

Varying Parameters analysis

Authorship: Vanya Vassov, Systems Biochemistry Group, LCSB, University of Luxembourg

Reviewer(s): Thomas Pfau, Systems Biology Group, LSRE, University of Luxembourg

Ines Thiele, Molecular Systems Physiology Group, LCSB, University of Luxembourg

Armut Heinken, Molecular Systems Physiology Group, ICSB, University of Luxembourg

In this tutorial, we show how computations are performed by varying one or two parameters over a fixed range of numerical values.

EQUIPMENT SETUP

if necessary, initialise the cobra toolbox

[Twitter Follow](#)

```

> Checking if git is installed ... Done.
> Checking if the repository is tracked using git ... Done.
> Checking if curl is installed ... Done.
> Checking if remote can be reached ... Done.
> Initializing and updating submodules ... Done.
> Adding all the files of the CMakeToolbox ... Done.
> Define CMake output... set to sup.
> Retrieving models ... Done.
> TranslateMPLS is installed and working properly.
> Configuring solver environment variables ...
- [=====] SLURM_PATH: C:\Program Files\IBM\SLURM\SLURM_Studio\bin\slurm\bin\slurm
- [=====] GURU_PATH: C:\Program Files\IBM\SLURM\SLURM_Studio\bin\slurm\bin\slurm
- [=====] TOPAS_PATH: C:\slurmbin\
- [=====] INDEX_PATH : --> set this path manually after installing the solver ( see ANSI/ISO/IEC 15924
Done.
> Checking available solvers and solver interfaces ... Done.
> Setting default solvers ... Done.
> Saving the PATHS path ... Done.
> The PATHS path was saved in the default location.

- Summary of available solvers and solver interfaces

```

Support	LP	MLP	QP	MDP	SLP
cpus_direct	Yes	0	0	0	0
depTimes	Yes	0	-	-	-
gphk	Yes	1	1	-	-
quartzk	Yes	1	1	1	1
lms_cpus	Yes	0	0	-	-
swlib	Yes	1	-	-	1
morek	Yes	0	0	0	-
pkcs	Yes	1	-	1	-
quadWinet	Yes	0	-	-	0
lswlib_cpus	Yes	1	1	1	1
qmg	experimental	-	-	1	-
lswlib_swlib	experimental	-	-	-	1
quartzk_mus	legacy	0	0	0	0
lmsw_ql	legacy	0	-	-	-
lmsw_legacy	legacy	-	-	-	-
lp_valve	legacy	1	-	-	-
qgll	legacy	0	0	0	0
Total	-	0	3	6	3

+ Legend: - = not applicable, # = solver not compatible or not installed, I = solver installed

```

> You can solve LP problems using: 'glpk' - 'qpsolve' - 'mosek' - 'ipol' - 'lpsolve_cplex' - 'lp_solve'
> You can solve MIP problems using: 'glpk' - 'qpsolve' - 'lpsolve_cplex'
> You can solve QP problems using: 'qpsolve' - 'ipol' - 'lpsolve_cplex' - 'qpqp'
> You can solve MIP problems using: 'qpsolve' - 'lpsolve_cplex'
> You can solve NLP problems using: 'mosek' - 'lpsolve_cplex'

```

```

> Checking for available updates ...
--> You cannot update your fork using updateCoberturaTools(). [XINSHI @ develop].
Please use the MATLAB devTools (https://github.com/xinshihuang/MATLAB\_devTools).

```

For solving linear programming problems in the analysis, certain solvers are required

```
changeCubicalver ('guru', 'all', 3);
changeCubicalver ('gluk', 'all', 1);
```

```

> Solver for LPproblems has been set to glpk.
> Solver for MILPproblems has been set to glpk.
> Solver glpk not supported for problems of type MIP. Currently used: cswlp_solver
> Solver glpk not supported for problems of type MIP. Currently used: cswlp_solver
> Solver glpk not supported for problems of type GP. Currently used: cswlp_solver

```

The present tutorial can run with "glpk" package, which does not require additional installation and configuration. Although, for the analysis of large models is recommended to use the "gurobi" package. For detail information, refer to the solver installation guide: <https://github.com/leahcooper/cobrapy/blob/master/docs/source/installation/cobrapy.md>

PROCEDURE

Before proceeding with the simulations, the path for the model needs to be set up. In this tutorial, the used model is the generic model of human metabolism, Recon 3 [9]. Therefore, we assume, that the cellular objectives include energy production or optimisation of uptake rates and by-product secretion for various physiological functions of the human body. If Recon 3 is not available, please use Recon 2.

```

%For Recon3D Change the model
modelFilename = 'Recon3D_model.mat';
modelDirectory = getAbsolutePath(modelFilename); %Look up the folder for the distributed Models.
modelFilename = [modelDirectory filesep modelFilename]; % Get the full path. Necessary to be sure, that the right model is loaded
model = readModel(modelFilename);

```

If Recon3 is used, the reaction nomenclature needs to be adjusted:

```

model.rename(find(ismember(model.Lname,'EX_glc(e)')=={'EX_glc_p(e)'});
model.rename(find(ismember(model.Lname,'EX_glc(e)')=={'EX_glc_p(e)'});

```

TROUBLESHOOTING

If there are multiple energy sources available in the model. Specifying more constraints is necessary. If we do not do that, we will have additional carbon and oxygen-energy sources available in the cell and the maximal ATP production.

To avoid this issue, all external carbon sources need to be closed.

```

%Closing the uptake of all energy and oxygen sources
for i=1:length(model.Lname)
    if strcmp(model.Lname(i),'EX_',3)
        model.subsystems(i)='Exchange/demand reaction';
    end
end
ids=strcmp('Exchange/demand reaction', model.subsystems);
c=@();
for i=1:length(ids)
    if model.lb(ids(i))~=0
        c=c+1;
        uptake(c)=model.name(ids(i));
    end
end

modelalter = model;
modelalter = changeBounds(modelalter, uptake, 0, 'l');

% The alternative way to do that, in case you were using another large model,
% that does not contain defined subsystems is
% to find uptake exchange reactions with following codes:
% [cellVec, cellObj] = findReactions(model);
% uptakes = model.name(cellObj);
% Selecting from the exchange uptake reactions those
% which contain at least 1 carbon in the metabolites included in the reaction:
% subuptakeModel = extractSubNetwork(model, uptakes);
% hicarbonReactions = findCarbonReactions(subuptakeModel,1);
% Closing the uptake of all the carbon sources
% modelalter = model;
% modelalter = changeBounds(modelalter, hicarbonReactions, 0, 'l');

```

Robustness analysis

Robustness analysis is applied to estimate and visualise how changes in the concentration of an environmental parameter (exchange rate) or internal reaction effect on the objective [2]. If we are interested in varying v_i between two values, i.e., $v_{i,min}$ and $v_{i,max}$, we can solve f optimisation problems:

$$\begin{aligned}
 \max Z_i &= c^T v \\
 \text{s.t.} \quad & k = 1, \dots, l \\
 & S v = 0, \\
 \text{fixing} \quad & v_i = v_{i,min} + \frac{(j-1)}{(J-1)} * (v_{i,max} - v_{i,min}) \\
 \text{constraints} \quad & v_{min} \leq v \leq v_{max} \quad (i = 1, \dots, n, i \neq j)
 \end{aligned}$$

The function `robustnessAnalysis` is used for this analysis:

```

% [controlFlux, objFlux] = robustnessAnalysis(model, controlReactions, nPoints,...
% plotReactions, objReactionsType)

```

where inputs are a COBRA model, a reaction that has been analysed and optional inputs:

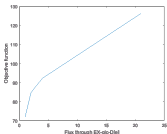
```
% INPUTS
% model          COBRA model structure
% controlRxn     Reaction of interest whose value is to be controlled
%
% OPTIONAL INPUTS
% nPoints        Number of points to show on plot (Default = 20)
% plotObjFlag    Plot results (Default true)
% objRxn         Objective reaction to be maximized
%                (Default = whatever is defined in model)
% objType        Maximize ('max') or minimize ('min') objective
%                (Default = 'max')
%
% OUTPUTS
% controlFlux    Flux value within the range of the maximum and minimum for
%                a reaction of interest
% objFlux        Optimal values of objective reaction at each control
%                reaction flux value
```

Here, we will investigate how robust the maximal ATP production of the network (i.e., the maximal flux through `DM_atp_c`) is with respect to varying glucose uptake rates and feed oxygen uptake.

```
modelRobust = modelAlter;
modelRobust = changeRxnBounds(modelRobust, 'EX_glc_0[e]', -10, 'b');
AtpRates = zeros(21, 1);
for i = 1:20
    modelRobust = changeRxnBounds(modelRobust, 'EX_glc_0[e]', -i, 'b');
    modelRobust = changeObjective(modelRobust, 'DM_atp_c');
    FBArobust = optimizeCbModel(modelRobust, 'max');
    AtpRates(i+1) = FBArobust.f;
end
plot(1:21, AtpRates)
```

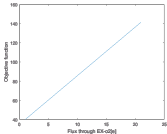
Warning: MATLAB has disabled some advanced graphics rendering features by switching to software OpenGL. For more information, click here.

```
xlabel('Flux through EX-glc-0[e]')
ylabel('Objective function')
```



We can also investigate the robustness of the maximal ATP production when the available glucose amount is fixed, while different levels of oxygen are available.

```
modelRobustoxy = modelAlter;
modelRobustoxy = changeRxnBounds(modelRobustoxy, 'EX_glc_0[e]', -20, 'b');
AtpRatesoxy = zeros(21, 1);
for i = 1:20
    modelRobustoxy = changeRxnBounds(modelRobustoxy, 'EX_o2[e]', -i, 'b');
    modelRobustoxy = changeObjective(modelRobustoxy, 'DM_atp_c');
    FBArobustoxy = optimizeCbModel(modelRobustoxy, 'max');
    AtpRatesoxy(i+1) = FBArobustoxy.f;
end
plot(1:21, AtpRatesoxy)
xlabel('Flux through EX-glc-0[e]')
ylabel('Objective function')
```



• Double robust analysis

Performs robustness analysis for a pair of reactions of interest and an objective of interest. The double robust analysis is implemented with the function `doubleRobustnessAnalysis()`:

```
% [controlFlux1, controlFlux2, objFlux] = doubleRobustnessAnalysis(model,...
% controlRun1, controlRun2, nPoints, plotResFlag, objRun, objType)
```

The inputs are a COBRA model, two reactions for the analysis and optional inputs:

```
% INPUTS
% model          COBRA model to analyze,
% controlRun1    The first reaction for the analysis,
% controlRun2    The second reaction for the analysis;
%
% OPTIONAL INPUTS
% nPoints        The number of flux values per dimension (Default = 20)
% plotResFlag    Indicates whether the result should be plotted (Default = true)
% objRun         is objective to be used in the analysis (Default = whatever
%               is defined in model)
% objType        Direction of the objective (min or max)
%               (Default = 'max')
```

```
modelRobustcov = modelAlter;
modelRobustcov = changeObjBounds(modelRobustcov, 'EX_glc_2[e]', -20, 'l');
modelRobustcov = changeObjBounds(modelRobustcov, 'EX_c2[e]', -10, 'l');
[controlFlux1, controlFlux2, objFlux] = doubleRobustnessAnalysis(modelRobustcov,...
'EX_glc_2[e]', 'EX_c2[e]', 20, 1, 'OBJ_obj_c_', 'max')
```

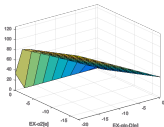
```

Double robustness analysis in progress ...
2% [
controlFlux1 =
-26.8888
-17.7223
-19.6851
-11.1676
-18.8982
-8.8227
-6.1013
-5.8578
-1.7886
8.8871

controlFlux2 =
-17.8888
-19.1111
-11.7223
-11.1013
-6.8516
-7.3556
-5.8887
-1.7778
-1.8889
8.8888

objFlux =
126.2946 126.7861 187.1179 97.3296 87.9413 78.3131 68.7668 /
121.7399 112.1012 182.3618 92.9767 83.5864 73.7982 64.2999 /
117.1846 107.5963 98.8892 88.4198 78.8315 69.2433 59.6158 /
112.6297 103.0416 93.8532 83.8609 74.2766 64.6884 55.1080 /
108.0748 98.4863 88.8983 79.3188 69.7217 60.1335 50.5612 /
103.5199 93.9314 84.3434 74.7912 65.1868 55.6385 45.9983 /
98.9650 89.3767 79.7884 70.2982 60.6418 51.0938 41.4354 /
94.4081 84.8218 75.2335 65.6453 56.0978 46.5487 36.8886 /
89.8532 80.2669 70.6786 61.0903 51.5428 42.0038 32.3356 /
33.3879 0 0 0 0 0 0

```



Phenotypic phase plane analysis (PhPP)

The PhPP is a method for describing in two or three dimensions, how the objective function would change if additional metabolites were given to the model [3].

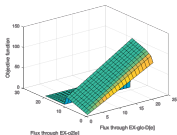
Essentially PhPP performs a `doubleRobustnessAnalysis()`, with the difference that shadow prices are retained. The code is as follows-

```

modelppp = modelalter;
ATPpppRates = zeros(21);
for i = 1:20
    for j = 1:20
        modelppp = changeRxnBound(modelppp, 'EX_glc_3(e)', -1, '0');
        modelppp = changeRxnBound(modelppp, 'EX_glc_6(e)', -1, '0');
        modelppp = changeObjctive(modelppp, 'DM_ATP_C_1');
        FBppp = optLinearCModel(modelppp, 'max');
        ATPpppRates(i+1,j+1) = FBppp.f;
    end
end

surf1(ATPpppRates) % 3d plot
xlabel('Flux through EX-glc-3(e)')
ylabel('Flux through EX-glc-6(e)')
zlabel('Objective function')

```

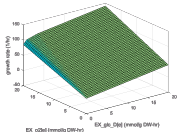
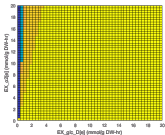


To generate a 2D plot: `plot2d(R2PhyObjPhase)`

Alternatively, use the function `phenotypePhasePlane()`. This function also draws the line of optimality, as well as the shadow prices of the metabolites from the two control reactions. In this case, control reactions are "EX_glc_D[e]" and "EX_c2[e]". The line of optimality signifies the state wherein, the objective function is optimal. In this case it is "EX_exp_e_".

```
modelPhpp = changedObjective(modelPhpp, "EX_exp_e_");
[growthRate, shadowPrice1, shadowPrice2] = phenotypePhasePlane(modelPhpp,...
    "EX_glc_D[e]", "EX_c2[e]");
```

generating Phpp



REFERENCES

- [4] Noorha A., et al. (2017). RecontMap: an interactive visualization of human metabolism. *Bioinformatics*, 33 (4): 805-807.
- [5] Edwards, J.S. and and Palsson, B. O. (2000). Robustness analysis of the Escherichia coli metabolic network. *Biotechnology Progress*, 16(8):927-39.
- [6] Edwards, J.S., Ramakrishna, R. and and Palsson, B. O. (2002). Characterizing the metabolic phenotype: A phenotype phase plane analysis. *Biotechnology and Bioengineering*, 77:27-36.