Sparse Linear Optimisation

Author: Ronan Fleming, Hoal Minh Le, Systems Biochemistry Group, University of Luxembourg.

Reviewer: Stefania Magnusdottir, Molecular Systems Physiology Group, University of Luxembourg.

In this satural, we will show how to use the sparse LP solver. This solver aims to solve the following optimisation problem $\min_i |x_i|$,

min. $\{x\}_0$ $xx = A_0x = B_0$ $A_0x = B_0$

It has been proved that zero-norm is a non-convex function and the minimization of zero-norm is a NP-hard problem. Non-convex approximations of zero-norm extensively developed. For a complete study of non-convex approximations of zero-norm, the reader is referred to Le Thie et al. (2016) ¹.

The method is described in Le Thie et al. (\$016). The sparse LP solver contains one convex (one-norm) and 6 non-convex approximation of zero-norms.

• Capped-L1 norm.

Logarithmic function
 SCAD (Smoothly Clipped Atleo
 p.nom with pub

p norm with Output
 The hatolid consist of two parts. Plut 1 shows a basic usage of the solver, in part 2 provides an application of the code for finding the minimal set of reactions.

subject to a LP objective. Ready-made scripts are provided for both parts. EQUIPMENT SETUP

Initialize the COBRA Toolbox.

If necessary, initialize The Cobra Toolbox using the Links Cobraction Sans function

nitCobraToolbox

COBRA model.

In this statist, the model used is the generic reconstruction of human metabolism, the Recon 256⁴, which is provided in the COBRA Toolbox. The Recon 2.06 model can also select your own model to work with. Settine proceeding with the

simulations, the path for the model needs to be set up:

| glass| CRITOR
| modelFirstance = "broad_vect.or";
| modelFirstance = "broad_vect.or";
| modelFirstance = "broad_vect.or";
| modelFirstance = critical ribustendates| beloker loade| Filebance| values up the filebance for the distributed Models.

modelFileHzme=[modelDirectory filesep modelFileHzme]; when the full path Necessary to bookle readCMHsodel(modelFileHzme);

NOTE: The following text, code, and results are shown for the Recon 2.04 model: PROCEDURE:

Example of using sparseLP solver on randomly generated data

tonly generates a matrix $A \subseteq \mathbb{R}^{n \times n}$ and a vector $A \subseteq \mathbb{R}^n$. The right hand side vector $b = A \cdot b$, these are these optional inputs for the method $b = a \cdot b$.

The two first maximum number of terrations (inhibituheration) and threshold (epolon) are atopping criterion conditions, that is the parameter of zero-norm approximation. The greater the value of three, the better the approximation of the zero-norm, However, the greater the value of these, the more local solutions the problem has. If the value of these is not right entire the solution will use a default value and opposite a gradually.

parame.chimacteration = 180; % topping criteria parame.cptice = 18-6; % topping criteria parame.theth = 2; % parameter of im approximation

Califie solve with a chosen approximation
ealstide = sparseEP(-cappells',coestraint,parase);

or with default parameter

```
Finding the minimal set of reactions subject to a LP objective
Set the scienance to distinguish between zero and non-zero flux, based on the numerical tolerance of the currently installed optimisation solver
feacTol = getCobratolyerParamo("LP", "feacTol");
Select the biomass reaction to optimise
model.biomacchool-strome(model_rwss.'biomacc reaction');
We will firstly find the optimal value subject to a LP objective
 [c.5.b.lb.ub.comes] = deal(model_c.model_6.model_b.model_lb.model_ub.model_comes);
vFBR = LPsolution, full:
We will now find the minimum number of reactions needed to achieve the same may objective found previously. Then one will add one more
constraint.A = [6 ; c'];
constraint.b = [b ; c'euFBA];
constraint_csense = [csense; "1"];
Call the sparseLP solver to solve the problem
Now we call the sparse linear step function approximations.
bestResult = 0;
 for intrinength(approximations)
```

forietf('www.c',exzfol,' active reactions in the sparseFBA colution with ', char(approximations(1)))

if section(1) notes is section(1) in section

Apporte number of action stactions in the most space has vaccor

(prized("von", parighet(dest))-destable); intime reactions in the best space flow believe analysis solution.")

Whan I have nightle a numberal bloom with the adulton

The nightle analysis and the solution of the control of the

If feasifron-feachil
fprintf()print()feasifron(, ' feachily error.')
warming('muserical icose with the sparmerP miletime')
end

_

REFERENCES
[1] Le Thi, H.A., Pham Dinh, T., Le, H.M., and Vo, X.T. (bithly, OC approximation approaches for sparse optimization. European Journal of Operational Research

[2] Triefe, I., Swainston, N., Fleming, R.M., Hoppe, A., Sahoo, S., Aurich, M.K., Haraldsdottir, H., Mo, M.L., Rolfsson, O., Stobbe, M.D., et al. (2015). A community-