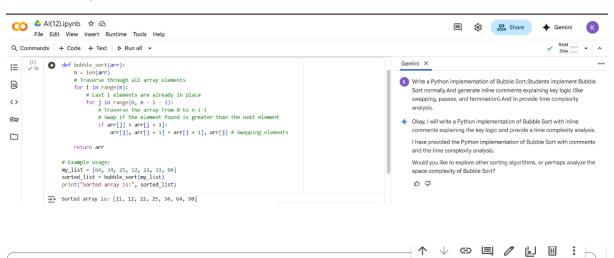
# Assignment-12.4

#### Task 1:

Write a Python implementation of Bubble Sort. Students implement Bubble Sort normally. And generate inline comments explaining key logic (like swapping, passes, and termination). And to provide time complexity analysis.

#### **Code and Output**:



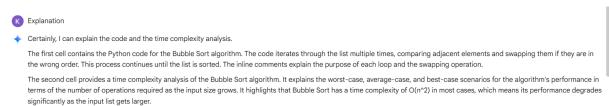
# Time Complexity Analysis of Bubble Sort

Bubble Sort has a time complexity of  $O(n^2)$  in the worst and average cases, where 'n' is the number of elements in the array.

- Worst Case: This occurs when the array is sorted in reverse order. In this case, the inner loop will always perform 'n-1' comparisons in the first pass, 'n-2' in the second, and so on. The total number of comparisons will be approximately n^2/2, resulting in O(n^2) complexity.
- Average Case: For a randomly ordered array, the number of comparisons is also approximately n^2/2, leading to O(n^2) complexity.
- Best Case: This occurs when the array is already sorted. In this case, although the outer loop still runs 'n' times, the inner loop will not perform any swaps if an optimization is added to stop the algorithm if no swaps occur in a pass. Without this optimization, it's still O(n^2). With the optimization, the best case becomes O(n). The implementation above does not include this optimization, so its best case is O(n^2).



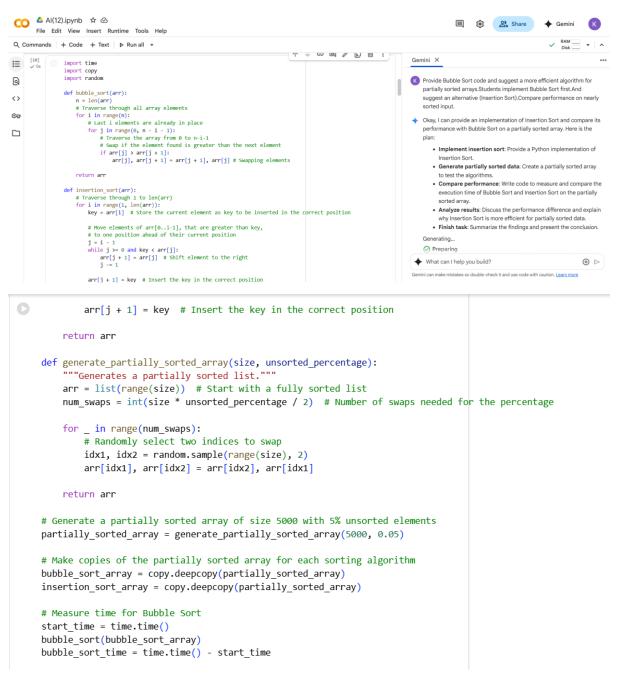
#### **Explanation:**



#### Task 2:

Provide Bubble Sort code and suggest a more efficient algorithm for partially sorted arrays. Students implement Bubble Sort first. And suggest an alternative (Insertion Sort). Compare performance on nearly sorted input.

### **Code and Output:**



```
# Measure time for Bubble Sort

start_time = time.time()

bubble_sort(bubble_sort_array)

bubble_sort_time = time.time() - start_time

# Measure time for Insertion Sort

start_time = time.time()

insertion_sort(insertion_sort_array)

insertion_sort_time = time.time() - start_time

print(f"Bubble Sort time: {bubble_sort_time:.6f} seconds")

print(f"Insertion Sort time: {insertion_sort_time:.6f} seconds")

Bubble Sort time: 0.930790 seconds

Insertion Sort time: 0.039405 seconds
```

#### **Explanation:**

- K explanation
- Certainly. Looking at the cells currently visible, I see:
  - 1. A code cell (cell id 540ee461) containing the Python implementation of the **Bubble Sort** algorithm. This function takes a list (arr) and sorts it in ascending order by repeatedly stepping through the list, comparing adjacent elements and swapping them if they are in the wrong order. The process continues until no swaps are needed in a pass, indicating the list is sorted.
  - 2. A markdown cell (cell id 2df7d192) providing a **Time Complexity Analysis of Bubble Sort**. This explains how the time taken by the algorithm scales with the size of the input list (n). It discusses the:
    - o Worst Case: O(n^2), which happens when the list is in reverse order.
    - o Average Case: O(n^2), for randomly ordered lists.
    - Best Case: O(n^2) for this specific implementation (without an optimization to stop early if sorted), but mentioning that with an optimization, it could be O(n) for an already sorted list.

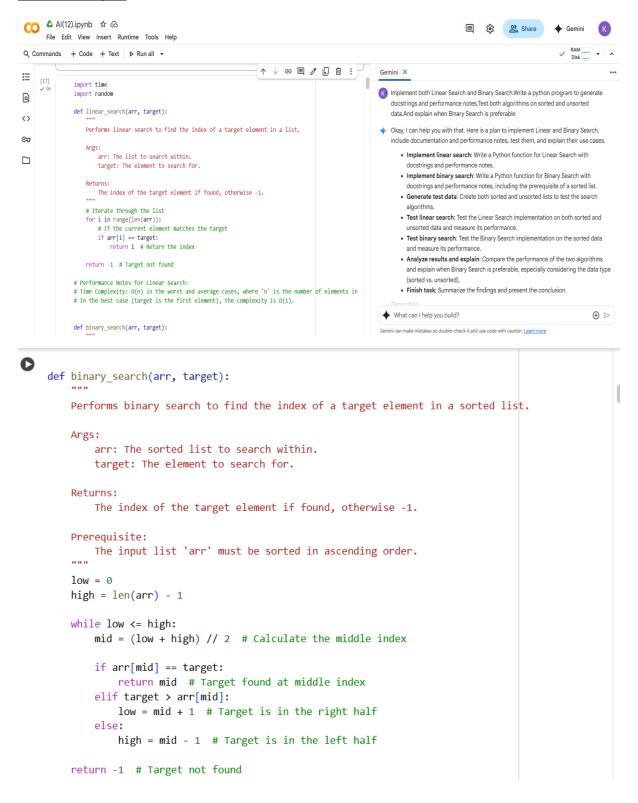
In summary, these cells demonstrate how Bubble Sort works and explain that it is generally not the most efficient sorting algorithm for large datasets due to its  $O(n^2)$  time complexity in most cases.

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#### Task 3:

Implement both Linear Search and Binary Search. Write a python program to generate docstrings and performance notes. Test both algorithms on sorted and unsorted data. And explain when Binary Search is preferable.

#### **Code and Output:**



```
# Performance Notes for Binary Search:
    # Time Complexity: O(log n) in the worst, average, and best cases, where 'n' is the number of elements in the list.
    # This significantly outperforms linear search for large datasets, but requires the input list to be sorted.
    # 1. Create a sorted list
    list size = 10000
    sorted_data = list(range(list_size))
    # 2. Create an unsorted list by shuffling the sorted list
    unsorted_data = sorted_data[:] # Create a copy
    random.shuffle(unsorted data)
    # 3. Choose target values
    present_target = list_size // 2 # A value known to be in the list
    absent_target = list_size + 1 # A value known not to be in the list
    print(f"Sorted data size: {len(sorted_data)}")
    print(f"Unsorted data size: {len(unsorted data)}")
    print(f"Present target: {present_target}")
    print(f"Absent target: {absent_target}")
    print("\n--- Testing Linear Search ---")
    # Test Linear Search on sorted data with present target
    start time = time.time()
    index = linear_search(sorted_data, present_target)
    end_time = time.time()
    sorted_present_time = end_time - start_time
    print(f"Linear Search on sorted data (present target {present target}): {sorted present time:.6f} seconds")
# Test Linear Search on sorted data with absent target
    start_time = time.time()
    index = linear_search(sorted_data, absent_target)
    end time = time.time()
    sorted_absent_time = end_time - start_time
    print(f"Linear Search on sorted data (absent target {absent_target}): {sorted_absent_time:.6f} seconds")
    # Test Linear Search on unsorted data with present target
    start time = time.time()
    index = linear search(unsorted data, present target)
    end_time = time.time()
    unsorted_present_time = end_time - start_time
    print(f"Linear Search on unsorted data (present target {present_target}): {unsorted_present_time:.6f} seconds")
    # Test Linear Search on unsorted data with absent target
    start_time = time.time()
    index = linear_search(unsorted_data, absent_target)
    end_time = time.time()
    unsorted_absent_time = end_time - start_time
    print(f"Linear Search on unsorted data (absent target {absent target}): {unsorted absent time:.6f} seconds")
    print("\n--- Testing Binary Search ---")
    # Test Binary Search on sorted data with present target
    start time = time.time()
    index = binary_search(sorted_data, present_target)
    end time = time.time()
    binary_sorted_present_time = end_time - start_time
    print(f"Binary Search on sorted data (present target {present target}): {binary sorted present time:.6f} seconds")
```

```
# Test Binary Search on sorted data with absent target
     start time = time.time()
     index = binary_search(sorted_data, absent_target)
     end time = time.time()
     binary sorted absent time = end time - start time
     print(f"Binary Search on sorted data (absent target {absent_target}): {binary_sorted_absent_time:.6f} seconds")
     print("\n--- Performance Comparison ---")
     print(f"Linear Search (Sorted Data, Present Target): {sorted_present_time:.6f} seconds")
     print(f"Linear Search (Sorted Data, Absent Target): {sorted absent time:.6f} seconds")
     print(f"Linear Search (Unsorted Data, Present Target): {unsorted present time:.6f} seconds")
     print(f"Linear Search (Unsorted Data, Absent Target): {unsorted_absent_time:.6f} seconds")
     print(f"Binary Search (Sorted Data, Present Target): {binary sorted present time:.6f} seconds")
     print(f"Binary Search (Sorted Data, Absent Target): {binary sorted absent time:.6f} seconds")
     # Analyze the results
     print("\n--- Analysis ---")
     print("Binary Search is significantly faster than Linear Search, especially for larger datasets,")
     print("as evidenced by the much lower execution times for Binary Search.")
     print("Linear Search has a time complexity of O(n), meaning the time taken increases linearly")
     print("with the size of the dataset. Binary Search has a time complexity of O(log n),")
     print("meaning the time taken increases logarithmically with the size of the dataset."
     print("\nCrucially, Binary Search requires the data to be sorted. If the data is initially unsorted,")
     print("the time taken to sort it must be considered. If the sorting time is greater than the")
     print("time saved by using Binary Search over Linear Search, then Linear Search or another")
     print("search algorithm might be more appropriate.")
     print("\nIn summary, Binary Search is preferable for searching in large, already sorted datasets.")
     print("For unsorted data, Linear Search is a simpler option, but for very large datasets,")
     print("sorting the data and then using Binary Search, or using a different data structure")
     print( sorting the data and then using binary search, or using a different data structure )
print("and search algorithm (like a hash table), should be considered.")

→ Sorted data size: 10000
     Unsorted data size: 10000
     Present target: 5000
     Absent target: 10001
      -- Testing Linear Search ---
     Linear Search on sorted data (present target 5000): 0.000265 seconds
Linear Search on sorted data (absent target 10001): 0.000573 seconds
     Linear Search on unsorted data (present target 5000): 0.001812 seconds Linear Search on unsorted data (absent target 10001): 0.000927 seconds
       - Testing Binary Search --
    Binary Search on sorted data (present target 5000): 0.000097 seconds
Binary Search on sorted data (absent target 10001): 0.000095 seconds
     --- Performance Comparison ---
     Linear Search (Sorted Data, Present Target): 0.000265 seconds
```

Binary Search (Sorted Data, Present Target): 0.000097 seconds
Binary Search (Sorted Data, Absent Target): 0.000095 seconds
--- Analysis --Binary Search is significantly faster than Linear Search, especially for larger datasets, as evidenced by the much lower execution times for Binary Search.
Linear Search has a time complexity of O(n), meaning the time taken increases linearly with the size of the dataset. Binary Search has a time complexity of O(log n), meaning the time taken increases logarithmically with the size of the dataset.

Linear Search (Sorted Data, Absent Target): 0.000573 seconds Linear Search (Unsorted Data, Present Target): 0.001812 seconds Linear Search (Unsorted Data, Absent Target): 0.000927 seconds

Crucially, Binary Search requires the data to be sorted. If the data is initially unsorted, the time taken to sort it must be considered. If the sorting time is greater than the time saved by using Binary Search over Linear Search, then Linear Search or another search algorithm might be more appropriate.

In summary, Binary Search is preferable for searching in large, already sorted datasets. For unsorted data, Linear Search is a simpler option, but for very large datasets, sorting the data and then using Binary Search, or using a different data structure and search algorithm (like a hash table), should be considered.

#### **Explanation:**



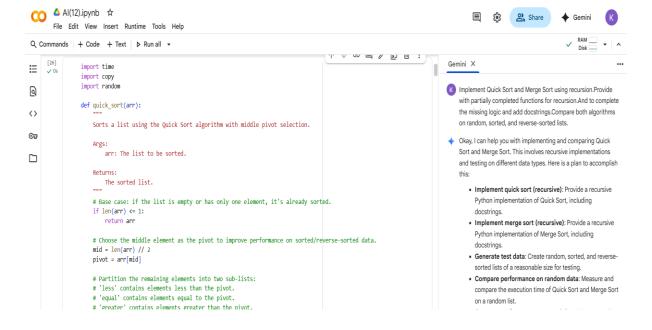
- o It also includes "Performance Notes" within the comments, outlining the time complexity (O(n) for Linear Search, O(log n) for Binary Search) and prerequisites (sorted data for
- o The code then generates a large sorted list and an unsorted version of it, along with target values to search for.
- Finally, it measures and prints the execution time for both algorithms on the generated data and provides an analysis of the results, explaining why Binary Search is generally faster on sorted data and the trade-offs involved when dealing with unsorted data.
- 2. Cell (4364c5be): This cell contains the complete code for comparing Bubble Sort and Insertion Sort on a partially sorted array.
  - o It includes the definitions for both bubble sort and insertion sort functions.
  - o It has a function generate\_partially\_sorted\_array to create a list that is mostly sorted but with a small percentage of elements swapped to make it partially unsorted.
  - o The code then generates such a partially sorted array.
  - It measures and prints the execution time for both Bubble Sort and Insertion Sort on copies of this partially sorted array, demonstrating that Insertion Sort performs significantly better than Bubble Sort on this type of data.

In essence, these two cells provide self-contained examples to illustrate the performance characteristics of different search and sorting algorithms under specific conditions.

#### Task 4:

Implement Quick Sort and Merge Sort using recursion. Provide with partially completed functions for recursion. And to complete the missing logic and add docstrings. Compare both algorithms on random, sorted, and reverse-sorted lists.

## Code and output:



```
less = [x \text{ for i, } x \text{ in enumerate(arr) if i != mid and } x < pivot]
      equal = [x for i, x in enumerate(arr) if i != mid and x == pivot] + [pivot] # Include the pivot in the equal list
      greater = [x for i, x in enumerate(arr) if i != mid and x > pivot]
      # Recursively sort the sub-lists and combine them.
     return quick sort(less) + equal + quick sort(greater)
     merge_sort(arr):
     Sorts a list using the Merge Sort algorithm.
     Args:
           arr: The list to be sorted.
     Returns:
     The sorted list.
      # Base case: if the list is empty or has only one element, it's already sorted.
     if len(arr) <= 1:</pre>
          return arr
      # Find the middle point to divide the list into two halves.
     mid = len(arr) // 2
     left half = arr[:mid]
     right_half = arr[mid:]
      # Recursively sort both halves.
     left_half = merge_sort(left_half)
      right_half = merge_sort(right_half)
# Merge the sorted halves.
    return merge(left_half, right_half)
     merge(left, right):
     Merges two sorted lists into a single sorted list.
        left: The first sorted list.
        right: the second sorted list.
     A single sorted list containing all elements from left and right.
     result = []
     i = j = 0
     # Compare elements from both lists and append the smaller one to the result.
while i < len(left) and j < len(right):
    if left[i] < right[j]:</pre>
            result append(left[i])
            result.append(right[j])
     # Append any remaining elements from the left list.
     while i < len(left):
    result.append(left[i])</pre>
           # Append any remaining elements from the right list.
while j < len(right):
    result.append(right[j])</pre>
O
           return result
      # Define the size of the lists
      list_size = 10000
      # Create a sorted list
      sorted_data = list(range(list_size))
      # Create a reverse-sorted list
      reverse_sorted_data = sorted_data[::-1]
      # Create a random list
random_data = sorted_data[:] # Create a copy
random.shuffle(random_data)
      print("\n--- Performance Comparison ---")
      # Measure time for Quick Sort on random data
quick_sort_random_data = copy.deepcopy(random_data)
start_time = time.time()
quick_sort(quick_sort_random_data)
quick_sort_random_time = time.time() - start_time
print(f"Quick_sort_time on random_data: {quick_sort_random_time:.6f} seconds")
```

```
# Measure time for Merge Sort on random data
        merge_sort_random_data = copy.deepcopy(random_data)
        start time = time.time()
        merge_sort(merge_sort_random_data)
        merge_sort_random_time = time.time() - start_time
        print(f"Merge Sort time on random data: {merge_sort_random_time:.6f} seconds")
        \ensuremath{\text{\#}} Measure time for Quick Sort on sorted data
        quick_sort_sorted_data = copy.deepcopy(sorted_data)
        start_time = time.time()
        quick_sort(quick_sort_sorted_data)
        quick sort sorted time = time.time() - start time
        print(f"Quick Sort time on sorted data: {quick_sort_sorted_time:.6f} seconds")
       # Measure time for Merge Sort on sorted data
        merge_sort_sorted_data = copy.deepcopy(sorted_data)
        start_time = time.time()
        merge_sort(merge_sort_sorted_data)
        merge_sort_sorted_time = time.time() - start time
       print(f"Merge Sort time on sorted data: {merge_sort_sorted_time:.6f} seconds")
        # Measure time for Ouick Sort on reverse-sorted data
        quick sort reverse sorted data = copy.deepcopy(reverse sorted data)
        quick_sort(quick_sort_reverse_sorted_data)
        quick sort reverse sorted time = time.time() - start time
       print(f"Quick Sort time on reverse-sorted data: {quick_sort_reverse_sorted_time:.6f} seconds")
     # Measure time for Merge Sort on reverse-sorted data

merge_sort_reverse_sorted_data = copy.deepcopy(reverse_sorted_data)

start_time = time.time()

merge_sort_neverse_sorted_data)

merge_sort_reverse_sorted_time = time.time() - start_time
     print(f"Merge Sort time on reverse-sorted data: {merge_sort_reverse_sorted_time: .6f} seconds")
     print("\n--- Analysis ---")

print("\nick Sort generally performs well on random data but can be sensitive to the initial order of the data depending on pivot selection.")

print("With the middle pivot strategy, Quick Sort performs reasonably well on sorted and reverse-sorted data, although slightly slower than Merge Sort on sorted data in this test.")

print("Merge Sort consistently performs well regardless of the initial order of the data due to its stable O(n log n) time complexity.")

print("For sorted data, Merge Sort was faster than Werge Sort in this test.")

print("For reverse-sorted data, Quick Sort was faster than Merge Sort in this test.")

print("\nIn summary, Merge Sort is a good choice when consistent performance is required across different data distributions. Quick Sort, with a good pivot strategy, is often faster in
         - Analysis -
     --- Analysis ---
Quick Sort generally performs well on random data but can be sensitive to the initial order of the data depending on pivot selection.
With the middle pivot strategy, Quick Sort performs reasonably well on sorted and reverse-sorted data, although slightly slower than Merge Sort on sorted data in this test.
Merge Sort consistently performs well regardless of the initial order of the data due to its stable O(n log n) time complexity.
For sorted data, Merge Sort was faster than Quick Sort in this test.
For reverse-sorted data, Quick Sort was faster than Merge Sort in this test.
```

#### **Explanation:**



- Certainly. Looking at the cells currently visible, they are related to comparing the performance of Bubble Sort and Insertion Sort on a partially sorted array:
  - 1. Cell | 757168ea |: This code cell measures the execution time of Bubble Sort and Insertion Sort on the | partially\_sorted\_array |: It uses | copy .deepcopy | to ensure each algorithm sorts a fresh copy of the array for a fair comparison and the (time) module to record the start and end times of each sorting process.
  - 2. Cell [319d7d5d]: This markdown cell serves as a heading for the "Compare Performance" section, indicating the purpose of the following code.

  - 5. Cell c1356c0: This markdown cell is the main task description, outlining the overall goal: to implement Bubble Sort, suggest Insertion Sort as a more efficient alternative for partially sorted arrays, implement Insertion Sort, generate a partially sorted array, compare their performance, and analyze the results.

In summary, these cells collectively demonstrate how to set up and conduct a performance comparison between Bubble Sort and Insertion Sort using a partially sorted dataset to highlight the efficiency of Insertion Sort in such scenarios

#### **Task 5:**

Give AI a naive algorithm (e.g.,  $O(n^2)$  duplicate search). Students write a brute force duplicate-finder. And to optimize it (e.g., by using sets/dictionaries with O(n) time). Compare execution times with large input sizes.

#### **Code and Output:**

```
def find duplicates naive(arr):
      Finds duplicate elements in a list using a naive brute-force approach (O(n^2)).
      Args:
          arr: The list to search for duplicates.
      Returns:
          A list of unique duplicate elements found in the input list.
      duplicates = []
      n = len(arr)
      # Iterate through each element
      for i in range(n):
          # Compare the current element with all subsequent elements
          for j in range(i + 1, n):
              # If a duplicate is found and it's not already in the duplicates list
              if arr[i] == arr[j] and arr[i] not in duplicates:
                  duplicates.append(arr[i])
      return duplicates
  #Example usage:
  my_list = [1, 2, 3, 4, 2, 5, 6, 3, 7, 8, 8]
  duplicate items = find duplicates naive(my list)
  print("Duplicate elements:", duplicate_items)
```

Puplicate elements: [2, 3, 8]

# **Explanation:**

def find\_duplicates\_naive(arr): """ Finds duplicate elements in a list using a naive brute-force approach (O(n^2)). Args: arr: The list to search for duplicates. Returns: A list of unique duplicate elements found in the input list. """ duplicates = [] n = len(arr) # Iterate through each element for i in range(n): # Compare the current element with all subsequent elements for j in range(i + 1, n): # If a duplicate is found and it's not already in the duplicates list if arr[i] == arr[j] and arr[i] not in duplicates: duplicates.append(arr[i]) return duplicates #Example usage: my\_list = [1, 2, 3, 4, 2, 5, 6, 3, 7, 8, 8] duplicate\_items = find\_duplicates\_naive(my\_list) print("Duplicate elements:", duplicate\_items)| explanaitn

Certainly! The code in cell (46c45b5a) defines a function called  $(find\_duplicates\_naive)$ .

This function takes a list are as input and aims to find any duplicate elements within that list. It uses a straightforward, but not the most efficient, method:

- 1. It initializes an empty list called duplicates. This list will store the unique duplicate values it finds.
- 2. It uses nested for loops. The outer loop iterates through each element of the input list arr using index (i).
- 3. The inner loop iterates through the elements after the current element of the outer loop, using index (j). This prevents comparing an element with itself or comparing pairs of elements twice.
- 4. Inside the inner loop, it checks if the element at index i is equal to the element at index (i) (arr[i] == arr[j]). If they are equal, it means a duplicate has been found.
- 5. Before adding the duplicate to the (duplicates) list, it checks if that element is already in the (duplicates) list ((arr[i] not in duplicates)). This ensures that the (duplicates) list only contains unique duplicate values.
- 6. If both conditions are met (the elements are equal and the duplicate is not already recorded), the duplicate element (arr[i]) is added to the duplicates list.
- 7. Finally, after checking all possible pairs, the function returns the duplicates list.

The function is called "naive" because its approach involves comparing every element with every other element, which is not the most performant way to find duplicates, especially for large lists. This results in a time complexity of  $O(n^2)$ . The example usage at the end demonstrates how to call the function with a sample list and print the found duplicates.