

张颢 (灏)

清华电子系 Rohm 11-105.

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Prerequisite:

Calculus. (Working knowledge)

Linear Algebra.

Probability. Linear Systems

Textbook and Reference

陆大经 张颢: 随机过程及应用 (1986) (2012)

A. Papoulis: Probability, Random Variables and Fourth Edition Stochastic Processes. "Cited Classic"

S. Ross: Stochastic Processes. second Edition

Homework and Exam.

100. = 10 + 30 + 60

(Projects) (Final)

1 of 3 6 of 10

3 Problems per Week

Taste.

Open Book

Electronic Version



# Stochastic Processes. (Random).

$X$ : Random Variable.  $\Omega \rightarrow \mathbb{R}$ . deterministic.

Statistical Experiment  $\Rightarrow$  Sample Points.

$P: 2^\Omega \rightarrow \mathbb{R}_+$ . Random Variables  $\Leftarrow$  Sample Space  
Possibility.

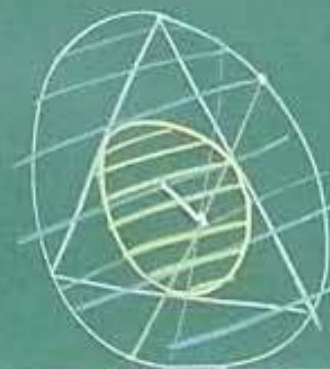
Distribution Functions.

$$F_X(x) = P(X \leq x) = P(X \in (-\infty, x]) \quad \forall p \in (0,1)$$

$$= P(\{\omega \in \Omega : X(\omega) \leq x\}) \quad \text{Bertrand Paradox.}$$

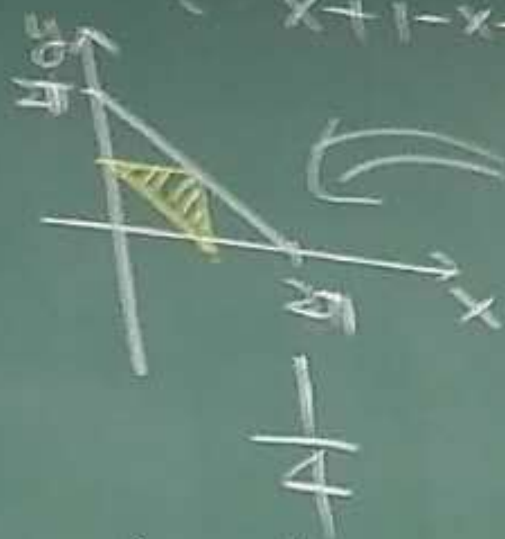


Equiprobable  
 $\frac{1}{2}$   $\frac{1}{3}$   $\frac{1}{4}$





$$\begin{cases} 0 \leq x \leq 1 \\ 0 \leq y \leq 1 \\ 0 \leq 1-x-y \leq 1 \end{cases}$$



$$\begin{cases} x+y \geq 1-x-y \\ y+1-x-y > x \\ x+1-x-y > y \end{cases}$$

$$\begin{cases} 0 \leq x \leq \pi \\ 0 \leq y \leq \pi \\ 0 \leq 2\pi - x - y \leq \pi \end{cases}$$



$$\begin{cases} 0 \leq x \leq 2\pi \\ 0 \leq y \leq 2\pi \\ 0 \leq 2\pi - x - y \leq 2\pi \end{cases}$$

first 6 winner,  $\frac{1}{2}, \frac{1}{2}$

$$5:3 = A:B$$

Pascal-Fermat Correspondence.

$\{ \underline{AAA}, \underline{BBB}, \underline{ABB}, \underline{BBA}, \underline{ABA}, \underline{BAB}, \underline{AAB}, \underline{BAA} \}$

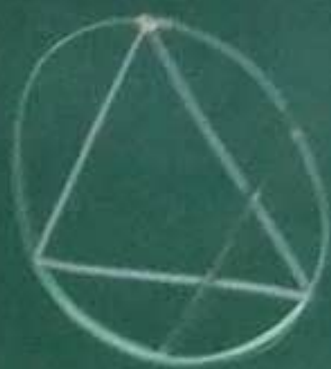
Fermat: 7:1.  $\{ BBB, A, BA, BBA \}$

$$P(A|B) = \frac{P(AB)}{P(B)}$$



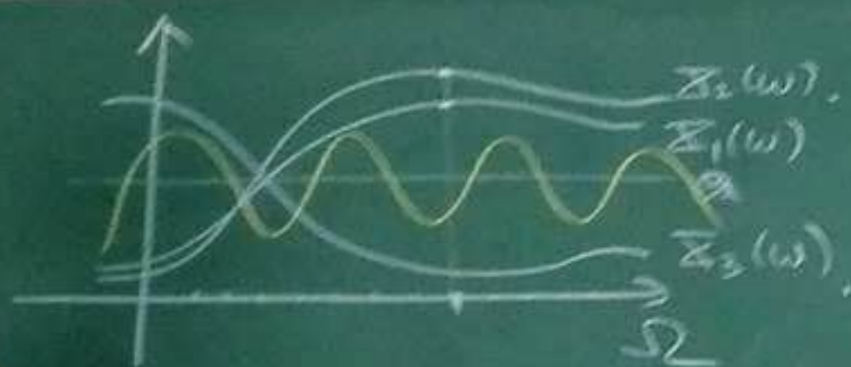
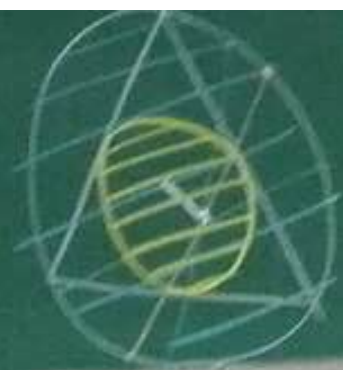
Multiple Random Variables,  $\mathcal{X}_1(\omega), \mathcal{X}_2(\omega), \dots, \mathcal{X}_n(\omega): \Omega \rightarrow \mathbb{R}$





Equiprobable

$$\frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{4}$$



$$X_3 = 2a - X_2$$

$$X_1, X_2, \dots, X_n, \dots, \Omega \rightarrow \mathbb{R}$$

Time      Relations

Independence  $X_1, X_2, \dots, X_n$  i.i.d.

- ① Correlation (Linear)    ② Markov Property    ③ Martingale