Flux Ralance Analysis (FRA

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INTRODUCTION

Final basions analysis (FRF) evaluates the metabolic fluid disblackoil. "And is one of the noter used modeling appointment for manufact operation." The applications of FRFs for modeline speciment belongs include prediction of the growth man, uplace which requires incommod training and manufactures included in the standard part is assessed as a facility and in a facility and included in manufactures and included in the standard part of a standard

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Equation 1: Formula of standard R

Suppose To instruction discharge leads to find the foreign continues one or more reaction fluxes to form what is served the objective function, and where $a,b,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ where $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ in $a,b'\in \mathcal{C}$ and $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ in $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ in $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ in $a,b'\in \mathcal{C}$ in $a,b'\in \mathcal{C}$ is a statistic matrix of $a,b'\in \mathcal{C}$ i

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1. Standard FBA
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2. Spanse FBA
2. Metabolite dilution FBA (mdFBA)
4. Geometric FBA

5. Parsimonious erzyme usage Flux Balance Analysis (pFBA) 6. Dynamic FBA

8. Flux enrichment analysis (FEA)

8. Flux enrichment analysis (FEA)

EQUIPMENT SETUP Initialise The Cobra Toolbox and set the solver

If necessary, initialise the cobra toolbox

If necessary, initialise the coora to

Institute ratio base

For solving LP problems in a FBA analysis, cetain solvers are required and can be set using the unanyecuter attotives function:

The present subsidiar our with girls continue, which does not require additional installation and configuration. Although, for the analysis of large models in

recommended to use the <u>COSTOR</u> package.

Setup the appropriate solver for the machine you are using by removing the "n." (comment sign for only the desired solver.

changeCobradalwer('qlpk','all'); % changeCobradalwer('toolab colos".'all');

.....

This satural will use the generic model of the human celular mestabolism¹, Record 2.0. Other COSRA models, including Record 3, may also be sur with this substant. For information or metabolities structures and reactions, and to deveload the based COSRA model releases, visit the Virsual Metabolic Human-Satisface (VMH, May January 184).

Sefure proceeding with the simulations, load the model into the workspace

clean CHTDS
modelExisting = "Recol.model.mat";
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modelExisting = (Recol.model.mod

In this tatorial we assume, that the cellular objectives include energy production or optimisation of uptake rates and by-product secretion for various physiological

1. Standard FBA

1. Assistance 1946.
Standard FBA predicts an optimal solution for a cellular objective within a given set of constraints on a metabolic network (see Equation 1). Constraints on the network see set by seleging limits on the uptake, consumption or production of mentabolities in macricos.

The time to determine a FBA solution depends on the size of the genome-scale model and is commonly less than a second for a medium sized model. Calculating maximal ATP energy production under serobic conditions:

For each new simulation, the original model will be copied to a new variable. This preserves the constraints of the original model to perform further simulations with new commander. Additionally, this method of resusting the model avoids confusion while performing multiple simulations at the same time. Interliamnistic is expect.)

monitorization is assert;

The ATP demandscript, i.e., the storm within the model is a reaction that involves hydrolysis of ATP to AZP, PI and proton in the optional or introducer's real bulleties. "On size of "Is.

The ATP demands of the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On size of "Is.

The ATP demands of the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On size of "Is.

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The ATP demands of the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the optional or introducer's real bulleties." "On the ATP to AZP, PI and proton in the ATP to AZP, PI and PI and

We will set this reaction as our objective with the "whaneyeds-year-lave" command. Maximising the flux through the ATP demand reaction will result in the network producing a maximal amount of ATP (up to the lint of the reaction).

sodelaershic = changebjective (sodelaershic, 'DE_HTP_C');
The glucose and ovgget, in this case, are provided in high amounts for calculating the flux through ATP demand.

The "example transmission from the first constraints of the lower ("), upper ("), or both the bounds ("), of the specified reaction. Here, we will strange the maximal upsake of glocole to 20 (Intolining)DW and of ougges to 1000 (Intolining)DW. The upsake of ougges is effectively unconstrainted (i.e. intolin).

w modelaremic = changestromount (modelaremic, "Mr_QD($\mathcal{Q}[s]$ ", -20, "1")) w for Rocco 2.8 uncomment these lines and wood-laremic of changestromount (modelaremic, "Mr_QD(\mathcal{Q} ", -210, "1")) w comment the lines below. Some consideration of complexity of the complexity of the complexity of the complexity of the complexity "-4100, "1" (1)", "-4100, "1" (1)", "-4100, "1" (1)", "-4100, "1" (1)", "-4100, "1", "4100, "1", "4100, "4100, "1", "4100, "41

The function eye is all excessions calculates one of the optimal elabora for a (maximum or retirmum) objective reaction within the defined solution space, in the slowe example, the maximum function through the <u>data are in a</u> 6-device).

[Restaurable: a splitterschelland*, (calcularables, "sair").

Anticipated results

When coppen and all carbon sources (internal and external) are provided the flux through ATP demand reaction can reach its maximum rate of 1000 PF

Troubleshooting

If there are multiple carbon sources available in the model, it may be necessary to specify more constraints in order to examine the effect of a single carbon source on ATP production.

To avoid this issue, all external carbon sources need to be closed with the exception of the single carbon source of interest.

Voluming the upstale of all energy and surges sources

(exchibod), purposal = fraids/carbo(each);

paramon,uptBoot) = TindmrCKsnc(momet); uptakec = model.rxnc(uptBool);

% modelalter = model; % modelalter = champetusbounds(modelalter, uptakes, 0, 'b'); % modelalter = champetusbounds(modelalter, 'BX)900026(m)', -2008, 'l');

n that does not contain defined Subsystem is n to find uptake exchange reactions with following or n [seläxc, selopt] = findExchans(model);

% Selecting from the exchange uptake reactions those % which contain at least 1 carbon in the metabolites included in the reacti subuptakehodel = extractionbruck(shoot), uptake();

cubuptakeModel = extractioDMetwork(model, uptakec); hitaminimum = fisoCarbonnas(cubuptakeModel,1); * Closing the uptake of all the carbon sources modelaiter = model;

madestires - model; model madestire, internations, \$, "0"]; consider a special madestires of the madestire o

wanagan = ("M_ABP, "M_ABP|"), "M_

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maximum til a maximi a maximi
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Anticipated results

Compared to the sensitic condition, ansensitic condition with only glucose as an energy source has reduced that through ATP cemand (bit PhositimingDM), signifying the need to arrige to it not the colditive phositynization. The results are dependent on the model you are using. For Record 3.0, under assentition condition with only glucose as an energy source, the faut and "PM devenance (she further institution) pdf.

2.Sparse FBA

Spanse FBA calculates the optimal solution of an objective function and finds the smallest set of reactions that can carry flux to achieve the objective. Spanse FBA minimises the number of reactions by keeping same maximal objective;

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Javan.
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Equation 2: Formula of Spanse

where the last constraint is optional and represents the requirement to safety an optimal objective value P² derived from any solution to a FDA problem. This approach is used to check for minimal sets of reactions that either should be active or should not be active in a flux balance model that is representative of a

[viparce, sparsekumbos], eccential/kumbool] = sparse/Mm(model, somecestr,...

```
As an optional input, there are different appointation types of zero-norm (only available when ministerin = "serve"). Default is eappenE.1.
```

```
pedia': Capped-La norm
: Exponential function
: Logarithmic function
a': I SCAD function
```

' : :math('Lg' norm with :math('p < 0')
: :math('Lg' norm with :math('0 < p < 1')
: Li norm
: : try all approximations and return the best result

Timing

The sine to determine a eyaxwerths j solution depends on the size of the genome-scale model and is taking from ≤ 1 second for a 1,000 reaction model, to ≤ 2 second for a model with more than 10,000 reaction model and p second for a model with more than 10,000 reaction model and p second for a 1,000 reaction model and glucose only conditions.

```
modelspar = modelsiter;

% Far Record.E model :

**modelspar = champebrohoused (modelspar, 'Exglic_D(e)', -28, 'l');

**modelspar = champebrohoused (modelspar, 'Exglic_D', e, 'l');

**modelspar = champebrohoused (modelspar, 'Exglie)', e, 'l');

**modelspar = champebrohoused (modelspar, 'Exglie)', -28, 'l');
```

modelupar (inapplicational profit (modelupar, "KL_02(n)", n, "-1");

societupar (inapplicational (modelupar, "KL_02(n)", n, "-1");

societupar (inapplicational (modelupar, "M_15_C");

(inparte, guarostation), eccential/bodice)] = quarceffix(modelupar, "mor");

Anticipated results:

 Interceptant research
 Commonly, a sparse FBA solution will have much smaller number of active reactions compared to a standard FBA on the same model will The budglate systematical and exceent Lot tracked return vectors with 1 and 4%, with sparse and essential exactions respectively.

endiplist oper-vertice/level. And research active-level return vectors with 1 and 0%, with sparse and essential reactions respectively, goldy the sparse flux solution, but only the non-over fluxes.

```
if abs(vaparce(1)) > 20-0
fprintf('%1.3f \t %1\0', vaparce(1), modelopar.nunc(1))
and
d
```

A Metabolis distinct flat behavior analysis intel® 100 flat is swinter of PRA for pedicing nethods for adobtation by accounting for growth associated distinct of all metabolises in a contract dependent mones. A Adobtation for all metabolises in a contract dependent mones. A Adobtation for the function number of produced by the selected of these up from the

surrounding m Timing

training

Since this is a MIXED integer Problem it can take a long time to solve.

Calculating ATP energy production under serobic condition using mdFRA:

```
In this function, there is an optional output newtors items, that represent reactions that are only active in this analysis.

In the volidal calculation can be pronounced with this Record 3.28 model.

In modellal is expected, the pronounced control of the property of th
```

modelnd = changedbjective|sodels
[col, newActives] = mdFBA|sodels

Troubleshooting:

An a model does not have a familie solution and the inner "see Terral Latertanians" are

% clear modeled
modelcossl = modelalter;
modelcossl = channelling

modelnoss! = changeObjective(modelnoss), 'DM_STp.C.'); [sol, newhotives] = mdFRM(modelnoss), 'getInvalidSalation', true)

Sometimes where an FSN analysis of a model with the same objection function and constraints in our many times, or using different LP logistims, we may get different and of studies for included instances in the desirable in the constraints and the same objective and only the same objective and the

This issue can be solved with wither of the following the methods

• geometric order, which provides a standard, central and reproducible solution,

p yrax, which provides a solution based on the minimal fluxes through the model, and classify each gene according to how it combinate to the optimal solution.

4. Geometric FBA

The geometric FBA solves the emailest frame that comains all sets of optimal FBA solutions and poets a set of multiple finant programming problems.
This FBA analysis applies iterations, where by each iteration reduces the permissible solution space. After a finite number of iterations, it neceives one single

% DEAGE: % flux = geometricFRM/model, varance

Timing:

The time to determine a geometric FBA solution depends on the size of the genome-scale model and the number of bestions. For a model with more than 10,000

mactions and several iterations takes > Xillainutes.

Calculating ATP energy production under assemble conditions using geometric FBA:

% modelgeo = changekonBounds (modelgeo, "EX_glc_0[e]", -20, "l"); % modelgeo = changekonBounds (modelgeo, "EX_glc(e]", -20, "l"); modelgeo = changekonBounds(modelgeo, "EX_glc(e]", -20, "l"); modelgeo = changekonBounds (modelgeo, "EX_glc(e]", θ , "l"); % modelgeo = changekonBounds (modelgeo, "EX_glc(e]", θ , "l");

modelgo = changeObjective(andelgo, 'M()F) ('); % NOOLSM: Depocing on the size of the most running this function might take very lon % FAMAGO = generatific (incolego, 'Tinsba', S=-2);

Display the unique fluxes from reactions, that are non-zero in the geometric FBA solution

 $\begin{array}{c} \text{fprintf("si,2f \ \ t \ sc\n", FBAgeo(1), acdelges.runs(1))}\\ \text{end} \\ \end{array}$

modelgeo = modelalter;

Toublehooding:

When the algorithm has convergence problems, change one of the optional injusts, x1 makes, into e.g. 1=-1. The default is 6 when there is flexibility to flux bounds

Error the optional parameters as parameter name followed by parameter value, Elux = geometric/FBA(model, 'epsilon', le=9)

Paralmonious enzyme usage Flox Balance Analysis (pFBA)
 The pFBA method was developed to achieve higher flux levels when more enzymes are required.¹

After performing the FRA to find the optimal value for the objective function, gFRA gets the answer of an another linear program to determine the flux distribution that minimises the total flux through all metabolic reactions in the model.

Training.
The time to determine a pFBA solution depends on the size of the genome-scale model and is taking from < 1 minute for a 1,000 reaction model, to 6 minutes for a model with more than 10,000 reaction.

we wancook as: n |Senetlasses Runflasses modellrrewPR| = sPRM/model, vararois| Given outputs in this function are:

Calculating ATP energy production under anaerobic conditions using pFRA:

* modelp = changeMunifounds (modelp, 'EX_c2[e]', 8, 'l'); modelp = changeMunifounds (modelp, 'EX_c2[e]', 8, 'l'];

Where Varagin' includes required inputs:

for init length (modelIrrevPM, lb) fprintf('%1.if \t %5\0', modelIrms/M.lb(1), modelIrms/M.rxms(1))

6. Dynamic FBA The dynamic FBA is an extension of standard FBA that accounts for cell outsize dynamics, implementing both dynamic (nonlinear programming) and static (LP)

optimisation of an objective function and applying constraints to the rates of change of flux in addition to the standard FBA constraints ⁶ The dynamic FBA method implemented in this function is essentially the same as the method described by Varma A, and B, C, Palsson².

modeldinamic = model;

* modeldinamic = changekumbounds (modeldinamic, "Ex_glc_B[e]", -20, "l"); * modeldinamic = changekumbounds (modeldinamic, "Ex_gle[e]", -200, "l"); * modeldinamic = changekumbounds (modeldinamic, "Ex_gle[e]", -200, "l"); * modeldinamic = changekumbounds (modeldinamic, "Ex_gle[e]", -200, "l"); modeldinamic = changeExcHounds (modeldinamic, 'EX_glc(e)', -20, 'b');

modeldinamic = changetembounds (modeldinamic, 'Er_32(e)', -1800, 'l'); modeldinamic = changetembounds (modeldinamic, 'Er_32(e)', -1800, 'l'); est = {'EX_Sic(e)' 'EX_sc(e)'};

onc = [18.8]; % Glucuse, Acetate concentration (all is set) Nec - 0.001; % initial biosec-Ct = 1.0/1000.0; % time steps

time = 1.0/dt; % cimulation time [concentrationMatrix, exchanges, time/ec.

Z. Rolax FDA Find the minimal set of relaxations on bounds and steady-state constraint to make the FBA problem feasible.

modelrelax = modelalter; FBAcel = relaxedFBA(sodelrelax)

The output PBB.++1 contains solution fields, where FIGURE , ν is set of reactions that need relaxation on steady state constraints $E^{\mu}\nu^{\mu}=0$; PSLvet .v is relaution on upper bound of reactions; 5. Flux enrichment analysis (FEA) The flux enrichment analysis calculates the likelihood that a set of fluxes would belong to a subsystem or pathway

PBLv+1 . p is relaxation on lower bound of reactions. Timing The time to calculate the FEA is < 1 second for any size of a model.

modelfea = model;

res = optimize(iModel(modelfea,'max'); activeReactions = find(res.x)

% You can also look for e.g. positive/negative/zeros flux reactio recultCell = FEM(modelfea, activeMeactions, 'subSystems')

[1] Otto, J. D., Thiele I., and Paleson, B. Ø. What is flux balance analysis? Nat. Bioschnol., 28(3), 245-248 (9310).

(I) Triele, I., et al. A community-driven global reconstruction of human metabolism. Nat. Biotechnol., 21(5), 419-425 (2013).

[3] Benyamini, T, Foiger, O., Ruppin, E., Schlomi, T. Flux balance analysis accounting for metabolite dilution. Genome Biology, 11(6) Rtd (2016) [4] Smallbone, K., and Simeonidis, E. Flux balance analysis: A geometric perspective. J Theor Biol., 25th: 311-315 (2008).

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