Natural Language Processing Vectors Space Model and Information Retrieval

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July 18, 2019

Motivation

- How does a search engine such as Duckduckgo or Google retrieve relevant documents from a given query?
- How can a company process the claims left by its users on its Web portals?

The following areas of knowledge study these problems:

- Information Retrieval: science of searching for information in a documents.
- Text Mining: Extraction of knowledge from text.

Both of them are closely related to NLP! (the borders between these fields are unclear)

Tokens and Types

Tokenization: The task of splitting a sentence or document into *tokens*. Additional transformations can be employed such as the removal of special characters (e.g., punctuation), lowercasing, etc. [Manning et al., 2008].

Example

Input: I like human languages and programming languages.

Tokens: [I] [like] [human] [languages] [and] [programming] [languages]

A *type* is a class of *token* containing a single sequence of characters. They are obtained by identifying unique tokens within the document.

Types

Tipos: [I] [like] [human] [languages] [and] [programming]

The token languages was repeated in the sentece

Vocabulary Extraction

A term is a normalized type. The vocabulary V, is the set of terms (normalized unique tokens) within a collection of documents or corpus D.

Stopwords removal

- In order to reduce the size of the vocabulary and eliminate terms that do not provide much information, terms that occur with high frequency are in the corpus are elminated.
- These terms are called *stopwords* and include articles, pronouns, prepositions and conjunctions.
 Example: [a, an, and, any, has, do, don't, did, the, on].¹

The removal of stopwords can be inconvenient in many NLP tasks!! Example: I don't like pizza => pizza ("I", "don't", and "like" were removed)

¹Related concepts: function words, closed-class words.

Stemming

A process in which terms are transformed to their root in order to reduce the size of the vocabulary. It is carried out on the basis of a set of word reduction rules.

Example: Porter's Algorithm.

(F)	Rule			Example	Example		
	SSES	\rightarrow	SS	caresses	\rightarrow	caress	
	IES	\rightarrow	Ι	ponies	\rightarrow	poni	
	SS	\rightarrow	SS	caress	\rightarrow	caress	
	S	\rightarrow		cats	\rightarrow	cat	

Example: d = I like human languages and programming languages => I like human languag and program languag²

The vocabulary of document *d* after removing stopwords and performing stemming:

termld	value		
t1	human		
t2	languag		
t3	program		

²http://9ol.es/porter_js_demo.html

Lemmatization

- Another strategy to transform words to their root. It performs a
 morphological analysis using reference dictionaries (lookup tables) to
 create equivalence classes between types.
- For example for the token saw, a stemming rule could return the term s, while through lemmatization a dictionary would give us see.

Zipf's law [1]

- The Zipf's law, proposed by George Kingsley Zipf in [Zipf, 1935], is an empirical law about the frequency of terms within a collection of documents (corpus).
- It states that the frequency f of a term in a corpus is inversely proportional to its r ranking in a sorted frequency table:

$$f = \frac{cf}{r^{\beta}} \tag{1}$$

- Where cf is a constant dependent on the collection and $\beta > 0$ is a decay factor.
- If β = 1, then f follows exactly Zipf's law, otherwise it follows a Zipf-like distribution.
- The law relates to the principle of minimum effort. We often use a few words to write ideas.
- The Zipf law is a type of power law distribution (long tail distributions)

Zipf's law [2]

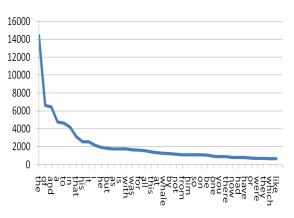


Figure: Zipf's law

- If we plot a log log graph, we obtain a straight line with slope $-\beta^{-1}$.
- Most frequent words can be used to buil a stopwords list.

Posting Lists and the Inverted Index

Let *D* be a collection of documents and *V* the vocabulary of all terms extracted from the collection:

- The posting list of a term is the list of all documents where the term appears at least once. Documents are identified by their ids.
- An inverted index is a dictionary-type data structure mapping terms
 t_i ∈ V into their corresponding posting lists.

Brutus
$$\longrightarrow$$
 $1 \longrightarrow 2 \longrightarrow 4 \longrightarrow 11 \longrightarrow 31 \longrightarrow 45 \longrightarrow 173 \longrightarrow 174$
Calpurnia \longrightarrow $2 \longrightarrow 31 \longrightarrow 54 \longrightarrow 101$

< term $> \rightarrow <$ docld $>^*$

Figure: Inverted Index

Web Search Engines [1]

A search engine is an information retrieval system designed for searching information on the Web (solving information needs) [Manning et al., 2008]. Its basic components are:

- Crawler: a robot that navigates the Web according to a defined strategy.
 It usually starts by browsing a set of seed websites and continues to browse their hyperlinks.
- Indexer: in charge of maintaining an inverted index with the content of the pages traversed by the Crawler.
- Query processor: in charge of processing user queries and searching the index for the documents most relevant to a query.
- Ranking function: the function used by the query processor to rank documents indexed in the collection by relevance according to a query.
- User interface: receives the query as input and returns the documents ranked by relevancy.

Web Search Engines [2]

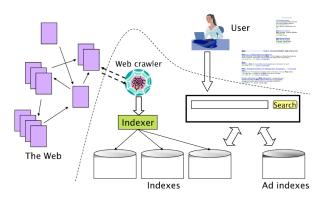


Figure: The various components of a web search engine [Manning et al., 2008].

The Vector Space Model

- In order to rank queries, or measure the similarity between two documents we need a similarity metric.
- Documents can be represented as vectors of terms, where each term is a vector dimension [Salton et al., 1975].
- These types of representations are called Bag of Words. Word order and linguistic structure is loss.
- Idea: the value of each dimension is a weight that represents the relevance of the term t_i in the document d.

$$d_j \to \overrightarrow{d_j} = (w(t_1, d_j), ..., w(t_{|V|}, d_j))$$
 (2)

• How can we model how informative is a term to a document?

Term Frequency - Inverted Document Frequency [1]

- Let Tf_{i,j} be the frequency of term t_i in document d_j.
- A term that appears 10 times should provide more information than one that appears once.
- What happens when we have documents that are much longer than the others?
- We can normalize by the maximum term frequency in the document.

$$Tf_{i,j} = \frac{f_{i,j}}{\max f_{i,j}}$$

- Does a term that appears in very few documents provide more or less information than one that appears several times?
- For example, the document The respected major of Pelotillehue. The term Pelotillehue appears in fewer documents than major, so it should be more descriptive.

Term Frequency - Inverted Document Frequency [2]

 Let N be the number of documents in the collection and n_i the number of documents containing term t_i, we define idf of t_i as follows:

$$idf_{t_i} = log_{10}(\frac{N}{n_i})$$

- A term that appears in all documents would have idf = 0 and one that appears in 10% of the documents would have idf = 1.
- The Tf-idf scoring model combines Tf and idf scores, resulting in the following weights w for a term in a document:

$$w(t_i,d_j) = Tf_i \times log_{10}(\frac{N}{n_i})$$

 Search engine queries can also be modeled as vectors too. However, queries have between 2 and 3 terms in average. To avoid having too many null dimensions, query vectors can be smoothed as follows:

$$w(t_i, d_j) = (0.5 + 0.5 \times Tf_{i,j})log_{10}(\frac{N}{n_i})$$

Similarity between Vectors

- Representing queries and documents as vectors allows calculating their similarity.
- One approach would be using the euclidean distance.
- The common approach is to calculate the cosine of the angle between the two vectors.
- If both documents are the same, the angle would be 0 and its cosine would be 1. On the other hand, if they are orthogonal the cosine is 0.
- The vectors are normalized by its euclidean norm $||d||_2$.
- The cosine similarity is calculated as follows:

$$cos(d_1, d_2) = \frac{d_1 \cdot d_2}{|d_1| \times |d_2|} = \frac{\sum_{i=1}^{|V|} (w(t_i, d_1) \times w(t_i, d_1))}{\sqrt{\sum_{i=1}^{|V|} w(t_i, d_1)^2} \times \sqrt{\sum_{i=1}^{|V|} w(t_i, d_2)^2}}$$

• This is wrongly called cosine distance. It is actually a similarity metric.

Cosine Similarity

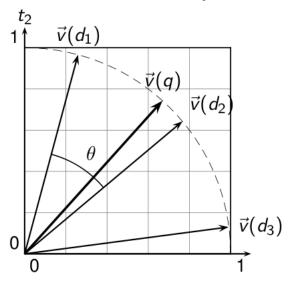


Figure: Cosine Similarity.

Exercise

 Suppose we have 3 documents formed from the following sequences of terms:

```
d_1 \rightarrow t_4 t_3 t_1 t_4

d_2 \rightarrow t_5 t_4 t_2 t_3 t_5

d_3 \rightarrow t_2 t_1 t_4 t_4
```

- Build a term-document matrix of 5 × 3 dimensions using simple *Tf-idf* weights (without normalization).
- We recommend you first build a list with the number of documents in which each term appears (useful for calculating idf scores)
- Then calculate the idf scores of each term.
- Fill up the cells of the matrix the Tf-idf values.
- Which is the closest document to d₁?

Result

Table: Tf-idf Matrix

	d1	d2	d3
t1	0.176	0.000	0.176
t2	0.000	0.176	0.176
t3	0.176	0.176	0.000
t4	0.000	0.000	0.000
t5	0.000	0.954	0.000

Document Clustering [1]

- How can we group documents that are similar with each other?
- Clustering is the process of grouping documents that are similar with each other.
- Each group of documents is called a cluster.
- In clustering we try to identify groups of documents in which the similarity between documents in the same cluster is maximized and the similarity of documents in different clusters is minimized.

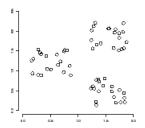


Figure: Set of documents where the clusters can be clearly identified.

Document Clustering [2]

- Document clustering allows identifying topics in a corpus and reducing the search space in a search engine i.e., the inverted index is organized according to the clusters.
- K-medias is a simple clustering algorithm that receives the number of clusters k as a parameter.
- The algorithm relies on the idea of centroid, which is the average vector of documents belonging to the same cluster.
- Let S be a set of 2-dimensional vectors $\{3,6\},\{1,2\},\{5,1\}$, the centroid of S is $\{(3+1+5)/3,(6+2+1)/3\}=\{3,3\}$.

K-Means

- 1. We start with k random centroids.
- 2. We calculate the similarity between each document and each centroid.
- 3. We assign each document to its closest centroid forming a cluster.
- The centroids are recalculated according to the documents assigned to them.
- 5. This process is repeated until convergence.

K-means

```
K-MEANS(\{\vec{x}_1,\ldots,\vec{x}_N\},K)
  1 (\vec{s}_1, \vec{s}_2, \dots, \vec{s}_K) \leftarrow \text{SELECTRANDOMSEEDS}(\{\vec{x}_1, \dots, \vec{x}_N\}, K)
  2 for k ← 1 to K
  3 do \vec{\mu}_k \leftarrow \vec{s}_k
  4 while stopping criterion has not been met
        do for k \leftarrow 1 to K
              do \omega_k \leftarrow \{\}
       for n \leftarrow 1 to N
              \mathbf{do}\ j \leftarrow \arg\min_{i'} |\vec{\mu}_{i'} - \vec{x}_n|
                    \omega_i \leftarrow \omega_j \cup \{\vec{x}_n\} (reassignment of vectors)
              for k \leftarrow 1 to K
 10
              do \vec{\mu}_k \leftarrow \frac{1}{|\omega_k|} \sum_{\vec{x} \in \omega_k} \vec{x} (recomputation of centroids)
 11
         return \{\vec{\mu}_1, \dots, \vec{\mu}_K\}
 12
```

Figure: K-means algorithm

Conclusions and Additional Concepts

- Representing documents as vectors is essential for calculating similarities between document pairs.
- Bag of words vectors lack linguistic structure.
- Bag of words vectors are high-dimensional and sparse.
- Word n-grams can help capturing multi word-expressions (e.g., New York => new_york)
- Modern information retrieval systems go beyond vector similarity (PageRank, Relevance Feedback, Query log mining, Google Knowledge Graph, Machine Learning).
- Information retrieval and text mining are less concerned with linguistic structure, and more interested in producing fast and scalable algorithms [Eisenstein, 2018].

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Salton, G., Wong, A., and Yang, C.-S. (1975). A vector space model for automatic indexing. *Communications of the ACM*, 18(11):613–620.



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