

Computer Architecture - Pipeline and Performance Problems

2. Pipeline Segment Timing Problem

Given: Segment times: $t_1 = 50$ ns, $t_2 = 30$ ns, $t_3 = 95$ ns, $t_4 = 45$ ns; Register delay $t_r = 5$ ns

Clock cycle time = $95 + 5 = 100$ ns

(i) Time to add 100 pairs = $(4 + 100 - 1) \times 100$ ns = 10,300 ns = 10.3 μ s

(ii) Split t_3 (95 ns) into two ≈ 47.5 ns parts. New max segment = 50 ns

New clock = $50 + 5 = 55$ ns, Stages = 5

Time = $(5 + 100 - 1) \times 55$ ns = 5,720 ns = 5.72 μ s

3. Morris Mano Pipeline Problem

Delays: Memory read = 40 ns, Multiply = 45 ns, Transfer to R3 = 5 ns, Add = 15 ns

(iii) Min clock cycle = $\max(40, 45, 5, 15) + \text{register delay} = 45 + 5 = 50$ ns

(iv) Non-pipeline time = $40 + 45 + 15 = 100$ ns

(v) Speedup for 10 tasks = $1000 / 650 \approx 1.54$

Speedup for 100 tasks = $10000 / 5150 \approx 1.94$

(vi) Max theoretical speedup = non-pipelined time / pipeline cycle = $100 / 50 = 2$

4. Floating Point Computation

250 billion operations, Speed = 100 MFLOPS = 10^8 ops/sec

Time = $2.5 \times 10^{11} / 10^8 = 2500$ seconds

5. Matrix Multiplication using Vector Processor

40x40 matrices

(i) Inner products = $40 \times 40 = 1600$

(ii) Multiply-add operations = $1600 \times 40 = 64,000$

6. Floating Point Pipeline Processors

4 processors with 40 ns cycle: 400 operations / 4 = 100 each $\rightarrow 100 \times 40$ ns = 4000 ns

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Single processor with 10 ns cycle: $400 \times 10 \text{ ns} = 4000 \text{ ns}$

-> Time is the same in both cases: 4000 ns