $|z| > \frac{1}{3}$
- ☐ d. poles at $z = \frac{1}{3}e^{\pm j\frac{\pi}{4}}$, ROC: $|z| \leq \frac{1}{3}$
- ☒ e. Incomplete question or none of the options is correct 

Your answer is correct.

The correct answer is: Incomplete question or none of the options is correct

Question 3

Correct

Mark 1.00 out of 1.00

Let $x[n]$ be a signal whose rational Z-transform $X(z)$ contains a pole at $z = \frac{1}{2}$. Given that $x_1[n] = (\frac{1}{4})^n x[n]$ is absolutely summable and $x_2[n] = (\frac{1}{8})^n x[n]$ is not absolutely summable. Then, $x[n]$ is

Select one:

- ☐ a. Left sided
- ☐ b. Right sided
- ☒ c. Two sided or both sided ✓
- ☐ d. Incomplete question or none of the options is correct

Your answer is correct.

The correct answer is: Two sided or both sided

Question 4

Correct

Mark 1.00 out of 1.00

Consider a discrete time signal given by $x[n] = -0.25nu[n] + 0.5nu[-n - 1]$. The region of convergence of its Z-transform would be:

Select one:

- ☐ a. Incomplete question or none of the options is correct
- ☒ b. the annular region between the two circles, both centered at origin and having radii 0.25 and 0.5. ✓
- ☐ c. the region inside the circle of radius 0.5 and centered at origin.
- ☐ d. the entire Z plane.
- ☐ e. the region outside the circle of radius 0.25 and centered at origin.

Your answer is correct.

The correct answers are: the annular region between the two circles, both centered at origin and having radii 0.25 and 0.5., Incomplete question or none of the options is correct

Question 5

Correct

Mark 1.00 out of 1.00

The Laplace transform of $f(t) = 2\sqrt{t/\pi}$ is $s^{-3/2}$. The Laplace transform of $g(t) = \sqrt{1/\pi t}$ is

Select one:

- ☐ a. $\frac{3}{2}s^{-5/2}$
- ☐ b. $s^{3/2}$
- ☐ c. $s^{1/2}$
- ☐ d. Incomplete question or none of the options is correct
- ☒ e. $s^{-1/2}$



Your answer is correct.

The correct answer is: $s^{-1/2}$

Question 6

Correct

Mark 1.00 out of 1.00

An input $x(t) = \exp(-2t)u(t) + \delta(t - 6)$ is applied to an LTI system with impulse response $h(t) = u(t)$. The output is:

Select one:

- ☐ a. $0.5[1 - \exp(-2t)]u(t) + u(t + 6)$
- ☐ b. $[1 - \exp(-2t)]u(t) + u(t + 6)$
- ☒ c. $0.5[1 - \exp(-2t)]u(t) + u(t - 6)$
- ☐ d. $[1 - \exp(-2t)]u(t) + u(t - 6)$
- ☐ e. Incomplete question or none of the options is correct

Your answer is correct.

The correct answer is: $0.5[1 - \exp(-2t)]u(t) + u(t - 6)$ **Question 7**

Correct

Mark 1.00 out of 1.00

Let the Laplace transform of a function $f(t)$ which exists for $t > 0$ be $F_1(s)$ and the Laplace transform of its delayed version $f(t - \tau)$ be $F_2(s)$. Let $F_1^*(s)$ be the complex conjugate of $F_1(s)$ with the Laplace variable set as $s = \sigma + j\omega$. If $G(s) = \frac{F_2(s)F_1^*(s)}{\|F_1(s)\|^2}$, then the inverse Laplace transform of $G(s)$ is:

Select one:

- ☐ a. An ideal impulse $\delta(t)$
- ☒ b. An ideal delayed impulse $\delta(t - \tau)$
- ☐ c. An ideal delayed step function $u(t - \tau)$
- ☐ d. Incomplete question or none of the options is correct
- ☐ e. An ideal step function $u(t)$

Your answer is correct.

The correct answer is: An ideal delayed impulse $\delta(t - \tau)$ **Question 8**

Correct

Mark 1.00 out of 1.00

Suppose $x[n]$ is an absolutely summable discrete-time signal. Its z-transform is a rational function with two poles and two zeroes. The poles are at $z = \pm 2j$. Which of the following statements is TRUE for the signal $x[n]$?

Select one:

- ☐ a. It is a periodic signal.
- ☐ b. It is a finite duration signal.
- ☐ c. It is a causal signal.
- ☒ d. It is a non-causal signal. ✓
- ☐ e. Incomplete question or none of the options is correct

Your answer is correct.

The correct answer is: It is a non-causal signal.

Question 9

Correct

Mark 1.00 out of 1.00

The input-output relationship of a causal stable LTI system is given as

$y[n] = \alpha y[n-1] + \beta x[n]$. If the impulse response $h[n]$ of this system satisfies the condition $\sum_{n=0}^{\infty} h[n] = 2$, the relationship between α and β is

Select one:

- ☐ a. Incomplete question or none of the options is correct
- ☐ b. $\alpha = 2\beta$
- ☐ c. $\alpha = 1 + \beta/2$
- ☐ d. $\alpha = -2\beta$
- ☒ e. $\alpha = 1 - \beta/2$



Your answer is correct.

The correct answer is: $\alpha = 1 - \beta/2$

Question 10

Correct

Mark 1.00 out of 1.00

A causal LTI system S with impulse response $h(t)$ has its input $x(t)$ and output $y(t)$ related through a linear constant-coefficient differential equation of the form

$$\frac{d^3 y(t)}{dt^3} + (1 + \alpha) \frac{d^2 y(t)}{dt^2} + \alpha(\alpha + 1) \frac{dy(t)}{dt} + \alpha^2 y(t) = x(t)$$

If

$$g(t) = \frac{dh(t)}{dt} + h(t)$$

How many poles does $G(s)$ have?

Answer:

The correct answer is: 2

Question 11

Correct

Mark 1.00 out of 1.00

How many signals have a Laplace transform that may be expressed as $\frac{(s-1)}{(s+2)(s+3)(s^2+s+1)}$ in its region of convergence?

Answer:

The correct answer is: 4

Question 12

Incorrect

Mark 0.00 out of 1.00

The transfer function of a causal LTI system is $H(s) = \frac{1}{s}$. If the input to the system is $x(t) = \frac{\sin(t)}{\pi t} u(t)$, where $u(t)$ is a unit step function, the system output $y(t)$ at $t \rightarrow \infty$ is

The correct answer is: 0.5

Question 13

Correct

Mark 1.00 out of 1.00

The z-transform $X[z]$ of a sequence $x[n]$ is given by $X[z] = \frac{0.5}{1-2z^{-1}}$. It is given that the region of convergence of $X[z]$ includes the unit circle. The value of $x[0]$ is ✓.

The correct answer is: 0

Question 14

Correct

Mark 1.00 out of 1.00

Let $H_1(z) = (1 - pz^{-1})^{-1}$, $H_2(z) = (1 - qz^{-1})^{-1}$, $H(z) = H_1(z) + rH_2(z)$. The quantities p, q and r are real numbers. Consider $p = \frac{1}{2}$, $q = -\frac{1}{4}$, $|r| < 1$. If the zero of $H(z)$ lies on the unit circle, then $|r| =$

 ✓.

The correct answer is: 0.5

Question 15

Correct

Mark 1.00 out of 1.00

Two causal discrete-time signals $x[n]$ and $y[n]$ are related as $y[n] = \sum_{m=0}^n x[m]$. If the z-transform of $y[n]$ is $\frac{2}{z(z-1)^2}$, the value of $x[2]$ is ✓.

The correct answer is: 0

◀ Quiz PwD



Quiz PwD ▶