

Atomically resolve a metabolic reconstruction

Author(s): Hulda S. Haraldsdóttir and German A. Preciat Gonzalez, Systems Biochemistry Group, University of Luxembourg.

Reviewer(s): Catherine Clancy, Molecular Systems Physiology Group, University of Luxembourg.

INTRODUCTION

Genome-scale metabolic network reconstructions have become a relevant tool in modern biology to study the metabolic pathways of biological systems *in silico*. However, a more detailed representation at the underlying level of atom mappings opens the possibility for a broader range of biological, biomedical and biotechnological applications than with stoichiometry alone.

A set of atom mappings represents the mechanism of each chemical reaction in a metabolic network, each of which relates an atom in a substrate metabolite to an atom of the same element in a product metabolite (Figure 1). To atom map reactions in a metabolic network reconstruction, one requires chemical structures in a data file format (SMILES, MDL MOL, InChIs), reaction stoichiometries, and an atom mapping algorithm.

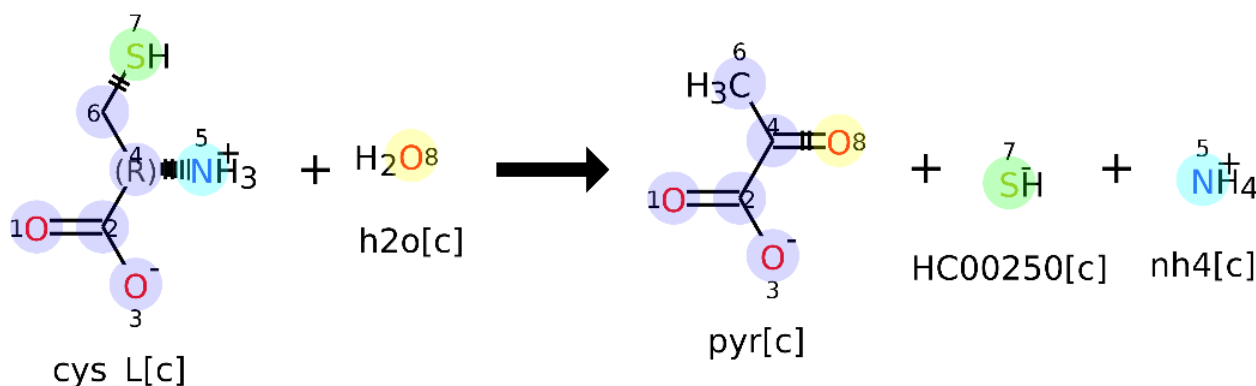


Figure 1. Set of atom mappings for reaction L-Cysteine L-Homocysteine-Lyase (VMH ID: r0193).

Metabolites chemical structures can be obtained by different approaches such as draw them based on the literature using chemoinformatic software, or obtain them from metabolic databases either manually or using a computational software as suggested in ¹. Here we recommend downloading the metabolites structures in MDL MOL format for the latest human metabolic reconstruction Recon 3 ² via the Virtual Metabolic Human database (VMH, <http://vmh.life>). Chemical structures and reaction stoichiometries from COBRA models are used to generate an MDL RXN file, which contains the information of a chemical reaction. Atom mapped reactions from Recon 3 can also be found in the VMH database in MDL RXN format. However, here we will atom map the chemical reactions using the Reaction Decoder Tool (RDT) algorithm ³, which was selected after comparing the performance of recently published algorithms ⁴. However, despite its good performance (accuracy and availability) RDT algorithm does not atom map hydrogen atoms.

In this tutorial, we will identify the conserved moieties using atom mapping data for the dopamine synthesis network (DAS) extracted from Recon 3² (Figure 2). Section 1 of the tutorial will cover obtaining and visualising an atom map of metabolic reactions, and section 2 of the tutorial covers the identification of conserved metabolic moieties.

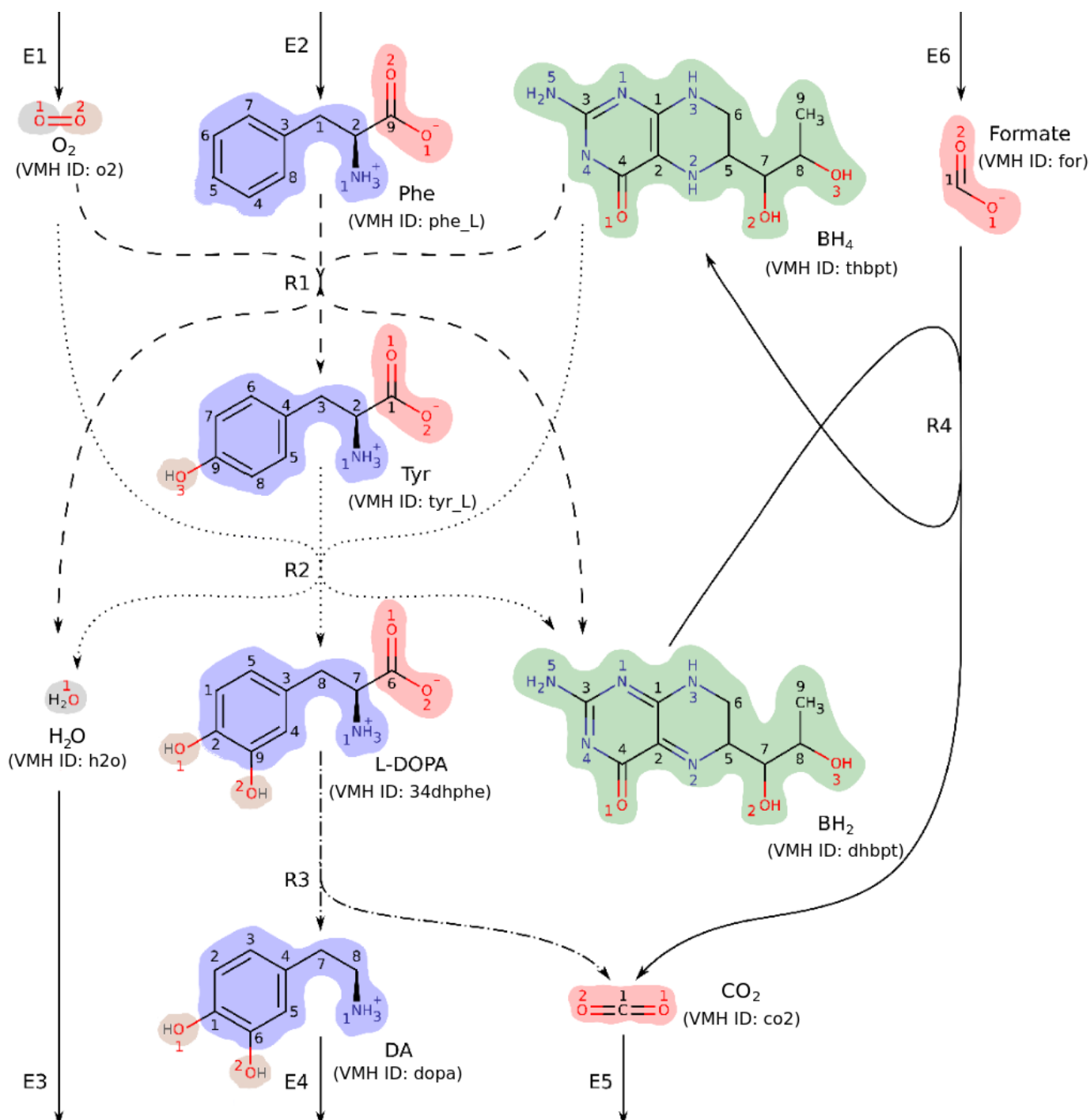


Figure 2: DAS: a small metabolic network consisting of reactions in the human dopamine synthesis pathway². Atoms belonging to the same conserved moiety have identically coloured backgrounds.

MATERIALS

To atom map reactions it is required to have Java version 8 and Linux. The atom mapping does not run on windows at present. Also, to standardise the chemical reaction format it is required to have JChem downloaded from ChemAxon with its respective license.

SECTION 1 Atom mapping of reactions

Atom mappings for the internal reactions of a metabolic network reconstruction are performed by the function `obtainAtomMappingsRDT`. The main inputs are a COBRA model structure and a directory

containing the molecular structures in MDL MOL format. For this tutorial, using the RDT algorithm, the atom mappings are generated based on the molecular structures contained in `cobratoolbox/tutorials/moieties/data/molFiles` (`molFileDir`) and the reconstructed DAS network without hydrogen atoms (`model`).

```
global CBTDIR
load([CBTDIR filesep 'tutorials' filesep 'atomicallyResolveReconstruction' filesep...
      'data' filesep 'subDas.mat'], 'model') % The subnetwork of the dopamine synthesis network
molFileDir = [CBTDIR filesep 'tutorials' filesep 'atomicallyResolveReconstruction' filesep...
              'data' filesep 'molFiles']; % The chemical structures of metabolites
```

The function `obtainAtomMappingsRDT` generates 4 different directories containing:

- the atom mapped reactions in MDL RXN format (directory *atomMapped*),
- the images of the atom mapped reactions (directory *images*),
- additional data for the atom mapped reactions (SMILES, and product and reactant indexes) (directory *txtData*), and
- the unmapped MDL RXN files (directory *rxnFiles*).

The input variable `outputDir` indicates the directory where the folders will be generated (by default the function assigns the current directory).

```
outputDir = [pwd filesep 'output'];
```

For some reactions, the RDT algorithm cannot compute the atom mappings (for a large reaction is generated an MDL RXN v3000 which is not compatible with the RDT algorithm). Therefore, is necessary to assign a maximum time of processing `maxTime` (by default the function assign 30 minutes as a maximum time for computing an atom mapping for a reaction).

```
maxTime = 1800; % seconds
```

The function `obtainAtomMappingsRDT` generates atom mapped reactions in a standard canonical format but it is **REQUIRED** to have a Chemaxon license installed. However, the reactions can be atom mapped without being standardised. The variable `isChemaxonInstalled` contains a logical value defined by the user if the license is installed or not.

```
isChemaxonInstalled = true; % Change variable to "true" if ChemAxon is installed
```

Now, let's obtain the atom map using `obtainAtomMappingsRDT`:

```
if ispc
    error('Error: atom mapping function should be run on Linux or MAC.')
else
    tic
    standardisedRxns = obtainAtomMappingsRDT(model, molFileDir, outputDir, maxTime, ...
        isChemaxonInstalled);
    toc
end
```

```
Generating RXN files.
Computing atom mappings for 4 reactions.
```

```
4 reactions were atom mapped
0 reactions are not standardised
0 reactions were not mapped
```

RDT algorithm was developed by:
SA Rahman et al.: Reaction Decoder Tool (RDT): Extracting Features from Chemical Reactions, Bioinformatics (2016), doi: 10.1093/bioinformatics/btw096
Elapsed time is 31.521840 seconds.

The output, `standardisedRxns`, is a list of atom mapped mass balanced reactions.

TIMING

The time to compute atom mappings for metabolic reactions depends on the size of the genome-scale model and the size of the molecules in the reactions. The above example may take ~1 min or less if `isChemaxonInstalled = false`.

Visualising results

The *images* directory contains a graphical representation of the atom mapped reactions. They show the bijection between atoms and each of the metabolite pools are coloured for an easy visualisation. Figure 3 shows the atom mapped reaction to produce dopamine and CO_2 from L-DOPA.

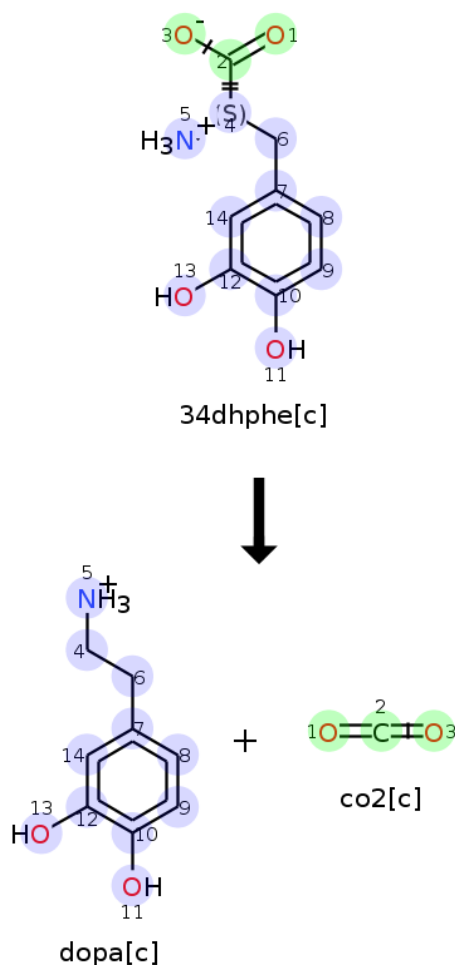


Figure 3: Reaction 3-hydroxy-L-tyrosine carboxy-lyase atom mapped (VMH ID: 3HLYCL) here represented as R3. Images generated by RDT algorithm, also shows where a reaction centre occurs.

The *rxnFiles* directory contains for all atom mapped reactions a corresponding MDL RXN file (Figure 4). Contained within these files are information of the chemical reaction, such as:

- the name of the reaction (on line 2 of the file),

- the chemical formula (on line 4 of the file),
- the number of substrates and products (on line 5 of the file), and
- specific information for each of the molecules (from line 6 onwards, after the identifier \$MOL).

```

1  $RXN
2  R1
3
4  phe_L[c] + thbpt[c] + o2[c] -> tyr_L[c] + dhbpt[c] + h2o[c]
5  3 3
6  $MOL
7  phe_L[c]
8  Mrv1637 03141717452D
9  InChIKey=COLNVLDHVVKWLRT-QMMGPOBSA-N
10 12 12 0 0 1 0 999 V2000
11 -0.7145 2.0625 0.0000 N 0 3 0 0 0 0 0 0 0 0 0 0 0 0
12 0.0000 2.4750 0.0000 C 0 0 1 0 0 0 0 0 0 0 0 0 0 0
13 0.7145 2.0625 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
14 0.7145 1.2375 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
15 1.4289 0.8250 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
16 1.4289 -0.0000 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
17 0.7145 -0.4125 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
18 0.0000 0.0000 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
19 0.0000 0.8250 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
20 0.0000 3.3000 0.0000 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0
21 -0.7145 3.7125 0.0000 O 0 5 0 0 0 0 0 0 0 0 0 0 0 0
22 0.7145 3.7125 0.0000 O 0 0 0 0 0 0 0 0 0 0 0 0 0 0
23 2 1 1 6 0 0 0
24 2 3 1 0 0 0 0
25 3 4 1 0 0 0 0
26 4 5 2 0 0 0 0
27 5 6 1 0 0 0 0
28 6 7 2 0 0 0 0
29 7 8 1 0 0 0 0
30 8 9 2 0 0 0 0
31 4 9 1 0 0 0 0
32 2 10 1 0 0 0 0
33 10 11 1 0 0 0 0
34 10 12 2 0 0 0 0
35 M CHG 2 1 1 11 -1
36 M END
37 $MOL
38 thbpt[c]

```

Figure 4: A MDL RXN file stored in the *rxnFiles* directory.

Specific information for each of the molecules includes the name of the metabolite, it's InChI key (if the metabolite does not contain an R group) and the number of atoms and bonds. Following this is the atom block, which contains detailed information on the coordinates, element, charge and atom mapping number for each of the atoms, and then finally, the bond block connects all the atoms in the metabolite.

```

regexp(fileread([outputDir filesep 'atomMapped' filesep 'R3.rxn']), '\n', 'split')

```

```

ans =
'$RXN'
'R3'
'Mrv1637      071201171820'
'34dhphe[c] -> dopa[c] + co2[c]'
' 1 2'
'$MOL'
'34dhphe[c]'
'Mrv1637 07121718202D

```

'InChIKey=WTDRDQBEARUVNC-LURJTMIESA-N'

' 14 14 0 0 1 0 999 V2000'
' -3.7934 0.8250 0.0000 N 0 3 0 0 0 0 0 0 0 0 1 0 0'
' -3.0789 1.2375 0.0000 C 0 0 1 0 0 0 0 0 0 0 2 0 0'
' -2.3645 0.8250 0.0000 C 0 0 0 0 0 0 0 0 0 0 3 0 0'
' -2.3645 -0.0000 0.0000 C 0 0 0 0 0 0 0 0 0 0 4 0 0'
' -1.6500 -0.4125 0.0000 C 0 0 0 0 0 0 0 0 0 0 5 0 0'
' -1.6500 -1.2375 0.0000 C 0 0 0 0 0 0 0 0 0 0 6 0 0'
' -2.3645 -1.6500 0.0000 C 0 0 0 0 0 0 0 0 0 0 7 0 0'
' -2.3645 -2.4750 0.0000 O 0 0 0 0 0 0 0 0 0 0 8 0 0'
' -3.0789 -1.2375 0.0000 C 0 0 0 0 0 0 0 0 0 0 9 0 0'
' -3.7934 -1.6500 0.0000 O 0 0 0 0 0 0 0 0 0 0 10 0 0'
' -3.0789 -0.4125 0.0000 C 0 0 0 0 0 0 0 0 0 0 11 0 0'
' -3.0789 2.0625 0.0000 C 0 0 0 0 0 0 0 0 0 0 12 0 0'
' -3.7934 2.4750 0.0000 O 0 5 0 0 0 0 0 0 0 0 13 0 0'
' -2.3645 2.4750 0.0000 O 0 0 0 0 0 0 0 0 0 0 14 0 0'
' 2 1 1 6 0 0 0 0'
' 2 3 1 0 0 0 0 0'
' 3 4 1 0 0 0 0 0'
' 4 5 2 0 0 0 0 0'
' 5 6 1 0 0 0 0 0'
' 6 7 2 0 0 0 0 0'
' 7 8 1 0 0 0 0 0'
' 7 9 1 0 0 0 0 0'
' 9 10 1 0 0 0 0 0'
' 9 11 2 0 0 0 0 0'
' 4 11 1 0 0 0 0 0'
' 2 12 1 0 0 0 0 0'
' 12 13 1 0 0 0 0 0'
' 12 14 2 0 0 0 0 0'

'M CHG 2 1 1 13 -1'

'M END'

'\$MOL'

'dopa[c]'

' Mrv1637 07121718202D'

'InChIKey=VYFYTYLLBUKUUH-UHFFFAOYSA-O'

' 11 11 0 0 1 0 999 V2000'
' 3.6536 2.2688 0.0000 N 0 3 0 0 0 0 0 0 0 0 1 0 0'
' 3.6536 1.4438 0.0000 C 0 0 0 0 0 0 0 0 0 0 2 0 0'
' 4.3680 1.0312 0.0000 C 0 0 0 0 0 0 0 0 0 0 3 0 0'
' 4.3680 0.2062 0.0000 C 0 0 0 0 0 0 0 0 0 0 4 0 0'
' 5.0825 -0.2063 0.0000 C 0 0 0 0 0 0 0 0 0 0 5 0 0'
' 5.0825 -1.0313 0.0000 C 0 0 0 0 0 0 0 0 0 0 6 0 0'
' 4.3680 -1.4438 0.0000 C 0 0 0 0 0 0 0 0 0 0 7 0 0'
' 4.3680 -2.2688 0.0000 O 0 0 0 0 0 0 0 0 0 0 8 0 0'
' 3.6536 -1.0313 0.0000 C 0 0 0 0 0 0 0 0 0 0 9 0 0'
' 2.9391 -1.4437 0.0000 O 0 0 0 0 0 0 0 0 0 0 10 0 0'
' 3.6536 -0.2063 0.0000 C 0 0 0 0 0 0 0 0 0 0 11 0 0'
' 1 2 1 0 0 0 0 0'
' 2 3 1 0 0 0 0 0'
' 3 4 1 0 0 0 0 0'
' 4 5 2 0 0 0 0 0'
' 5 6 1 0 0 0 0 0'
' 6 7 2 0 0 0 0 0'
' 7 8 1 0 0 0 0 0'
' 7 9 1 0 0 0 0 0'
' 9 10 1 0 0 0 0 0'
' 9 11 2 0 0 0 0 0'
' 4 11 1 0 0 0 0 0'

'M CHG 1 1 1'

'M END'

'\$MOL'

'co2[c]'

' Mrv1637 07121718202D'

'InChIKey=CURLTUGMZLYLDI-UHFFFAOYSA-N'

' 3 2 0 0 1 0 999 V2000'
' 6.8504 -0.2438 0.0000 O 0 0 0 0 0 0 0 0 0 0 14 0 0'
' 7.6754 -0.2438 0.0000 C 0 0 0 0 0 0 0 0 0 0 12 0 0'

```
'      8.5004    -0.2438    0.0000 0    0    0    0    0    0    0    0    0    0    13    0    0'
'  1  2  2  0  0  0  0'
'  2  3  2  0  0  0  0'
'M  END'
'
'
'
```

The *txtData* directory contains the TXT information of the reaction including the SMILES format, which holds the standard canonical format of the reaction, the reactant input atom index and the product input atom index.

```
regexp(fileread([outputDir filesep 'txtData' filesep 'R3.txt']), '\n', 'split')
```

```
ans =
'
'
'//'
'SELECTED AAM MAPPING'
'[0:1]=[C:2]([0:-:3])[CH:4]([NH3+:5])[CH2:6][C:7]:1:[CH:8]:[CH:9]:[C:10]([OH:11]):[C:12]([OH:13]):[CH:14]'
'
'
'//'
'REACTANT INPUT ATOM INDEX<->AAM ID'
'{1=5, 2=4, 3=6, 4=7, 5=8, 6=9, 7=10, 8=11, 9=12, 10=13, 11=14, 12=2, 13=3, 14=1}'
'PRODUCT INPUT ATOM INDEX<->AAM ID'
'{1=11, 2=10, 3=9, 4=5, 5=4, 6=3, 7=2, 8=1, 9=7, 10=8, 11=6, 12=12, 13=13, 14=14}'
'
'
```

SECTION 2 Identifying conserved metabolic moieties

A conserved moiety is a group of atoms within molecules connected by reactions, that follow identical paths through a metabolic network and therefore, its amount remains constant (Figure 5). Representative examples from energy metabolism include the AMP and NAD moieties. With the set of atom mappings for a metabolic network the set of linearly independent conserved moieties for the metabolic network can be identified, each of which corresponds to a particular identifiable molecular substructure⁵.

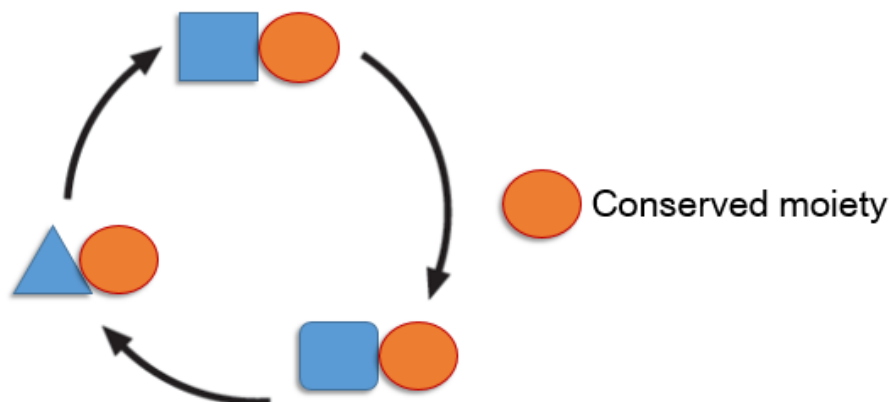


Figure 5: A graphical representation of a conserved moiety

In this section, we will identify conserved moieties in a subnetwork of the DAS network (Figure 2) by graph theoretical analysis of its atom transition network. The method is described in ⁵. This section consists of two parts:

Part 1 covers basic usage of the code.

Part 2 covers decomposition of a composite moiety resulting from variable atom mappings between the recurring metabolite pair O_2 and H_2O .

Part 1: Identify conserved moieties in DAS

Step 1: Generate an atom transition network for DAS based on atom mappings for internal (mass and charge balanced) reactions.

The atom transition network is generated based on the reconstructed DAS network (`model`) and atom mappings for internal reactions, obtained in the previous section and predicted with the RDT algorithm ³.

```
if ~isChemaxonInstalled
    copyfile([CBTDIR filesep 'tutorials' filesep 'atomicallyResolveReconstruction' filesep ...
            'data' filesep 'atomMapped'],[outputDir filesep 'atomMapped'])
end
atomMappedDir = [outputDir filesep 'atomMapped'];
ATN = buildAtomTransitionNetwork(model, atomMappedDir);
```

Atom mappings found for 4 model reactions.
Generating atom transition network for reactions with atom mappings.

The output variable (`ATN`) is a Matlab structure with several fields. `ATN.A` is the incidence matrix of the directed graph representing the atom transition network. Each row represents a particular atom in one of the 11 DAS metabolites. `ATN.mets` indicates which metabolite in DAS each atom belongs to. To find rows of `ATN.A` corresponding to atoms in CO_2 , run:

```
ico2 = find(ismember(ATN.mets, 'co2[c]'))'
```

```
ico2 =  
      88      89      90
```

The order of atoms in `ATN.A` matches their order in MDL MOL files encoding metabolite structures (Figure 7), e.g., `ATN.A(90,:)` is the row corresponding to the second oxygen atom (number 3 in Figure 6).

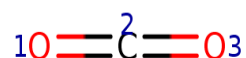


Figure 6: Rows for CO_2 atoms in `ATN.A` are ordered as shown.

`ATN.elements` contains the element symbols of atoms, e.g.,


```
ATN.elements{90}
```

```
ans = 0
```

Each column of `ATN.A` represents a particular atom transition in one of the four internal reactions in DAS. Reaction identifiers of atom transitions are given in `ATN.rxns`. To find all atom transitions that involve CO_2 atoms, run:

```
tco2 = find(any(ATN.A(ico2,:), 1))
```

```
tco2 =
```

```
75    76    77    95    96    97
```

```
ATN.rxns(tco2)'
```

```
ans =
```

```
'R3'    'R3'    'R3'    'R4'    'R4'    'R4'
```

i.e., three atom transitions in each of the reactions R3 and R4 involve atoms in CO_2 . To find atoms connected to CO_2 atoms via these atom transitions, run:

```
cco2 = find(any(ATN.A(:, tco2) < 0, 2));  
ATN.mets(cco2)'
```

```
ans =
```

```
'34dhphe[c]'    '34dhphe[c]'    '34dhphe[c]'    'for[c]'    'for[c]'    'for[c]'
```

i.e., CO_2 atoms are connected to atoms in the metabolites L-DOPA (VMH ID: 34dhphe) and formate (VMH ID: for).

Step 2: Identify conserved moieties in DAS by graph theoretical analysis of the atom transition network generated in Step 1.

```
tic  
[L,Lambda,moietyFormulas,moieties2mets,moieties2vectors,atoms2moieties] = ...  
    identifyConservedMoieties(model, ATN);  
t = toc;  
fprintf('Computation time: %.1e s\n\n', t); % Print computation time
```

```
Computation time: 2.0e-01 s
```

This function outputs the moiety matrix (`L`), the moiety supergraph (`Lambda`), the chemical formulas of moieties (`moietyFormulas`), and three vectors that map between the various inputs and outputs. The 10×5 moiety matrix `L` has a row for each metabolite and a column for each conserved moiety in DAS. Each column is a moiety vector, with elements corresponding to the number of instances of a conserved moiety in each metabolite. To find the number of instances of moiety 2 in L-DOPA, run

```
iLDOPA = find(ismember(model.mets, '34dhphe[c]'))
```

```
iLDOPA = 7
```

```
full(L(iLDOPA, 2))
```

```
ans = 1
```

i.e., L-DOPA contains one instance of moiety 2.

The 19×17 moiety supergraph (Λ) contains the graphs of all seven conserved moieties in DAS (Figure 7).

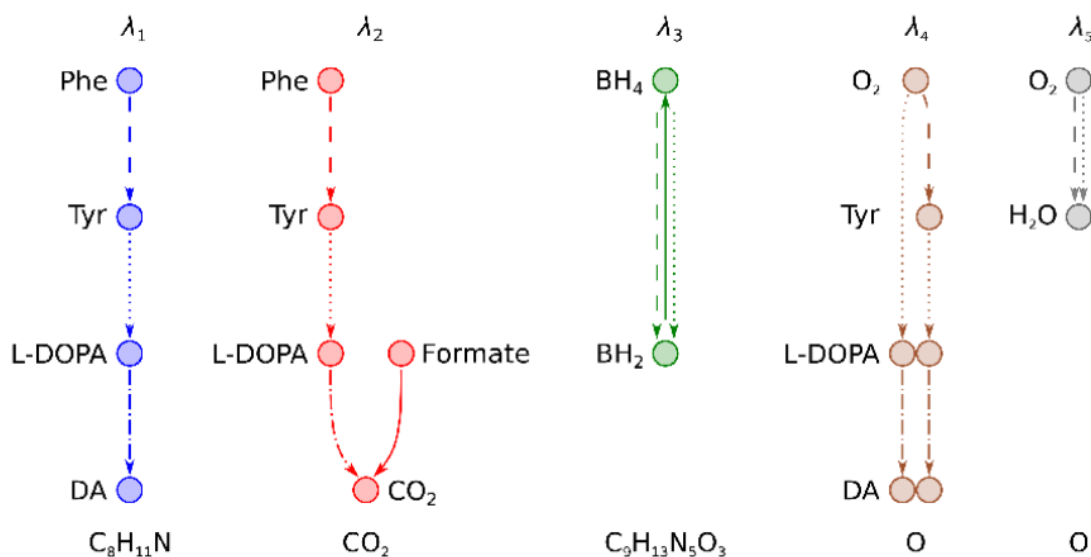


Figure 7: Graphs of the five conserved moieties in DAS. Each node represents an instance of a conserved moiety in a particular metabolite. Each directed edge represents conservation of a moiety between two metabolites. The chemical formula of each moiety is given below its graph.

Each row of Λ represents a single instance of a conserved moiety in a particular metabolite. The vector `moieties2vectors` maps between the rows of Λ and the columns of L . To obtain the incidence matrix of a particular moiety graph, e.g., λ_2 in Figure 7, run

```
i2 = find(moieties2vectors == 2);  
c2 = find(any(Lambda(i2, :)));  
lambda2 = full(Lambda(i2, c2))
```

```
lambda2 =
```

```
-1    0    0    0  
 1   -1    0    0  
 0    1   -1    0  
 0    0    1    1  
 0    0    0   -1
```

The vector `moieties2mets` maps the rows of Λ to metabolite indices in the DAS reconstruction (`model`). To find metabolites containing instances of moiety 2, run

```
m2 = moieties2mets(i2);  
mets2 = model.mets(m2)'
```

```
mets2 =
```

```
'phe_L[c]'    'tyr_L[c]'    '34dhphe[c]'    'co2[c]'    'for[c]'
```

The chemical formula of moiety 2 is given by,

```
moietyFormulas{2}
```

```
ans = C02
```

Finally, the vector `atoms2moieties` maps each atom in the atom transition network for DAS to a particular instance of a conserved moiety. To find atoms in L-DOPA that belong to moiety 2, run

```
find(ismember(atoms2moieties, i2) & ismember(ATN.mets, '34dhphe[c]'))'
```

```
ans =
```

```
74    75    76
```

Step 3: Classify moieties

```
types = classifyMoieties(L, model.S)
```

```
types =
```

```
'Transitive'  
'Transitive'  
'Internal'  
'Transitive'  
'Transitive'
```

The internal moiety (λ_3 in Figure 3) is conserved in both the open and closed DAS network, whereas the transitive and integrative moieties are only conserved in the closed network⁶.

Part 2: Effects of variable atom mappings between recurring metabolite pairs

Here, we will again identify conserved moieties in DAS but with a slightly different set of atom mappings (Figure 8). The different atom mappings gives rise to a different atom transition network with a different set of conserved moieties. In particular, it contains a single composite moiety, λ_8 in Figure 5, in place of the two moieties λ_4 and λ_5 in Figure 3. The composite moiety is the result of variable atom mappings between the recurring metabolite pair O₂ and H₂O in reactions R1 and R2.

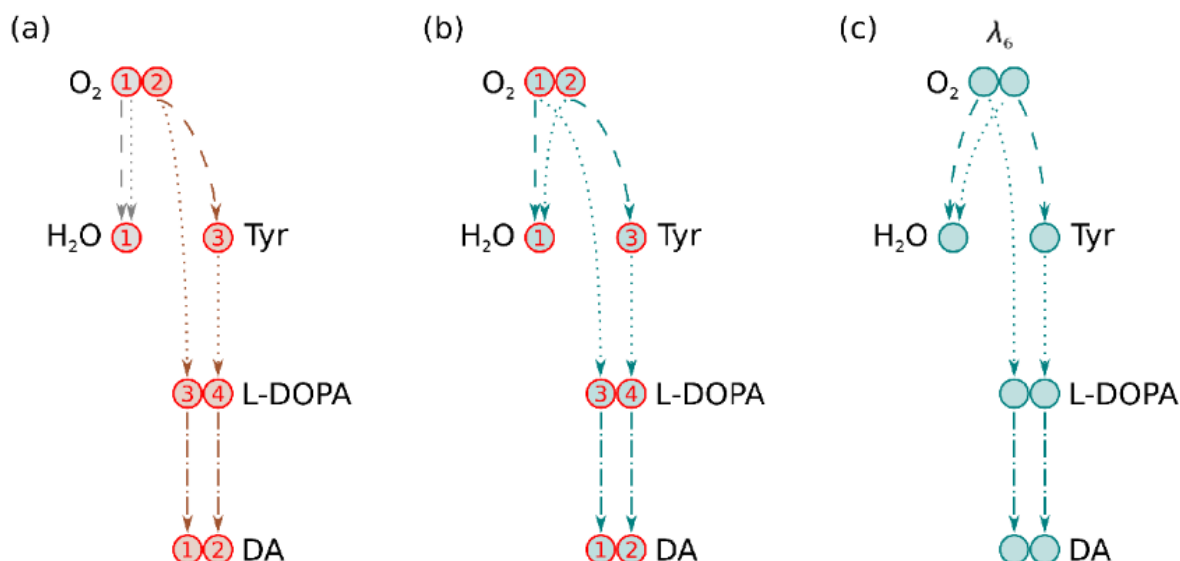


Figure 8: (a) Oxygen atom transitions used in Part 1. Oxygen atom 1 in O_2 maps to the oxygen atom in H_2O in both R1 and R2. These atom transitions contain two separate moieties, with two disconnected moiety graphs (λ_4 and λ_5 in Figure 7), and two linearly independent moiety vectors ($L(:,4)$ and $L(:,5)$). (b) Oxygen atom transitions used in Part 2. A different oxygen atom maps from O_2 to H_2O in R1 than in R2. These atom transitions contain only one composite moiety. (c) The composite moiety graph arising from the oxygen atom transitions in (b).

Step 1: Identify conserved moieties with the alternative set of atom mappings.

```
% Create an alternative MDL RXN file
R2rxn = regexp(fileread([outputDir filesep 'atomMapped' filesep 'R2.rxn'])), '\n', 'split');
R2rxn{2} = 'alternativeR2';
R2rxn{135}(62:63) = '18';
R2rxn{151}(62:63) = '19';
fid2 = fopen([outputDir filesep 'atomMapped' filesep 'alternativeR2.rxn'], 'w');
fprintf(fid2, '%s\n', R2rxn{:});
fclose(fid2);
```

```
% Create an alternative DAS model
alternativeModel = model;
alternativeModel.rxns{2} = 'alternativeR2';
```

```
% Identify conserved moieties
ATN = buildAtomTransitionNetwork(alternativeModel, atomMappedDir);
```

Atom mappings found for 4 model reactions.
Generating atom transition network for reactions with atom mappings.

```
[L,Lambda,moietyFormulas,moieties2mets,moieties2vectors,atoms2moieties] = ...
    identifyConservedMoieties(alternativeModel, ATN);
```

Step 2: Decompose the composite moiety vector

First, extract the internal stoichiometric matrix for DAS, by running:

```
rbool = ismember(alternativeModel.rxns, ATN.rxns);
mbool = any(alternativeModel.S(:,rbool), 2);
```

```
N = alternativeModel.S(mbool, rbool);
```

To decompose the moiety matrix computed in Step 1, run:

```
changeCobraSolver('gurobi6', 'milp');
```

```
> Gurobi interface added to MATLAB path.
```

```
D = decomposeMoietyVectors(L, N);
```

Note that you can use any Mixed Integer Linear Programme (MILP) solver that is supported by the COBRA toolbox. The decomposed moiety matrix D is identical to the original moiety matrix computed in Part 1. Moiety vectors D(:,4) and D(:,5) are the linearly independent components of the composite moiety vector L(:,4) above.

```
full(D(:,[4 5]))'
```

```
ans =
```

0	0	1	0	0	1	0	0	0	0
0	0	1	1	0	0	2	2	0	0

One disadvantage of decomposing moiety vectors is that it is difficult to keep track of which atoms belong to the decomposed moieties. We can, however, estimate the chemical formulas of the decomposed moieties using the elemental matrix for DAS. The elemental matrix is a numerical representation of the chemical formulas of metabolites in DAS.

```
[E,elements] = constructElementalMatrix(alternativeModel.metFormulas,...  
    alternativeModel.metCharges);  
decomposedMoietyFormulas = estimateMoietyFormulas(D, E, elements);  
decomposedMoietyFormulas([4 5])'
```

```
ans =
```

```
'H0'    'O'
```

i.e., each decomposed moiety contains an oxygen atom.

References

1. Haraldsdóttir, H.S., Thiele, I., Fleming, R.M. Comparative evaluation of open source software for mapping between metabolite identifiers in metabolic network reconstructions: application to Recon 2. *J. Cheminform* 6(1), 2 (2014).
2. Elizabeth Brunk, et al. Recon 3D: A Three-Dimensional View of Human Metabolism and Disease. Submitted
3. Rahman, S.A., et al. Reaction Decoder Tool (RDT): extracting features from chemical reactions. *Bioinformatics* 32(13), 2065–2066 (2016).
4. Preciat et al. Comparative evaluation of atom mapping algorithms for balanced metabolic reactions: application to Recon 3D. *J Cheminform*, 9: 39 (2017).
5. Hulda S. Haraldsdóttir and Ronan M. T. Fleming. Identification of conserved moieties in metabolic networks by graph theoretical analysis of atom transition networks. *PLOS Comput. Biol*, 12(11) (2016).

6. Iman Famili and B. Ø. Palsson. The convex basis of the left null space of the stoichiometric matrix leads to the definition of metabolically meaningful pools. *#Biophys. J*, 85(1):16–26 (2003).