## A. 文章原理公式及完整实验结果

#### A.1 第 2.2 节的优化过程

变量 M 和 P 可以如下交替进行求解:

步骤 1: 优化 M 时, 固定 P, 将第 2.2 节 MDC 目标函数 (2) 转换为:

$$\min_{\mathbf{M}} \sum_{k=1}^{c} \sum_{i=1}^{n} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \right\|_{2}$$
(A.1)

引入辅助变量  $h_{ik} = (\|\mathbf{X}_{MSPE}^i\mathbf{P} - \mathbf{M}_K\mathbf{P}\|_2)^{-1}$ 来表示投影空间中  $\mathbf{X}_{MSPE}^i$  与  $\mathbf{M}_K$  之间的距离,因此上式可以表示为:

$$\min_{\mathbf{M}} \sum_{k=1}^{c} \sum_{i=1}^{n} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \right\|_{2} = \sum_{k=1}^{c} \sum_{i=1}^{n} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \right\|_{2}^{2} h_{ik}$$
(A.2)

计算公式 (A.2) 对  $M_{\iota}$  的偏导数,可得:

$$\frac{\partial \sum_{k=1}^{c} \sum_{i=1}^{n} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \right\|_{2}^{2} h_{ik}}{\partial \mathbf{M}_{k}}$$

$$= \sum_{i=1}^{n} 2(\mathbf{M}_{k} \mathbf{P} - \mathbf{X}_{MSPE}^{i} \mathbf{P}) \mathbf{P}^{\mathsf{T}} h_{ik}$$

$$= \sum_{i=1}^{n} 2(\mathbf{M}_{k} \mathbf{P} - \mathbf{X}_{MSPE}^{i} \mathbf{P}) \mathbf{P}^{T} h_{ik}$$
(A.3)

令公式 (A.3) 为 0,可得出  $M_{\nu}$ :

$$\mathbf{M}_{k} = \frac{\sum_{i=1}^{N} \mathbf{X}_{MSPE}^{i} h_{ik}}{\sum_{i=1}^{N} h_{ik}}$$
(A.4)

(A.5)

步骤 2: 优化 P 时, 固定 M, 将目标函数 (2) 转换为:

$$\min_{\mathbf{P}} \sum_{k=1}^{c} \sum_{i=1}^{n} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \right\|_{2} \\
+ \sigma \sum_{i,j} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{X}_{MSPE}^{j} \mathbf{P} \right\| \mathbf{W}_{ij} \\
+ \varsigma \left\| \mathbf{P} \right\|_{2,1} \\
s.t. \mathbf{P}^{T} \mathbf{P} = \mathbf{I}$$

公式(A.5)可以看作由三部分组成,所以可以将其先拆分成三部分,并逐一分析每个部分的数学含义进行求解:

①第一部分求解:在此通过引入辅助变量 $\tilde{\mathbf{H}}$ 和 $\hat{\mathbf{H}}$ ,可得:

$$\sum_{k=1}^{c} \sum_{i=1}^{n} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \right\|_{2}^{2}$$

$$= \sum_{k=1}^{c} \sum_{i=1}^{n} \left\| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \right\|_{2}^{2} h_{ik}$$

$$= \sum_{k=1}^{c} \sum_{i=1}^{n} \left( \mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{i}^{\mathsf{T}} h_{ik} - 2 \mathbf{M}_{k} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{i}^{\mathsf{T}} h_{ik} + \mathbf{M}_{k} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{M}_{k}^{\mathsf{T}} h_{ik} \right)$$

$$= \sum_{i=1}^{n} \mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{i}^{\mathsf{T}} \left( \sum_{k=1}^{c} h_{ik} \right) - \sum_{k=1}^{c} \sum_{i=1}^{n} 2 \mathbf{M}_{k} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{i}^{\mathsf{T}} h_{ik}$$

$$+ \sum_{k=1}^{c} \mathbf{M}_{k} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{M}_{k}^{\mathsf{T}} \left( \sum_{i=1}^{N} h_{ik} \right)$$

$$\Rightarrow Tr(\mathbf{X}_{MSPE} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{\tilde{H}}) - Tr(2 \mathbf{M} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{H}) + Tr(\mathbf{M} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{M}^{\mathsf{T}} \mathbf{\hat{H}})$$

$$\Rightarrow Tr(\mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{\tilde{H}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{P}) - Tr(2 \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{H} \mathbf{M} \mathbf{P}) + Tr(\mathbf{P}^{\mathsf{T}} \mathbf{M}^{\mathsf{T}} \mathbf{\hat{H}} \mathbf{M} \mathbf{P})$$
(A.6)

② 第 二 部 分 求 解 : 在 此 通 过 引 入 辅 助 变 量  $Q = [q_{ij}]_{n\times n}$  , 其 中

$$q_{ij} = \begin{cases} \frac{1}{2 \|\mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{X}_{MSPE}^{j} \mathbf{P}\|_{2}} & \|\mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{X}_{MSPE}^{j} \mathbf{P}\|_{2} \neq 0 \\ 0 & \|\mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{X}_{MSPE}^{j} \mathbf{P}\|_{2} = 0 \end{cases}, \quad q_{ij} \text{ 可以看作是 } \mathbf{W}_{ij} \text{ 增加了一个权重。}$$

 $\mathbf{X}_{MSPE}^{i}$  距离  $\mathbf{X}_{MSPE}^{i}$  越远则  $\mathbf{W}_{ij}$  越小,进一步降低了它们之间的相似性。如果  $\mathbf{X}_{MSPE}^{i}$  与  $\mathbf{X}_{MSPE}^{j}$  重合,则  $\mathbf{W}_{ii}$  是无效的。由此可得:

$$\mu \sum_{i,j} \| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{X}_{MSPE}^{j} \mathbf{P} \|_{2}^{2} \mathbf{W}_{ij} q_{ij}$$

$$= \mu \sum_{i,j} (2 \mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{i}^{\mathsf{T}} - 2 \mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{j}^{\mathsf{T}}) \mathbf{W}_{ij} q_{ij}$$

$$= 2 \mu \sum_{i,j} (\mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{i}^{\mathsf{T}} - \mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{j}^{\mathsf{T}}) \mathbf{W}_{ij} q_{ij}$$

$$= 2 \mu \sum_{i} \mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{i}^{\mathsf{T}} \sum_{j} \mathbf{W}_{ij} q_{ij} - 2 \sum_{i,j} \mathbf{X}_{MSPE}^{i} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{j}^{\mathsf{T}} \mathbf{W}_{ij} q_{ij}$$

$$= 2 \mu Tr(\mathbf{X}_{MSPE} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{R}) - 2 \mu Tr(\mathbf{X}_{MSPE} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{W})$$

$$= 2 \mu Tr(\mathbf{X}_{MSPE} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} (\mathbf{R} - \mathbf{W} \otimes \mathbf{Q}))$$

$$= 2 \mu Tr(\mathbf{X}_{MSPE} \mathbf{P} \mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L})$$

$$= 2 \mu Tr(\mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L})$$

$$= 2 \mu Tr(\mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{P})$$
(A.7)

其中 $\otimes$ 代表 **W** 和 **Q** 的哈达玛积 (Hadamard), **L** = **R** - **W**  $\otimes$  **Q** , **L** 是由 **W**  $\otimes$  **Q** 求出的拉普拉斯矩阵,由此可得:

$$\mathbf{R} = \begin{bmatrix} R_{11} & 0 & \cdots & 0 \\ 0 & R_{22} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & R_{NN} \end{bmatrix}, R_{ii} = \sum_{j} \mathbf{W}_{ij} q_{ij}$$
(A.8)

③第三部分求解:

$$\left\|\mathbf{P}\right\|_{2,1} = 2Tr(\mathbf{P}^{\mathsf{T}}\mathbf{D}\mathbf{P}) \tag{A.9}$$

其中D可表示为:

$$\mathbf{D} = \begin{bmatrix} D_{11} & 0 & \cdots & 0 \\ 0 & D_{22} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & D_{MM} \end{bmatrix}, D_{ii} = \frac{1}{2 \|\mathbf{P}\|_{2}}$$
(A.10)

④最后,整合以上三部分可得:

$$\min_{\mathbf{P}} \sum_{k=1}^{c} \sum_{i=1}^{n} \| \mathbf{X}_{MSPE} \mathbf{P} - \mathbf{M}_{k} \mathbf{P} \|_{2} + \sigma \sum_{i,j} \| \mathbf{X}_{MSPE}^{i} \mathbf{P} - \mathbf{X}_{MSPE}^{j} \mathbf{P} \| \mathbf{W}_{ij} + \varsigma \| \mathbf{P} \|_{2,1}$$

$$\Leftrightarrow \min_{\mathbf{P}} Tr(\mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{X}_{MSPE} \mathbf{P}) - Tr(2\mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{M} \mathbf{P})$$

$$+ Tr(\mathbf{P}^{\mathsf{T}} \mathbf{M}^{\mathsf{T}} \mathbf{M} \mathbf{P}) + 2\sigma Tr(\mathbf{P}^{\mathsf{T}} \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L} \mathbf{X}_{MSPE} \mathbf{P}) + 2\varsigma Tr(\mathbf{P}^{\mathsf{T}} \mathbf{A} \mathbf{P})$$

$$\Leftrightarrow \min_{\mathbf{P}} Tr(\mathbf{P}^{\mathsf{T}} ((\mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{X}_{MSPE} - 2\mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{M} + \mathbf{M}^{\mathsf{T}} \mathbf{M})$$

$$+ 2\sigma \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L} \mathbf{X}_{MSPE} + 2\varsigma \mathbf{A}) \mathbf{P}$$

$$\Leftrightarrow \min_{\mathbf{P}} Tr(\mathbf{P}^{\mathsf{T}} ((\mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{X}_{MSPE} - (\mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{M} + \mathbf{M}^{\mathsf{T}} \mathbf{X}_{MSPE}) + \mathbf{M}^{\mathsf{T}} \mathbf{M})$$

$$+ 2\sigma \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L} \mathbf{X}_{MSPE} + 2\varsigma \mathbf{A}) \mathbf{P}$$

$$\mathbf{B} = (\mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{X}_{MSPE} - (\mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{M} + \mathbf{M}^{\mathsf{T}} \mathbf{X}_{MSPE}) + \mathbf{M}^{\mathsf{T}} \mathbf{M})$$

$$+ 2\sigma \mathbf{X}_{MSPE}^{\mathsf{T}} \mathbf{L} \mathbf{X}_{MSPE} + 2\varsigma \mathbf{A})$$
(A.11)

显然, $\mathbf{B}$  是一个实对称矩阵。因此,可以根据 $\mathbf{B}$  的特征值分解结果求解 $\mathbf{P}$ ,且所得到的 $\mathbf{P}$  必然是正交的。 $\mathbf{P} \in R^{2d \times q}$  由特征向量组成,其对应的特征值是q 的非零最小值。q 代表投影空间中变量的个数。当获得最终优化后的变量 $\mathbf{M}$  和 $\mathbf{P}$  后,可根据下式求得第二层样本空间,即由保持降维式聚类模块 MDC 生成的样本空间  $\mathbf{X}_{MDC}$ :

$$\mathbf{X}_{MDC} = \mathbf{MP} \tag{A.12}$$

## A.2 第 2.3 节的优化过程

因此,在求解第 2.3 节 DSICM 目标函数(12)时,变量 $\Phi$ , Q和 $\Theta$ 可以如下交替进行求解:

步骤 1: 优化 $\Phi$ 时,固定 $\mathbb{Q}$ 和 $\Theta$ ,将公式(12)中的目标函数转换为:

$$\min_{\boldsymbol{\Phi}} \frac{\mathcal{G}}{n^{2}} \boldsymbol{\Phi}^{T} (\mathbf{K}_{MDC} \mathbf{Q} \mathbf{1} (\mathbf{K}_{MDC} \mathbf{Q})^{T} - \mathbf{K}_{MDC} \mathbf{Q} \mathbf{1} (\mathbf{K}_{MDC})^{T} 
- \mathbf{K}_{MSPE} \mathbf{1} \mathbf{Q}^{T} (\mathbf{K}_{MDC})^{T}) + \mathbf{K}_{MSPE} \mathbf{1} (\mathbf{K}_{MSPE})^{T} \boldsymbol{\Phi} 
+ \frac{1}{n^{2}} [Tr(\boldsymbol{\Phi}^{T} \mathbf{K}_{MDC} \mathbf{Q} \mathbf{D} (\boldsymbol{\Phi}^{T} \mathbf{K}_{MDC} \mathbf{Q})^{T}) 
+ Tr(\boldsymbol{\Phi}^{T} \mathbf{K}_{MSPE} \mathbf{D} (\boldsymbol{\Phi}^{T} \mathbf{K}_{MSPE})^{T}) 
- 2Tr(\boldsymbol{\Phi}^{T} \mathbf{K}_{MDC} \mathbf{Q} \mathbf{W} (\boldsymbol{\Phi}^{T} \mathbf{K}_{MSPE})^{T})] 
s.t. \boldsymbol{\Phi}^{T} \mathbf{K} \boldsymbol{\Phi} = \mathbf{I}$$
(A.13)

对此可以推导出第 j 次迭代列的解  $\Phi_j$  。通过设置令公式(A.13)对  $\Phi_{j(:,i)}$  的偏导数为零,得到  $\Phi_j$  中的第 i 列向量:

$$\frac{1}{n^{2}}Tr(\boldsymbol{\Phi}^{\mathsf{T}}\mathbf{K}_{MDC}\mathbf{Q}\mathbf{D}(\boldsymbol{\Phi}^{\mathsf{T}}\mathbf{K}_{MDC}\mathbf{Q})^{\mathsf{T}}) + \mathbf{K}_{MSPE}^{\mathsf{T}}\mathbf{D}(\mathbf{K}_{MSPE}^{\mathsf{T}})^{\mathsf{T}} 
- \mathbf{K}_{MDC}\mathbf{Q}\mathbf{W}(\mathbf{K}_{MSPE}^{\mathsf{T}})^{\mathsf{T}} - \mathbf{K}_{MSPE}^{\mathsf{T}}\mathbf{W}\mathbf{Q}^{\mathsf{T}}(\mathbf{K}_{MDC})^{\mathsf{T}})\boldsymbol{\Phi}_{j(:,i)} 
+ \frac{\partial}{n^{2}}(\mathbf{K}_{MDC}\mathbf{Q}\mathbf{1}\mathbf{Q}^{\mathsf{T}}(\mathbf{K}_{MDC})^{\mathsf{T}} - \mathbf{K}_{MDC}\mathbf{Q}\mathbf{1}(\mathbf{K}_{MSPE}^{\mathsf{T}})^{\mathsf{T}} 
- \mathbf{K}_{MSPE}^{\mathsf{T}}\mathbf{1}\mathbf{Q}^{\mathsf{T}}(\mathbf{K}_{MDC})^{\mathsf{T}} + \mathbf{K}_{MPSE}^{\mathsf{T}}\mathbf{1}(\mathbf{K}_{MPSE}^{\mathsf{T}})^{\mathsf{T}})\boldsymbol{\Phi}_{j(:,i)} 
= -\lambda \mathbf{K}\boldsymbol{\Phi}_{j(:,i)}$$
(A.14)

步骤 2: 优化 $\mathbf{Q}$ 时,固定 $\mathbf{\Phi}$ 和 $\mathbf{\Theta}$ ,将公式(13)中的目标函数转换为:

$$\min_{\mathbf{Q}} \frac{\mathcal{G}}{n^{2}} \mathbf{\Phi}^{T} (\mathbf{K}_{MDC} \mathbf{Q} \mathbf{1} (\mathbf{K}_{MDC} \mathbf{Q})^{\mathsf{T}} - \mathbf{K}_{MDC} \mathbf{Q} \mathbf{1} (\mathbf{K}_{MDC})^{\mathsf{T}} - \mathbf{K}_{MSPE} \mathbf{1} \mathbf{Q}^{\mathsf{T}} (\mathbf{K}_{MDC})^{\mathsf{T}})) \mathbf{\Phi} 
+ \frac{1}{n^{2}} (Tr(\mathbf{\Phi}^{\mathsf{T}} \mathbf{K}_{MDC} \mathbf{Q} \mathbf{D} (\mathbf{\Phi}^{\mathsf{T}} \mathbf{K}_{MDC} \mathbf{Q})^{\mathsf{T}}) - 2Tr(\mathbf{\Phi}^{\mathsf{T}} \mathbf{K}_{MDC} \mathbf{Q} \mathbf{W} (\mathbf{\Phi}^{\mathsf{T}} \mathbf{K}_{MSPE})^{\mathsf{T}})) 
+ Tr(\mathbf{E}^{\mathsf{T}} (\mathbf{Q} - \mathbf{\Theta})) + \frac{\rho \mathbf{1}}{2} (\|\mathbf{Q} - \mathbf{\Theta}\|_{F}^{2})$$
(A.15)

梯度下降算法(Gradient-Descent)是一种优化方法,通过计算目标函数的梯度并沿着负梯度方向更新参数,逐步调整参数以最小化目标函数值,从而找到最优解,这一过程反复迭代直至满足收敛条件。因此公式(A.15)可以使用梯度下降算法求解变量 $\mathbf{Q}$ 的封闭解,并经过(j+1)次迭代后, $\mathbf{Q}_{i+1}$ 可以转换为:

$$\mathbf{Q}_{j+1} = \mathbf{Q}_{j} - \frac{2}{n^{2}} ((\mathbf{K}_{MDC})^{\mathsf{T}} \mathbf{\Phi} \mathbf{\Phi}^{\mathsf{T}} \mathbf{K}_{MDC} \mathbf{Q} \mathbf{D}$$

$$- (\mathbf{K}_{MDC})^{\mathsf{T}} \mathbf{\Phi} \mathbf{\Phi}^{\mathsf{T}} (\mathbf{K}_{MSPE} \mathbf{W}) + \mathbf{E} + \rho \mathbf{1} (\mathbf{Q} - \mathbf{L})$$

$$+ \frac{2\partial}{n^{2}} [(\mathbf{K}_{MDC})^{\mathsf{T}} \mathbf{\Phi} \mathbf{\Phi}^{\mathsf{T}} \mathbf{K}_{MDC} \mathbf{Q} \mathbf{1} - (\mathbf{K}_{MDC})^{\mathsf{T}} \mathbf{\Phi} \mathbf{\Phi}^{\mathsf{T}} \mathbf{K}_{MSPE} \mathbf{1}]$$
(A.16)

步骤 3: 优化 $\Theta$ 时,固定 $\Phi$ 和Q,将公式(13)中的目标函数转换为:

$$\min_{\mathbf{\Theta}} \ \gamma \|\mathbf{\Theta}\|_{*} + Tr(\mathbf{E}^{\mathsf{T}}(\mathbf{Q} - \mathbf{\Theta})) + \frac{\alpha}{2} (\|\mathbf{Q} - \mathbf{\Theta}\|_{F}^{2})$$
(A.17)

在经过(j+1)次迭代之后, $\Theta_{j+1}$ 可以优化为:

$$\mathbf{\Theta}_{j+1} = \min_{\mathbf{\Theta}_{j}} \lambda_{1} Tr(\mathbf{\Theta}_{j}^{\mathsf{T}} \mathbf{\Theta}_{j})^{\frac{1}{2}} + Tr(\mathbf{E}_{1j}^{\mathsf{T}}(\mathbf{Q}_{j} - \mathbf{\Theta}_{j})) + \frac{\alpha_{j}}{2} (\|\mathbf{Q}_{j} - \mathbf{\Theta}_{j}\|_{F}^{2})$$
(A.18)

奇异值阈值(Singular Value Thresholding,SVT)算子是一种矩阵降噪技术,通过保留矩阵的主要奇异值,将其余奇异值置零以减少噪声和冗余信息,从而实现数据压缩和去噪处理。因此公式(A.18)可使用 SVT 算子求解得到最终优化变量 $\Theta$ 。

当获得最优变量 $\Phi$ 时,通过 $\mathbf{X}_{MDC}$ '=[ $\Phi^{\mathsf{T}}\varphi(\mathbf{X}_{OP})^{\mathsf{T}}\varphi(\mathbf{X}_{MDC})$ ]<sup>T</sup>可得到与 MSPE 保持样本数据结构信息的局部和全局一致性后的一次聚类包络样本集,其中d'表示 DSICM 后的样本维数。DSICM 使算法能够在构造多层样本空间的情况下保持样本数据结构信息的局部和全局一致性,从而实现有效的样本转换。

# A.3 第 4.2.1 节 MSPE、MDC 和 DSICM 的有效性验证完整实验结果

表 A.1-表 A.4 分别对应本文算法各阶段的样本的质量在 ACC、F1、AUC、AP 的比较。 表 A.1 本文算法各阶段的样本的质量(ACC)

数据集	OF (%)	MSPE (%)	MDC (%)	DSICM (%)	DSJPE (%)
AD	$54.00\pm9.55$	$64.67 \pm 4.47$	$66.67 \pm 7.84$	72.67±10.38	75.58±9.59
LSVT	$80.48\pm6.39$	$94.29\pm3.98$	$95.24\pm4.45$	95.80±3.33	96.54±4.48
PD	$62.70\pm1.86$	$70.75\pm1.74$	$66.84 \pm 1.52$	$71.03\pm1.40$	74.14±4.18
Pendigits	$98.13 \pm 0.05$	$98.62 \pm 0.07$	$99.09\pm0.35$	$98.78 \pm 0.12$	99.27±0.26
Statlog	$86.13 \pm 0.53$	$88.65 \pm 0.75$	$85.86\pm0.69$	$86.02 \pm 0.75$	88.36±0.45
Vehicle	$80.35\pm1.31$	83.90±0.19	$83.40\pm0.77$	87.30±0.81	87.16±0.81
heart	$80.89 \pm 4.26$	$85.56\pm2.83$	$90.91\pm4.08$	$91.20\pm4.25$	92.44±3.37
Maxlittle	$85.54 \pm 4.01$	86.77±2.57	$88.27 \pm 3.86$	89.23±5.65	91.25±8.39
Urban	79.91±3.87	$90.67 \pm 2.65$	$88.27 \pm 2.36$	93.51±3.35	94.46±1.47
WDBC	95.66±1.52	97.57±1.38	$98.59 \pm 0.38$	98.99±1.09	99.18±0.72
Wisconsin	96.30±1.72	$97.18\pm1.48$	$97.89\pm0.79$	98.06±0.50	98.41±0.74
PID	$70.39 \pm 2.74$	$74.14 \pm 4.27$	80.08±2.16	$82.95 \pm 2.25$	83.63±2.99
LR	$85.84 \pm 0.16$	$89.65 \pm 0.21$	$87.92 \pm 0.30$	89.06±0.11	89.79±0.34
GSAD	$99.20\pm0.15$	99.45±0.09	96.67±1.04	$97.45 \pm 0.30$	96.05±0.60
HAR	98.25±0.32	98.72±0.07	98.36±0.27	98.35±0.15	99.10±0.26

#### 表 A.2 本文算法各阶段的样本的质量(F1)

数据集	OF (%)	MSPE (%)	MDC (%)	DSICM (%)	DSJPE (%)
AD	$50.24\pm8.44$	64.78±8.32	72.09±7.55	73.85±9.76	74.12±10.90
LSVT	$76.57 \pm 4.38$	$93.61\pm4.60$	$94.75 \pm 4.86$	$95.24 \pm 6.52$	95.77±5.62
PD	$60.12\pm1.65$	$70.62\pm1.73$	$66.89 \pm 1.52$	$70.94\pm2.46$	71.54±3.18
Pendigits	$97.74\pm0.13$	99.04±0.09	$97.95 \pm 0.05$	98.03±0.09	99.04±0.09
Statlog	$80.98\pm1.85$	85.60±1.07	$75.24\pm0.84$	$77.26 \pm 0.91$	$85.59\pm1.05$
Vehicle	$80.57 \pm 0.56$	$84.55 \pm 0.96$	$90.53 \pm 0.83$	90.83±1.47	$87.40\pm0.70$
heart	$79.95 \pm 4.23$	$86.14\pm2.63$	$90.43 \pm 2.92$	$90.86\pm3.72$	91.09±3.67
Maxlittle	$80.30\pm4.78$	$79.36\pm4.24$	$79.35 \pm 3.67$	$84.54\pm8.68$	87.15±5.87
Urban	$76.06\pm2.12$	$90.77 \pm 2.76$	$87.32\pm1.81$	9437±2.37	$92.13\pm3.67$
WDBC	95.23±1.33	97.63±1.52	$97.31 \pm 0.46$	$98.80\pm0.69$	98.85±1.47
Wisconsin	95.16±1.59	95.95±1.69	$97.69\pm0.84$	97.87±0.56	98.11±1.28
PID	$71.23\pm3.96$	$74.82\pm2.20$	$77.43 \pm 2.66$	74.66±3.16	75.98±1.90
LR	$85.83 \pm 0.19$	89.61±0.23	$87.87 \pm 0.32$	$89.01 \pm 0.05$	90.18±1.26
GSAD	99.16±0.15	99.43±0.10	96.55±0.99	$97.37 \pm 0.33$	96.17±0.47
HAR	98.35±0.29	98.79±0.08	98.46±0.25	98.42±0.14	99.20±0.22

#### 表 A.3 本文算法各阶段的样本的质量(AUC)

数据集	OF (%)	MSPE (%)	MDC (%)	DSICM (%)	DSJPE (%)
AD	58.04±3.75	73.90±7.25	70.00±9.39	$78.73 \pm 9.24$	81.83±8.51
LSVT	$79.02 \pm 7.72$	$94.83\pm3.15$	96.75±1.90	$93.30\pm9.26$	96.59±3.92
PD	$60.14\pm3.58$	$71.79\pm2.96$	$68.05\pm1.38$	$72.12\pm3.06$	72.16±5.66
Pendigits	$99.10\pm0.18$	99.52±0.06	$98.96 \pm 0.07$	$98.99 \pm 0.10$	$99.47 \pm 0.05$
Statlog	$90.36 \pm 0.75$	91.98±0.59	$87.61 \pm 0.65$	$88.77 \pm 0.71$	$91.29 \pm 0.60$
Vehicle	$87.29 \pm 0.68$	$89.62\pm1.24$	$90.53\pm2.20$	$92.52 \pm 0.42$	92.12±1.19
heart	$81.64 \pm 5.54$	$86.92\pm3.04$	91.81±3.49	$91.95 \pm 4.44$	92.08±2.67
Maxlittle	$93.34 \pm 0.94$	$92.89 \pm 0.89$	92.66±1.14	$83.34 \pm 2.46$	93.78±1.32
Urban	$89.48 \pm 1.00$	94.63±1.89	$92.94 \pm 0.56$	$95.45 \pm 0.85$	96.25±2.11
WDBC	$96.00\pm1.80$	98.77±1.16	$98.08 \pm 0.36$	$98.30 \pm 0.83$	98.61±1.13
Wisconsin	95.81±1.61	96.08±1.12	$97.62 \pm 1.05$	$97.29 \pm 1.00$	98.01±0.57
PID	$73.51 \pm 4.11$	$74.43\pm3.73$	$80.00\pm2.35$	$81.97 \pm 2.58$	82.21±2.49
LR	$92.59\pm0.09$	94.57±0.11	93.66±0.16	$94.25 \pm 0.05$	95.88±0.57
GSAD	$99.48 \pm 0.09$	99.65±0.07	$97.78 \pm 0.69$	$98.40\pm0.21$	97.66±0.33
HAR	98.99±0.18	99.27±0.05	99.06±0.15	99.04±0.09	99.51±0.14

表 A.4 本文算法各阶段的样本的质量(AP)

数据集	OF (%)	MSPE (%)	MDC (%)	DSICM (%)	DSJPE (%)
AD	$71.46 \pm 9.75$	$78.21 \pm 8.08$	$77.78 \pm 10.81$	$82.42\pm5.54$	84.38±8.77
LSVT	$78.08\pm5.49$	$93.60\pm5.58$	$97.56\pm2.71$	$96.78\pm4.42$	97.84±3.33
PD	$60.18\pm3.32$	$71.60\pm2.62$	66.39±1.93	$73.00\pm3.48$	73.76±3.35
Pendigits	$99.56 \pm 0.03$	$98.89 \pm 0.09$	$99.58 \pm 0.02$	$99.59\pm0.04$	99.80±0.04
Statlog	$95.28\pm0.24$	$96.26\pm0.27$	$93.96\pm0.35$	$94.43 \pm 0.44$	96.47±0.37
Vehicle	89.93±1.01	$92.52\pm1.30$	$91.42 \pm 0.77$	94.12±1.17	$93.96\pm0.72$
heart	$77.70\pm7.72$	83.15±5.18	$89.84\pm5.37$	$90.28\pm5.39$	92.02±5.51
Maxlittle	$77.01\pm5.23$	$76.90\pm4.37$	$71.45\pm8.12$	$80.63\pm10.35$	81.57±4.15
Urban	$94.01\pm0.84$	$97.80\pm0.80$	96.61±0.31	98.48±1.04	$98.02\pm1.06$
WDBC	$94.15\pm2.05$	$96.54\pm2.46$	$95.94\pm0.66$	$97.43 \pm 0.64$	97.81±1.33
Wisconsin	$92.41\pm2.71$	$92.56\pm3.35$	$95.89\pm1.47$	$96.72 \pm 0.72$	98.10±2.49
PID	$74.08\pm5.54$	$75.31\pm5.34$	$78.05\pm3.05$	$75.40\pm3.60$	$80.85 \pm 2.74$
LR	$98.96 \pm 0.02$	$99.24 \pm 0.04$	99.10±0.01	99.15±0.01	99.38±0.09
GSAD	$99.59 \pm 0.05$	99.66±0.09	99.03±0.34	$99.09 \pm 0.07$	96.17±0.65
HAR	99.31±0.16	99.53±0.09	99.34±0.19	99.36±0.09	99.54±0.07

# A.5 第 4.2.2 节 MDC 和 DSICM 的有效性验证完整结果

表 A.5-表 A.8 分别对应 MDC 与 KM 在 ACC、F1、AUC、AP 上的比较。

表 4.5	MDC = KMZ	F ACC	上的比较结果
$A \times A \cdot J$		L ACC	

数据集	KM	MDC	KM&DSIM	DSICM	DSICM (ESAE)	DSICM (ESAE)
.,,.,	(%)	(%)	(%)	(%)	(%)	(%)
AD	75.33±7.30	66.67±7.84	66.00±5.96	72.67±10.38	67.33±10.11	76.00±4.35
LSVT	92.86±1.67	$95.24\pm4.45$	94.76±2.61	$95.80\pm3.33$	$96.07 \pm 9.85$	97.41±5.86
PD	66.21±1.70	$66.84\pm1.52$	$70.75\pm3.40$	$71.03\pm1.40$	$69.89\pm2.74$	74.60±4.56
Pendigits	$98.64 \pm 0.28$	99.09±0.35	98.83±1.46	$98.78 \pm 0.12$	$98.84 \pm 0.57$	99.50±0.82
Statlog	$85.59\pm0.76$	$85.86\pm0.69$	85.13±0.30	$86.02\pm0.75$	85.92±1.26	88.57±2.39
Vehicle	$79.93\pm2.93$	$83.40\pm0.77$	85.67±1.98	87.30±0.81	80.61±4.93	87.30±3.79
heart	$90.89 \pm 0.50$	90.91±4.08	$88.44 \pm 2.30$	$91.20\pm4.25$	90.96±5.28	92.67±3.20
Maxlittle	87.69±3.61	$88.27 \pm 3.86$	88.31±3.19	89.23±5.65	$88.08\pm5.57$	94.07±2.67
Urban	$72.62\pm2.99$	$88.27 \pm 2.36$	76.49±1.90	93.51±3.35	82.31±1.78	94.02±0.46
WDBC	$97.99\pm0.24$	$98.59\pm0.38$	$98.73 \pm 0.29$	98.99±1.09	98.10±3.70	99.15±2.91
Wisconsin	97.53±1.01	$97.89\pm0.79$	$97.89\pm0.85$	$98.06\pm0.50$	97.86±1.37	99.12±0.44
PID	$78.52\pm2.52$	$80.08\pm2.16$	81.72±3.13	82.95±2.25	$78.95 \pm 1.72$	$82.53\pm3.79$
LR	$87.73 \pm 0.33$	$87.92\pm0.30$	$89.83 \pm 0.15$	89.06±0.11	$88.09 \pm 2.62$	$90.07 \pm 4.46$
GSAD	$96.60\pm2.34$	96.67±1.04	$97.58 \pm 0.12$	97.45±0.30	$97.94 \pm 1.57$	$97.72 \pm 0.40$
HAR	98.35±0.27	98.36±0.27	$98.58 \pm 0.16$	98.35±0.15	$98.81 \pm 1.24$	99.39±0.15

#### 表 A.6 MDC与 KM在 F1上的比较结果

数据集	KM (%)	MDC (%)	KM&DSIM (%)	DSICM (%)	DSICM (ESAE) (%)	DSICM (ESAE) (%)
AD	53.70±8.28	72.09±7.55	70.01±6.01	73.85±9.76	75.00±11.64	74.59±7.40
LSVT	$92.50\pm5.34$	94.75±4.86	94.19±2.92	95.24±6.52	92.18±5.96	$94.73 \pm 4.27$
PD	62.62±1.62	66.89±1.52	$70.79 \pm 3.44$	$70.94\pm2.46$	$70.81 \pm 3.64$	75.96±3.31
Pendigits	$98.62 \pm 0.28$	97.95±0.05	96.21±0.41	98.03±0.09	$98.99 \pm 1.47$	99.46±0.73
Statlog	81.49±0.99	$75.24\pm0.84$	$79.46 \pm 1.22$	$77.26 \pm 0.91$	$85.95\pm5.78$	86.81±1.58
Vehicle	81.51±0.73	90.53±0.83	$85.88 \pm 2.02$	90.83±1.47	$86.04\pm4.18$	91.54±2.59
heart	79.77±2.99	$90.43\pm2.92$	$88.54 \pm 2.43$	90.86±3.72	$91.80\pm2.70$	93.29±2.95
Maxlittle	$71.98\pm3.81$	79.35±3.67	$83.54\pm4.60$	$84.54 \pm 8.68$	87.54±3.67	91.58±2.33
Urban	$72.58\pm5.98$	$87.32\pm1.81$	$77.31\pm4.93$	9437±2.37	74.98±3.13	$75.58\pm4.98$
WDBC	95.94±1.68	97.31±0.46	98.65±0.31	98.80±0.69	99.32±0.47	96.69±1.73

表 A.6 MDC 与 KM 在 F1 上的比较结果(续)

数据集	KM (%)	MDC (%)	KM&DSIM (%)	DSICM (%)	DSICM (ESAE) (%)	DSICM (ESAE) (%)
Wisconsin	93.10±3.17	97.69±0.84	97.72±0.84	97.87±0.56	98.56±0.49	98.57±0.47
PID	$72.66\pm2.95$	$77.43 \pm 2.66$	$74.54\pm2.08$	$74.66 \pm 3.16$	83.17±3.02	$77.03\pm3.33$
LR	87.67±0.35	$87.87 \pm 0.32$	$89.91 \pm 0.20$	$89.01 \pm 0.05$	84.32±6.69	89.77±1.33
GSAD	96.42±2.49	96.55±0.99	$97.49\pm0.10$	$97.37 \pm 0.33$	98.42±1.57	$95.24\pm2.58$
HAR	$98.46 \pm 0.25$	$98.46 \pm 0.25$	98.65±0.17	$98.42 \pm 0.14$	94.25±1.70	98.98±0.57

## 表 A.7 MDC与KM在AUC上的比较结果

	KM	MDC	KM&DSIM	DSICM	DSICM	DSICM
数据集	(%)	(%)	(%)	(%)	(ESAE)	(ESAE)
	(70)	(70)	(70)	(70)	(%)	(%)
AD	66.16±7.98	70.00±9.39	69.48±4.42	78.73±9.24	80.50±8.73	80.00±5.86
LSVT	$92.14\pm6.00$	96.75±1.90	$93.70\pm4.70$	$93.30\pm9.26$	91.43±4.96	$93.30\pm5.90$
PD	63.78±1.57	68.05±1.38	71.61±4.71	$72.12\pm3.06$	69.48±3.77	$75.50\pm3.69$
Pendigits	99.70±0.18	$98.96 \pm 0.07$	$99.40\pm2.64$	$98.99 \pm 0.10$	99.14±1.49	$99.48 \pm 0.69$
Statlog	90.12±0.67	87.61±0.65	87.20±1.12	$88.77 \pm 0.71$	$88.62 \pm 7.78$	$89.72 \pm 1.56$
Vehicle	88.04±1.32	90.53±2.20	90.98±1.31	$92.52\pm0.42$	91.14±3.89	92.99±1.29
heart	80.01±3.36	91.81±3.49	90.92±5.63	91.95±4.44	$91.70\pm2.58$	$92.94 \pm 2.81$
Maxlittle	81.09±17.95	92.66±1.14	$93.56 \pm 0.72$	$83.34 \pm 2.46$	93.72±2.11	$90.31 \pm 4.22$
Urban	73.31±2.97	92.94±0.56	84.21±1.77	$95.45 \pm 0.85$	$85.14 \pm 1.83$	98.53±1.37
WDBC	97.67±1.40	98.08±0.36	$98.27 \pm 0.01$	$98.30 \pm 0.83$	99.14±0.60	96.74±1.54
Wisconsin	96.92±1.87	97.62±1.05	97.88±1.37	$97.29 \pm 1.00$	$98.57 \pm 0.78$	$98.69 \pm 0.72$
PID	$67.35\pm10.02$	$80.00\pm2.35$	81.75±4.77	$81.97 \pm 2.58$	$83.23\pm2.70$	$76.92 \pm 3.33$
LR	93.57±0.17	93.66±0.16	94.66±0.08	$94.25 \pm 0.05$	$91.72 \pm 6.77$	$94.33\pm3.07$
GSAD	97.48±1.85	97.78±0.69	98.48±0.21	$98.40 \pm 0.21$	93.05±0.92	98.48±0.89
HAR	99.06±0.15	99.06±0.15	99.18±0.10	99.04±0.09	96.48±1.17	99.46±0.24

## 表 A.8 MDC与KM在AP上的比较结果

数据集	KM (%)	MDC (%)	KM&DSIM (%)	DSICM (%)	DSICM (ESAE) (%)	DSICM (ESAE) (%)
AD	70.18±10.17	77.78±10.81	75.52±1.48	82.42±5.54	81.39±11.74	79.75±2.74
LSVT	91.72±7.58	$97.56\pm2.71$	$96.24 \pm 2.65$	96.78±4.42	93.14±5.26	96.33±2.47
PD	61.82±2.17	66.39±1.93	$71.63 \pm 4.95$	$73.00\pm3.48$	69.27±6.33	76.40±3.14
Pendigits	$99.70\pm0.05$	$99.58 \pm 0.02$	$92.57 \pm 0.98$	$99.59 \pm 0.04$	93.23±1.17	99.65±0.17
Statlog	$95.55 \pm 0.32$	93.96±0.35	$95.27 \pm 0.55$	$94.43 \pm 0.44$	95.98±2.56	$95.72\pm0.21$
Vehicle	91.25±0.96	$91.42 \pm 0.77$	$92.90\pm0.66$	94.12±1.17	94.17±2.06	95.11±1.56
heart	81.00±4.36	$89.84 \pm 5.37$	87.66±4.77	90.28±5.39	$93.24\pm4.14$	93.93±1.76
Maxlittle	57.00±14.15	$71.45\pm8.12$	$78.74 \pm 9.12$	80.63±9.35	$88.46 \pm 4.82$	91.61±4.61
Urban	90.12±0.96	96.61±0.31	$92.09\pm0.73$	98.48±1.04	$94.28 \pm 0.64$	95.17±1.33
WDBC	$95.65\pm2.46$	95.94±0.66	96.92±1.31	97.43±0.64	99.20±0.56	96.96±1.81
Wisconsin	90.11±3.65	$95.89 \pm 1.47$	95.99±1.76	$96.72 \pm 0.72$	97.52±0.73	$97.38\pm0.93$
PID	70.31±6.04	$78.05 \pm 3.05$	80.11±4.06	$75.40\pm3.60$	82.72±4.60	$78.18 \pm 0.77$
LR	$99.09 \pm 0.03$	$99.10\pm0.01$	99.22±0.03	99.15±0.01	$94.52 \pm 2.83$	99.41±0.16
GSAD	$98.90 \pm 0.51$	$99.03 \pm 0.34$	$99.14 \pm 0.05$	$99.09\pm0.07$	$96.14 \pm 0.26$	96.34±0.46
HAR	$99.34 \pm 0.19$	99.34±0.19	$99.47 \pm 0.06$	99.36±0.09	$97.95 \pm 0.96$	99.47±0.37

# A.6 第 4.3 节算法比较的完整结果

表 A.9-表 A.12 分别对应不同 SAE 算法在 ACC、F1、AUC、AP 上的比较。

1X A.9	-1X A.12 ))		内 SAE 昇伝 長 A.9 不同 SA			AP	儿儿状。	
	SDSAE	SPSAE	ESGSAE	GSTAE	WGLAE	DSAE	SGAE	DSJPE-
数据集	(%)	(%)	-FF (%)	(%)	(%)	(%)	(%)	ESAE (%)
AD	55.58	57.78	67.33	71.11	52.67	56.67	56.11	76.67
ΑD	$\pm 4.36$	$\pm 4.27$	$\pm 2.49$	$\pm 8.16$	$\pm 5.48$	$\pm 5.27$	$\pm 1.07$	±8.16
LSVT	76.62	84.33	92.76	84.66	75.71	72.38	71.59	97.62
LSVI	$\pm 5.29$	$\pm 5.36$	$\pm 0.62$	$\pm 4.32$	$\pm 5.43$	$\pm 5.48$	$\pm 5.77$	$\pm 1.68$
PD	64.88	64.22	66.72	73.89	64.00	59.63	63.88	<b>75.98</b>
1D	$\pm 1.84$	$\pm 2.34$	$\pm 0.87$	$\pm 4.27$	$\pm 6.81$	$\pm 3.14$	$\pm 1.71$	±4.29
Pendigits	75.17	91.60	98.00	93.53	98.85	92.53	90.33	99.54
Tellargits	$\pm 1.88$	$\pm 0.57$	$\pm 0.12$	$\pm 0.77$	$\pm 1.24$	$\pm 1.22$	$\pm 0.30$	$\pm 0.11$
Statlog	98.60	85.87	87.28	85.42	99.83	85.31	74.13	89.42
Statiog	$\pm 0.34$	$\pm 0.86$	$\pm 0.12$	$\pm 0.38$	±0. 12	$\pm 0.50$	$\pm 0.24$	$\pm 0.81$
Vehicle	72.00	74.76	81.91	79.71	83.48	55.25	65.86	87.36
Venicie	$\pm 2.25$	$\pm 2.93$	$\pm 0.42$	$\pm 2.93$	$\pm 12.53$	$\pm 2.22$	$\pm 0.23$	±1.15
heart	94.58	88.90	84.67	82.56	80.22	82.67	69.67	94.67
Heart	$\pm 0.53$	$\pm 2.53$	±1.99	$\pm 3.55$	$\pm 9.21$	$\pm 1.27$	$\pm 3.60$	$\pm 2.98$
Maxlittle	83.65	91.93	92.00	92.15	89.54	81.23	88.97	98.75
Maxitue	$\pm 0.71$	$\pm 4.22$	$\pm 3.34$	$\pm 4.94$	$\pm 6.10$	$\pm 1.29$	$\pm 2.86$	±1.71
Urban	93.20	77.81	83.20	76.98	72.53	70.49	82.90	98.75
Orban	$\pm 1.17$	$\pm 1.17$	$\pm 1.01$	$\pm 0.73$	$\pm 8.63$	$\pm 2.75$	$\pm 0.15$	±1.71
WDBC	95.77	93.03	99.81	99.34	95.05	94.29	90.65	98.08
WDBC	$\pm 0.17$	$\pm 2.49$	$\pm 0.45$	$\pm 1.27$	$\pm 5.99$	$\pm 1.96$	$\pm 0.26$	$\pm 0.89$
Wisconsin	97.65	96.62	97.09	96.92	97.19	96.32	88.97	99.82
vv isconsin	$\pm 0.25$	$\pm 2.40$	$\pm 1.31$	$\pm 1.56$	$\pm 2.49$	$\pm 0.80$	$\pm 0.52$	$\pm 0.40$
PID	76.17	78.76	72.27	77.81	95.19	69.30	73.29	84.06
TID	$\pm 1.03$	$\pm 3.62$	$\pm 3.46$	$\pm 2.84$	$\pm 4.60$	$\pm 1.60$	$\pm 1.83$	$\pm 3.34$
LR	93.20	94.88	95.55	92.10	96.18	89.50	84.30	94.38
LIX	$\pm 1.17$	$\pm 0.12$	$\pm 0.78$	$\pm 0.99$	$\pm 1.55$	$\pm 2.08$	$\pm 0.05$	$\pm 0.37$
GSAD	95.77	98.89	99.07	97.42	98.78	91.17	87.86	96.71
USAD	$\pm 0.17$	$\pm 0.59$	$\pm 0.36$	$\pm 0.43$	$\pm 0.17$	$\pm 4.31$	$\pm 1.22$	$\pm 0.33$
HAD	97.36	98.13	97.81	98.22	99.0	97.88	97.03	99.51
HAR	±0.72	±0.45	±0.18	±1.10	2±0.11	±0.90	±4.18	$\pm 0.43$

			表 A.10 不同	SAE 算法的	比较 (F1)			
数据集	SDSAE	SPSAE	ESGSAE	GSTAE	WGLAE	DSAE	SGAE	DSJPE-
数1/6未	(%)	(%)	-FF (%)	(%)	(%)	(%)	(%)	ESAE (%)
AD	66.99	67.02	69.32	67.19	42.78	54.21	66.67	71.86
AD	$\pm 6.60$	$\pm 2.11$	$\pm 9.47$	$\pm 8.21$	$\pm 8.49$	$\pm 5.94$	$\pm 3.24$	$\pm 2.14$
LSVT	72.60	81.87	88.92	63.25	73.32	66.70	78.53	95.79
LSVI	$\pm 2.22$	$\pm 8.52$	$\pm 5.56$	$\pm 4.89$	$\pm 6.30$	$\pm 9.12$	$\pm 2.20$	$\pm 3.97$
PD	63.47	63.93	68.09	67.10	63.87	58.73	65.21	77.07
PD	$\pm 1.69$	$\pm 6.80$	$\pm 2.00$	$\pm 5.91$	$\pm 6.82$	$\pm 3.52$	$\pm 9.46$	$\pm 2.90$
Pendigits	73.20	91.51	99.36	91.68	98.84	92.56	91.51	99.55
Pendigns	$\pm 2.30$	$\pm 2.49$	$\pm 0.34$	$\pm 0.82$	$\pm 1.26$	$\pm 1.23$	$\pm 0.40$	$\pm 0.14$
Statlog	72.62	75.75	82.76	81.71	99.80	81.78	75.55	87.81
Statiog	$\pm 6.69$	$\pm 3.28$	$\pm 0.80$	±1.16	$\pm 0.13$	$\pm 0.43$	$\pm 4.69$	$\pm 1.04$
Vehicle	74.75	70.19	73.56	70.41	82.58	53.42	68.27	91.61
venicie	$\pm 5.12$	$\pm 4.23$	$\pm 8.64$	$\pm 3.33$	$\pm 13.96$	$\pm 1.33$	$\pm 6.24$	$\pm 3.79$
haant	79.44	81.24	84.53	82.54	78.95	81.90	57.16	93.61
heart	±1.48	±4.61	±2.04	±4.84	±10.43	±1.26	±4.00	±2.96

表 A.10 不同 SAE 算法的比较(F1)(续)

数据集	SDSAE	SPSAE	ESGSAE	GSTAE	WGLAE	DSAE	SGAE	DSJPE-
	(%)	(%)	-FF (%)	(%)	(%)	(%)	(%)	ESAE (%)
Maxlittle	85.13	87.02	89.09	95.95	83.06	70.88	84.29	92.43
	$\pm 1.64$	$\pm 5.10$	$\pm 4.87$	$\pm 5.04$	$\pm 8.45$	$\pm 2.88$	$\pm 2.52$	$\pm 3.25$
Urban	72.30	78.29	76.09	72.51	61.58	61.28	81.22	81.31
Orban	$\pm 0.51$	$\pm 2.92$	$\pm 5.72$	$\pm 1.37$	$\pm 9.33$	$\pm 4.77$	$\pm 4.89$	±1.99
WDBC	95.05	94.36	94.44	94.30	94.91	93.84	92.83	97.15
	$\pm 4.18$	$\pm 3.39$	$\pm 2.65$	$\pm 1.01$	$\pm 6.05$	$\pm 2.09$	$\pm 3.42$	$\pm 1.82$
<b>XX</b> '::	97.46	96.81	96.91	95.51	96.97	95.91	84.29	99.13
Wisconsin	$\pm 0.21$	$\pm 1.16$	$\pm 1.30$	$\pm 1.98$	$\pm 2.62$	$\pm 0.93$	$\pm 4.81$	$\pm 0.80$
PID	73.76	82.04	68.22	69.52	94.92	64.08	66.52	79.75
	$\pm 0.32$	$\pm 4.06$	$\pm 3.97$	$\pm 6.96$	$\pm 4.51$	$\pm 1.31$	$\pm 7.74$	±3.29
LR	95.59	96.28	96.34	83.27	92.29	89.74	87.41	90.18
	$\pm 3.49$	$\pm 1.76$	$\pm 3.05$	$\pm 2.27$	$\pm 2.79$	$\pm 4.32$	$\pm 0.01$	$\pm 1.26$
GSAD	97.83	99.39	99.37	95.35	93.76	91.36	89.50	96.73
	$\pm 1.96$	$\pm 0.53$	$\pm 0.16$	$\pm 2.04$	$\pm 0.94$	$\pm 1.65$	$\pm 0.69$	$\pm 0.18$
HAR	98.18	98.72	99.08	97.39	93.24	97.31	96.60	99.78
	±1.75	±0.37	±0.69	±0.37	±1.57	±3.37	±3.57	±0.16

## 表 A.11 不同 SAE 算法的比较(AUC)

数据集	SDSAE	SPSAE	ESGSAE	GSTAE	WGLAE	DSAE	SGAE	DSJPE-
	(%)	(%)	-FF (%)	(%)	(%)	(%)	(%)	ESAE (%)
AD	52.00	58.19	79.00	75.27	37.67	48.49	62.81	82.11
	$\pm 4.47$	$\pm 2.27$	$\pm 12.94$	$\pm 4.69$	$\pm 0.96$	$\pm 2.37$	$\pm 3.00$	±3.74
LSVT	66.07	77.50	61.43	75.50	76.00	67.86	66.43	96.62
	$\pm 3.09$	$\pm 12.28$	$\pm 19.50$	$\pm 5.02$	$\pm 7.83$	$\pm 9.45$	$\pm 4.76$	$\pm 2.67$
PD	60.73	63.93	67.87	71.72	64.13	60.06	63.35	<b>79.30</b>
PD	$\pm 2.72$	$\pm 6.80$	$\pm 2.00$	$\pm 3.83$	$\pm 7.09$	$\pm 2.86$	$\pm 2.61$	±4.94
Dandigita	68.64	93.29	99.09	81.42	89.41	86.08	94.35	99.75
Pendigits	$\pm 1.21$	$\pm 1.73$	$\pm 0.19$	$\pm 0.72$	$\pm 0.64$	$\pm 0.68$	$\pm 0.37$	$\pm 0.08$
Statlog	80.11	87.72	89.62	89.36	83.25	74.19	84.42	92.69
Statiog	$\pm 5.06$	$\pm 3.17$	$\pm 0.46$	$\pm 0.74$	$\pm 0.06$	$\pm 0.27$	$\pm 0.82$	$\pm 0.94$
Vehicle	67.51	70.96	82.48	74.80	66.68	54.36	60.19	93.11
Venicle	$\pm 3.54$	$\pm 1.24$	$\pm 5.59$	$\pm 2.15$	$\pm 6.48$	$\pm 1.40$	$\pm 3.21$	$\pm 0.48$
heart	84.90	87.16	84.25	85.25	80.24	81.46	60.19	95.68
Heart	$\pm 1.62$	$\pm 1.98$	$\pm 1.90$	$\pm 4.24$	$\pm 0.86$	$\pm 1.21$	$\pm 5.32$	±1.99
Maxlittle	84.12	86.52	87.54	77.19	85.24	68.50	80.77	95.68
Maximie	$\pm 6.31$	$\pm 8.29$	$\pm 7.49$	$\pm 10.06$	$\pm 9.85$	$\pm 2.98$	$\pm 3.79$	±1.99
Urban	67.32	75.69	85.17	90.15	72.68	70.05	80.03	90.61
Olban	$\pm 1.12$	$\pm 6.72$	$\pm 3.89$	$\pm 1.43$	$\pm 5.53$	$\pm 2.35$	$\pm 0.53$	$\pm 1.94$
WDBC	95.25	96.13	96.94	95.07	95.32	94.23	95.57	98.54
	$\pm 3.17$	$\pm 1.39$	$\pm 2.85$	$\pm 0.62$	$\pm 5.52$	$\pm 1.79$	$\pm 3.24$	$\pm 1.38$
Wisconsin	97.71	96.60	97.42	96.74	97.07	95.95	80.77	99.03
	$\pm 0.27$	$\pm 1.48$	$\pm 1.04$	$\pm 1.34$	$\pm 1.82$	$\pm 0.66$	$\pm 3.79$	$\pm 0.94$
PID	73.24	78.30	66.41	71.92	95.40	63.72	60.78	82.94
	$\pm 1.21$	$\pm 4.39$	$\pm 4.47$	$\pm 4.06$	$\pm 3.77$	$\pm 1.27$	$\pm 3.80$	$\pm 2.16$
LR	96.52	95.57	98.08	91.81	91.39	89.93	85.19	97.56
	$\pm 0.54$	$\pm 1.75$	$\pm 0.83$	$\pm 3.04$	$\pm 1.27$	$\pm 3.79$	$\pm 5.29$	$\pm 0.14$
GSAD	98.48	99.26	99.10	95.75	87.19	92.82	94.46	98.52
ODAD	$\pm 0.34$	$\pm 0.01$	$\pm 0.28$	$\pm 2.59$	$\pm 3.09$	$\pm 1.11$	$\pm 0.14$	$\pm 0.16$
HAR	98.23	98.42	98.97	97.17	87.11	94.63	95.15	99.67
ПАК	±1.38	±0.34	±0.94	±1.88	±4.40	±1.24	±0.58	±0.08

表 A.12 不同 SAE 算法的比较(AP)

次 A.12 小門 SAL 弄石川 U.C. ト DOAE - OCAE - DOUBLE								
数据集	SDSAE	SPSAE	ESGSAE	GSTAE	WGLAE	DSAE	SGAE	DSJPE-
	(%)	(%)	-FF (%)	(%)	(%)	(%)	(%)	ESAE (%)
AD	60.49	67.05	72.07	69.36	39.20	45.81	58.02	71.86
	$\pm 7.78$	$\pm 3.40$	$\pm 9.23$	$\pm 11.84$	$\pm 9.96$	$\pm 9.13$	$\pm 2.78$	$\pm 2.14$
LSVT	75.09	84.53	76.71	93.68	82.31	76.45	76.66	97.24
LSVI	$\pm 7.65$	$\pm 10.63$	$\pm 16.15$	$\pm 16.47$	$\pm 5.64$	$\pm 5.85$	$\pm 4.45$	$\pm 2.88$
PD	60.38	61.50	67.46	74.59	58.39	55.79	64.73	76.91
1 D	$\pm 1.70$	$\pm 5.68$	$\pm 2.03$	$\pm 3.94$	$\pm 4.12$	$\pm 3.60$	$\pm 3.30$	$\pm 4.06$
Pendigits	88.53	94.35	99.57	90.31	88.99	82.64	87.31	99.92
rendigits	$\pm 0.52$	$\pm 0.16$	$\pm 0.09$	$\pm 0.90$	$\pm 1.10$	$\pm 1.25$	$\pm 0.57$	$\pm 0.04$
Statlog	90.93	91.16	95.46	97.94	83.14	69.43	86.75	96.77
Statiog	$\pm 2.29$	$\pm 1.95$	$\pm 0.24$	$\pm 0.65$	$\pm 0.17$	$\pm 0.61$	$\pm 6.04$	$\pm 0.17$
Wahiala	76.13	79.74	87.11	74.46	64.01	42.22	69.43	94.81
Vehicle	$\pm 2.76$	$\pm 2.96$	$\pm 4.52$	$\pm 3.68$	$\pm 11.43$	$\pm 1.97$	$\pm 3.49$	$\pm 2.42$
haant	82.96	72.83	82.09	88.83	68.34	72.62	60.02	92.46
heart	$\pm 2.94$	$\pm 2.01$	$\pm 4.75$	$\pm 6.58$	$\pm 15.66$	$\pm 2.09$	$\pm 5.27$	$\pm 5.83$
Maxlittle	87.19	88.55	88.11	93.88	93.19	80.61	80.73	91.41
Maxiittie	$\pm 5.49$	$\pm 6.92$	$\pm 6.62$	$\pm 5.05$	$\pm 5.95$	$\pm 2.58$	$\pm 3.60$	±3.88
T I.d	89.13	92.67	94.62	96.18	63.70	60.09	82.57	95.96
Urban	$\pm 0.54$	$\pm 2.85$	±1.59	$\pm 6.65$	$\pm 9.53$	$\pm 1.98$	$\pm 5.36$	$\pm 0.43$
MDDG	96.51	96.38	97.50	96.75	90.59	87.39	98.04	97.91
WDBC	$\pm 0.92$	$\pm 2.18$	$\pm 5.50$	$\pm 2.30$	$\pm 8.59$	$\pm 4.62$	$\pm 1.09$	$\pm 1.05$
****	96.45	92.35	94.97	94.66	93.98	91.46	80.73	98.62
Wisconsin	$\pm 1.55$	$\pm 2.50$	$\pm 1.44$	$\pm 3.61$	±6.15	$\pm 2.67$	$\pm 3.60$	±1.63
DID	72.31	76.70	71.04	75.64	89.83	66.60	61.21	81.11
PID	$\pm 3.81$	$\pm 4.61$	$\pm 3.56$	$\pm 4.69$	$\pm 8.10$	$\pm 3.78$	$\pm 5.93$	$\pm 4.00$
T.D.	98.08	98.16	99.33	93.99	93.45	92.72	84.17	99.73
LR	$\pm 1.54$	$\pm 0.72$	±0.94	±4.61	±1.58	$\pm 3.48$	$\pm 0.46$	$\pm 0.22$
CCAD	99.22	99.62	99.30	95.85	90.39	96.68	90.35	97.10
GSAD	$\pm 0.32$	$\pm 0.26$	±0.39	$\pm 2.59$	±1.65	$\pm 0.21$	$\pm 0.23$	±0.31
HAD	98.70	98.55	99.35	99.34	85.90	96.36	94.22	99.78
HAR	$\pm 0.65$	±1.09	$\pm 0.08$	$\pm 1.07$	±1.26	$\pm 3.33$	$\pm 3.00$	$\pm 0.09$
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# A.7 第 4.4 节参数分析的完整结果

表 A.13 对应不同 MSPE 拼接数 υ 对算法性能影响的完整结果。

表 A.14 不同 MSPE 拼接数 υ 对算法性能影响(分类精度)

数据集	$\upsilon = 0$	$\upsilon = 1$	$\upsilon = 2$	v=3
AD	54.00±9.55	64.67±4.47	73.33±6.24	71.33±3.80
LSVT	$82.38\pm9.00$	96.19±3.61	95.71±5.16	95.71±3.10
PD	$62.70\pm1.86$	70.75±1.74	68.10±1.08	69.48±1.93
Pendigits	$98.13 \pm 0.05$	$98.62 \pm 0.07$	$99.20\pm0.24$	99.39±0.13
Statlog	86.13±0.53	$88.65 \pm 0.75$	$89.13 \pm 0.62$	89.73±0.81
Vehicle	$80.35\pm1.31$	83.90±0.19	$87.73\pm2.46$	87.87±3.95
heart	$80.89 \pm 4.26$	$85.56\pm2.83$	$84.67 \pm 3.46$	89.11±2.53
Maxlittle	$85.54 \pm 4.01$	$86.77 \pm 2.57$	$78.77 \pm 3.35$	84.00±4.30
Urban	$79.91 \pm 3.87$	$73.42\pm2.48$	$96.27 \pm 2.00$	$97.42 \pm 0.91$
WDBC	95.66±1.52	97.57±1.38	$99.58 \pm 0.24$	$100.0 \pm 0.00$
Wisconsin	96.30±1.72	$97.18\pm1.48$	98.15±0.85	98.06±0.39
PID	$70.39 \pm 2.74$	$74.14\pm4.27$	81.56±1.60	84.38±1.20
LR	$85.84 \pm 0.16$	89.65±0.21	$90.41 \pm 0.31$	$92.26 \pm 0.17$
GSAD	$99.20\pm0.15$	99.45±0.09	99.56±0.11	99.59±0.08
HAR	$98.25 \pm 0.32$	$98.72 \pm 0.07$	99.38±0.15	99.68±0.03