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Several families go out to dinner together. To increase their social interaction, they would like to sit at tables so that at most **two** members of the same family are at the same table. Further, each table has a capacity of how many people can sit there and is coloured either red or blue. We would like to ensure that at most 60 percent of the people are seated at a blue table, and similarly, at most 60 percent of the people are seated at a red table. Show how to formulate a seating arrangement that meets these objectives as a maximum flow problem. Assume that the dinner contingent has p families and the ith family has a_i members. Also assume that there are q tables available and the jth table has a seating capacity of b_j and is coloured either red or blue. You should clearly state the set of vertices and edges, the edge capacities and briefly explain why the maximum flow formulation solves the desired problem.

as a solution to the integral medel our sylvation orangement man flow peroblem (with all edge capacities as integers) Consider the following flow notwerk, with sown & dest node The entire flow supresents no of heaple with I fen = 2 pen LO.6 PJ 0.607 90 auniliary nodes/gadgets Connect all families ithe vto assign the family tj (tj e[2]) with (xi) to all and node Capacity mode

Now consider the sum of capacitus of table which are blue = \(\sum_{\text{i}} \) = \(\text{P}. \) & som of capactes of fred table = \(\text{Q}. \) Add edges from 6 & r to t with capacity. [061] 6 LO.6 Q] (Ln denotes genealest int 5 x) If the man flow to such a flow retwork has a flow = \(\sum a i = \a_1 + \a_2 - \approx \rho \) we obtain the arrangement by stabing the flows on edge from fi to ti \(\text{Will frow now why all constraints are satisfied off such a flow exists: (1) The flow through every family node fi is. atmost ai. Alsof such a firm has value ai, all members of the family are assigned a table & hence if it is trave for all family we obtain a correct averangement (covered for this constraint). (2) Since reach table can have almost 2 people from same family, each family has the edge capacity 2 to every table rode. (3) More the sum of flows through all able talely are directed to the (1) node & vin werea for seed table. Each of the redge has capacity - capacity of the lable tj The edge for a rode that capacity gint (0.61) & vice-week for I node to t. This ensures room flow through r & b cannot enceed the row 0.6 x capably of onstruction (all red tables 5 60%. all below tales ≤ 60%. all) While: we give by so that one sod table may be full heart the total comprisal 8. 8 the full street the best with integer value supresent the heart & only & person contributes to I und of flow.