# Natural Language Processing MEMMs and CRFs

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- The goal of sequence labeling is to assign tags to words, or more generally, to assign discrete labels to discrete elements in a sequence [?].
- Well known examples of this problem are: part-of-speech tagging (POS) and Named Entity Recognition (NER).
- Maximum-entropy Markov models (MEMMs) make use of log-linear models for sequence labeling tasks.
- In the early NLP literature, logistic regression was often called maximum entropy classification [?].
- Hence, MEMMs will look very similar to the multi-class softmax models seen in the lecture about linear models.
- In contrast to HMMs, here we rely on parameterized functions.

The goal of MEMMs is model the following conditional distribution:

$$P(s_1, s_2 \ldots, s_m | x_1, \ldots, x_m)$$

- Where each x<sub>j</sub> for j = 1...m is the j-th input symbol (for example the j-th word in a sentence), and each s<sub>i</sub> for j = 1...m is the j-th tag.<sup>1</sup>
- We expecto this P(DET,NOUN,VERB|the,dog,barks) to be higher than P(VERB,VERB,VERB|the,dog,barks)

¹These slides are based on lecture notes of Michael Collins http://www.cs.columbia.edu/~mcollins/. The notation and terminology has been adapted to be consistent with the other material.

- We use S to denote the set of possible tags.
- We assume that S is a finite set.
- For example, in part-of-speech tagging of English, S would be the set of all
  possible parts of speech in English (noun, verb, determiner, preposition, etc.).
- Given a sequence of words  $x_1, \ldots, x_m$ , there are  $k^m$  possible part-of-speech sequences  $s_1, \ldots, s_m$ , where k = |S| is the number of possible parts of speech.
- We want to estimate a distribution over these  $k^m$  possible sequences.

In a first step, MEMMs use the following decomposition:

$$P(s_{1}, s_{2}..., s_{m}|x_{1},..., x_{m}) = \prod_{i=1}^{m} P(s_{i}|s_{1}..., s_{i-1}, x_{1},..., x_{m})$$

$$= \prod_{i=1}^{m} P(s_{i}|s_{i-1}, x_{1},..., x_{m})$$
(1)

- The first equality is exact (it follows by the chain rule of conditional probabilities).
- The second equality follows from an independence assumption, namely that for all i,

$$P(s_i|s_1...,s_{i-1},x_1,...,x_m) = P(s_i|s_{i-1},x_1,...,x_m)$$

- Hence we are making a first order Markov assumption similar to the Markov assumption made in HMMs.
- The tag in the *i*-th position depends only on the tag in the (i-1)-th position.
- Having made these independence assumptions, we then model each term using a log-linear (Softmax) model:

$$P(s_{i}|s_{i-1},x_{1},\ldots,x_{m}) = \frac{\exp(\vec{w}\cdot\vec{\phi}(x_{1},\ldots,x_{m},i,s_{i-1},s_{i}))}{\sum_{s'\in S}\exp(\vec{w}\cdot\vec{\phi}(x_{1},\ldots,x_{m},i,s_{i-1},s'))}$$
(2)

Here  $\vec{\phi}(x_1, \dots, x_m, i, s_{i-1}, s_i)$  is a feature vector where:

- $x_1, \dots, x_m$  is the entire sentence being tagged.
- *i* is the position to be tagged (can take any value from 1 to *m*)
- s is the previous tag value (can take any value in S).
- s' is the new tag value (can take any value in S)

## Example of Features used in Part-of-Speech Tagging

- 1.  $\vec{\phi}(x_1, \cdots, x_m, i, s_{i-1}, s_i)_{[1]} = 1$  if  $s_i = \mathsf{ADVERB}$  and word  $x_i$  ends in "-ly"; 0 otherwise. If the weight  $\vec{w}_{[1]}$  associated with this feature is large and positive, then this feature is essentially saying that we prefer labelings where words ending in -ly get labeled as ADVERB.
- 2.  $\vec{\phi}(x_1, \dots, x_m, i, s_{i-1}, s_i)_{[2]} = 1$  if  $i = 1, s_i = VERB$ , and  $x_m = ?$ ; 0 otherwise. If the weight  $\vec{w}_{[2]}$  associated with this feature is large and positive, then labelings that assign VERB to the first word in a question (e.g., "Is this a sentence beginning with a verb?") are preferred.
- 3.  $\vec{\phi}(x_1, \dots, x_m, i, s_{i-1}, s_i)_{[3]} = 1$  if  $s_{i-1} = \text{ADJECTIVE}$  and  $l_i = \text{NOUN}$ ; 0 otherwise. Again, a positive weight for this feature means that adjectives tend to be followed by nouns.
- 4.  $\vec{\phi}(x_1, \cdots, x_m, i, s_{i-1}, s_i)_{[4]} = 1$  if  $s_{i-1}$ = PREPOSITION and  $s_i$ = PREPOSITION. A negative weight  $\vec{w}_{[4]}$  for this function would mean that prepositions don't tend to follow prepositions.

<sup>2</sup>Source: https://blog.echen.me/2012/01/03/ introduction-to-conditional-random-fields/

## **Feature Templates**

It is possible to define more general feature templates covering unigrams, bigrams, n-grams of words as well as tag values of  $s_{i-1}$  and  $s_i$ .

- 1. A word unigram and tag unigram feature template:
  - $\vec{\phi}(x_1, \cdots, x_m, i, s_{i-1}, s_i)_{[hash(j,k)]} = 1$  if  $s_i = \mathsf{TAG}_{[j]}$  and  $x_i = \mathsf{WORD}_{[k]}$ ; 0 otherwise  $\forall j, k$ .
  - Notice that j is and index spanning all possible tags in S and k is another index spanning the words in the vocabulary V.
- 2. A word bigram and tag bigram feature template:

$$\vec{\phi}(x_1,\cdots,x_m,i,s_{i-1},s_i)_{[hash(j,k,u,v)]}=1$$
 if  $s_{i-1}=\mathsf{TAG}_{[j]}$  and  $s_i=\mathsf{TAG}_{[k]}$  and  $x_{i-1}=\mathsf{WORD}_{[u]}$  and  $x_j=\mathsf{WORD}_{[v]};$  0 otherwise  $\forall j,k,u,v$ .

The function hash(j, k, ...) will map each different feature to a unique index in the feature vector.

Notice that the resuling vector will be very high-dimensional and sparse.

### MEMMs and Multi-class Softmax

- Notice that the log-linear model from above is very similar to the multi-class softmax model presented in the lecture about linear models.
- A general log-linear model has the following form:

$$P(y|x; \vec{w}) = \frac{\exp(\vec{w} \cdot \vec{\phi}(x, y))}{\sum_{y' \in Y} \exp(\vec{w} \cdot \vec{\phi}(x, y'))}$$

A multi-class softmax model has the following form:

$$\hat{\vec{y}} = \operatorname{softmax}(\vec{x} \cdot W + \vec{b})$$

$$\hat{\vec{y}}_{[i]} = \frac{e^{(\vec{x} \cdot W + \vec{b})_{[i]}}}{\sum_{j} e^{(\vec{x} \cdot W + \vec{b})_{[j]}}}$$
(3)

## MEMMs and Multi-class Softmax

- Difference 1: in the log-linear model we have a fixed parameter vector  $\vec{w}$  instead of having multiple vectors (one column of W for each class value).
- Difference 2: the feature vector of the log-linear model  $\vec{\phi}(x,y)$  includes information of the label y, whereas the input vecotr  $\vec{x}$  of the softmax model is independent of y.
- Log-linear models allow using features that consider the interaction between x and y (e.g., x end in "ly" and y is an ADVERB).

## Training MEMMs

- Once we've defined the feature vectors  $\vec{\phi}$ , we can train the parameters  $\vec{w}$  of the model in the usual way for linear models.
- We set the negative log-likelihood as the loss function and optimize parameters using gradient descent from the training examples.
- This is equivalent as using the cross-entropy loss.
- "Any loss consisting of a negative log-likelihood is a cross-entropy between the empirical distribution defined by the training set and the probability distribution defined by model" [?].

## **Decoding with MEMMs**

- The decoding problem is as follows.
- We are given a new test sequence  $x_1, \ldots, x_m$ .
- Our goal is to compute the most likely state sequence for this test sequence,

$$\operatorname{argmax}_{s_1,\ldots,s_m} P(s_1,\ldots,s_m|x_1,\ldots,x_m). \tag{4}$$

- There are k<sup>m</sup> possible state sequences, so for any reasonably large sentence length m brute-force search through all the possibilities will not be possible.
- We can use the Viterbi alogrithm in a similar way as used for HMMs.

## **Decoding with MEMMs**

- The basic data structure in the algorithm will be a dynamic programming table π with entries π[j, s] for j = 1,..., m, and s ∈ S.
- π[j, s] will store the maximum probability for any state sequence ending in state s
  at position j.
- · More formally, our algorithm will compute

$$\pi[j,s] = \max_{s_1,\ldots,s_{j-1}} \left( P(s|s_{j-1},x_1,\ldots,x_m) \prod_{k=1}^{j-1} P(s_k|s_{k-1},x_1,\ldots,x_m) \right)$$

for all j = 1, ..., m, and for all  $s \in S$ .

### Links

- sequence-tagging-lstm-crf/
   https://www.quora.com/
- What-are-the-pros-and-cons-of-these-three-sequence-models-MaxEnt
- https: //people.cs.umass.edu/~mccallum/papers/crf-tutorial.pdf

• https://www.depends-on-the-definition.com/

Questions?

Thanks for your Attention!

### References I



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Goodfellow, I., Bengio, Y., and Courville, A. (2016). *Deep learning*. MIT press.