

# **CT Week 6 : List and Insertion sort**

# Lecture 1 : Lists of List

\* Week - 6

L.O.L. (List of Lists)

Para = [ sentence1, sentence2, ... ]  
sentence = [ word1, word2, ... ]  
Word = [ letter1, letter2, ... ]

e.g. [ [I, t, , was, monday, morning] ]  
[ [I, t], [w, a, s], [m, o, n, d, a, y], [m, o, r, n, i, n, g] ]

- All sentence start with capital letter.

for each SL in PL  
firstword = first(SL)  
firstchar = first(firstword)  
check firstchar capital.

- C, S, K

[CUSTOMERS]

CUSTOMER → [SHOPS]

[SHOPS] → [CATEGORIES]

- Paragraph - (List of sentences)
- sentence - (List of word)
- word - (List of letter)

(List of)

[It was Monday Morning]

[ [I, t], [w, a, s], [m, o, n, d, a, y], [m, o, r, n, i, n, g] ]

check all sentence start with capital letter?

for each SL in PL

firstword = first(SL)

firstchar = first(firstword)

## Lecture 2 : Insertion sort and ordered list

- Systematically building up an ordered list one element at a time by inserting it into the correct place so this is insertion.

# Ordered list ◦ List in Order — Ascending / descending  
Preserving

# Insertion sort ◦ Pick one card / Iter

- Compare it with rest of them which qualified once
- Then Insert at right position

Nested Iteration  
 $O(n^2)$

( 3 188 ) — (Make Increasing Order)  
( 2 193 )  
( 10 203 )  
( 11 220 )

QN : 1,2,3

# Lecture 3 : Pseudocode for insertion sort and ordered list

## Pseudocode: Sorting lists

### Arranging lists in order

- Sorting a list often makes further computations simple
  - Finding the top  $k$  values
  - Finding duplicates
  - Grouping by percentiles — top quarter, next quarter, ...
- Many clever algorithms exist, we look at a simple one
- Insertion sort
  - Create a second sorted list
  - Start with an empty list
  - Repeatedly insert next value from first list into correct position in the second list

### Inserting into a sorted list

- We have a list  $l$  arranged in ascending order
- We want to insert a new element  $x$  so that the list remains sorted
- Move items from  $l$  to a new list till we find the place to insert  $x$
- Insert  $x$  and copy the rest of  $l$
- Be careful to handle boundary conditions
  - $l$  is empty
  - $x$  is smaller than everything in  $l$
  - $x$  is larger than everything in  $l$

```
Procedure SortedListInsert(l,x)
  newList = []
  inserted = False
  foreach z in l {
    if (not(inserted)) {
      if (x < z) {
        newList = newList ++ [x]
        inserted = True
      }
    }
    newList = newList ++ [z]
  }
  if (not(inserted)) {
    newList = newList ++ [x]
  }
  return(newList)
End SortedListInsert
```

## Insertion sort

- Once we know how to insert, sorting is easy
- Create an empty list
- Insert each element from the original list into this second list
- Return the second list
- **Invariant** — second list is always sorted
  - `[]` is sorted, since it is empty
  - Inserting into a sorted list returns a sorted list

Procedure InsertionSort(l)

```
sortedList = []  
foreach z in l {  
    sortedList =  
        SortedListInsert(sortedList,z)  
}  
return(sortedList)
```

End InsertionSort

## Summary

- Sorting is an important pre-processing step
- Insertion sort is a natural sorting algorithm
- Repeatedly insert each item of the original list into a new sorted list
- We assumed that the list is sorted in ascending order
- Reverse the comparisons to sort in descending order

QN : 2,3

## Lecture 4 : Examples using sorted lists

L. 4.1 - (Ex using Sorted Lists)

① 2 student have same birthday

↳ Sort by birthday (sorting)

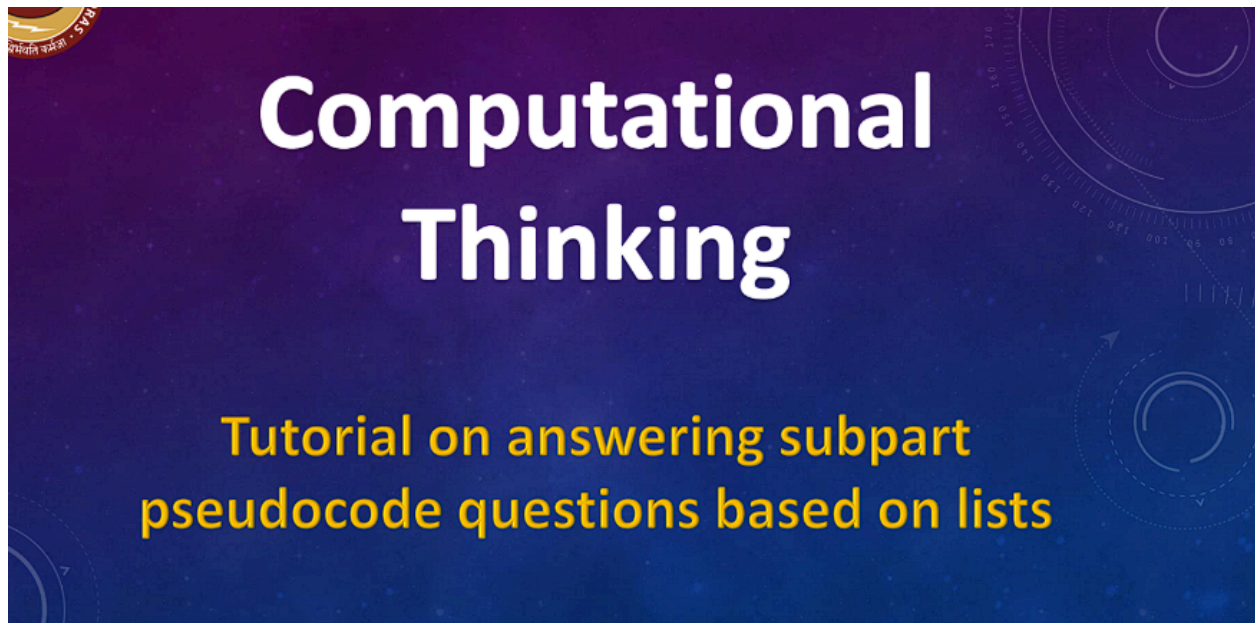
↳ for mark, City, or ~~or~~ many thing ✓

$[ (s_1, m_1), (s_2, m_2) ]$

(Sort one part of an Object)

Sorting is not only arranging in order, Grouping to some attributes to

## Tutorial 6.1 on answering subpart pseudocode questions based on lists



We have a new table containing information of 1000 books for a library. In the procedure given below, the parameter **books** is list sorted in an ascending order based on the number of pages. Each element in **books** corresponds to a book from the library and is represented by a list [SeqNo, Pages]. **X** is a row from the table.

```
1  Procedure Insert(X, books)
2      sBooks = [ ]
3      inserted = False
4      foreach Y in books {
5          if (X.Pages <= last(Y) and not(inserted)) {
6              sBooks = sBooks ++ [[X.SeqNo, X.Pages]]
7              inserted = True
8          }
9          sBooks = sBooks ++ [Y]
10     }
11     if (not(inserted)) {
12         sBooks = sBooks ++ [[X.SeqNo, X.Pages]]
13     }
14     return (sBooks)
15 End Procedure Insert
```

Q1: **Z** is some arbitrary value containing a book's details. Consider the following code:

```
someBooks = [ ]  
someBooks = Insert(Z, someBooks)
```

Which of the following lines in the procedure **Insert** will be executed during the above call? It is a Multiple Select Question (MSQ).

- ☐ Line 5
- ☐ Line 6
- ☐ Line 7
- ☐ Line 9
- ☒ Line 12
- ☐ No lines. An empty list cannot be passed as a parameter to the procedure.

```
1  Procedure Insert(X, books)  
2      sBooks = [ ]  
3      inserted = False  
4      foreach Y in books {  
5          if (X.Pages <= last(Y) and not(inserted)) {  
6              sBooks = sBooks ++ [[X.SeqNo, X.Pages]]  
7              inserted = True  
8          }  
9          sBooks = sBooks ++ [Y]  
10     }  
11     if (not(inserted)) {  
12         sBooks = sBooks ++ [[X.SeqNo, X.Pages]]  
13     }  
14     return (sBooks)  
15 End Procedure Insert
```

Q2: **Z** is a row in the table with the following data: **Z.SeqNo** is 12 and **Z.Pages** is 350.

What will be the contents of the list **someBooks** at the end of execution of the following code?

```
someBooks = [ [5, 220], [10, 350], [15, 350], [20, 400] ]  
someBooks = Insert(Z, someBooks)
```

- ☐ [ [5, 220], [10, 350], [15, 350], [20, 400] ]
- ☒ [ [5, 220], [12, 350], [10, 350], [15, 350], [20, 400] ]
- ☐ [ [5, 220], [10, 350], [12, 350], [15, 350], [20, 400] ]
- ☐ [ [5, 220], [10, 350], [15, 350], [12, 350], [20, 400] ]

```
1  Procedure Insert(X, books)  
2      sBooks = [ ]  
3      inserted = False  
4      foreach Y in books {  
5          if (X.Pages <= last(Y) and not(inserted)) {  
6              sBooks = sBooks ++ [[X.SeqNo, X.Pages]]  
7              inserted = True  
8          }  
9          sBooks = sBooks ++ [Y]  
10     }  
11     if (not(inserted)) {  
12         sBooks = sBooks ++ [[X.SeqNo, X.Pages]]  
13     }  
14     return (sBooks)  
15 End Procedure Insert
```

Q3: Execute the following pseudocode on the “Library” table. Which of the following statements are true after execution? It is a Multiple Select Question (MSQ).

```
books = [ ]
while(Table 1 has more rows) {
    Read top row X from Table 1
    books = Insert(X, books)
    Move X to Table 2
}
```

- ☒ first(books) corresponds to a book having the least number of pages in the library.
- ☐ first(books) corresponds to a book having the most number of pages in the library.
- ☒ last(last(books)) is the most number of pages among all the books in the library.
- ☐ first(last(books)) is the least number of pages among all the books in the library.
- ☐ last(first(books)) is the most number of pages among all the books in the library.
- ☒ last(first(books)) is the least number of pages among all the books in the library.

## Lecture 5 : Systematic process of hypothesis verification to find relation between Mathematics and Physics marks using lists

L. 6.50-

Maths Grade  $\rightarrow$  Physics Grade

Maths Grade: P, B, C, D

Physics Grade: A, B, C, D

① Math Mark high the Physics Mark is

② Top half (P, B)  $\rightarrow$  New Q

Math

P = [ ]

B = [ ]

C = [ ]

D = [ ]

1. Arrange in Ascending order.

2. Use Insertion Sort.

3. Put grade for Math and Physics

4. And then check common for same grade in each grade list

Hy

P = [ ]

B = [ ]

C = [ ]

D = [ ]

Refuse Confirm

## Lecture 6 : Pseudocode for systematic process of hypothesis verification to find relation between Mathematics and Physics marks using lists

Pseudocode: List example, correlating student performance

### Correlating marks in Maths and Physics

- We want to test the following hypothesis  
*Student who perform well in Mathematics perform at least as well in Physics*
- Assign grades {A,B,C,D} in both subjects
  - “Perform well in Maths” — grade B or above
  - “Perform at least as well in Physics” — Physics grade  $\geq$  Maths grade
- Algorithm
  - Assign grades in each subject
  - Construct lists of students with grades A and B in both subjects — four lists
  - Count students in A list for Maths who are also in A list for Physics
  - Count students in B list for Maths who are also in A list or B list for Physics
  - Use these counts to confirm or reject the hypothesis

## Assigning grades

- Assign grades {A,B,C,D} approximately at quartile boundaries
  - Top 25% get A, next 25% get B, next 25% get C, bottom 25% get D
- To calculate quartiles, extract marks as a list and sort the list
- Need to identify the students — each entry in the marks list is a pair [StudentId,Marks]
- Procedure to extract marks information as a list for a subject
- Get the marks lists for Maths and Physics

Procedure BuildMarksList(field)

```
marksList = []
while (Table 1 has more rows) {
  Read the first row X in Table 1
  marksList = marksList ++
    [[X.SeqNo, X.field]]
  Move X to Table 2
}
```

```
return(marksList)
```

End BuildMarksList

```
mathsList = BuildMarksList(Mathematics)
```

```
physicsList = BuildMarksList(Physics)
```

Navigation icons

- Use insertion sort for `mathList` and `physicsList`?
  - Entries are [id,marks]
  - To compare [i1,m1] and [i2,m2], only look at m1, m2
- Extracting values at the beginning and end of a list
  - `first(1)` and `last(1)`  
`first([1,2,3,4])` is 1,  
`last([1,2,3,4])` is 4
  - The remainder of the list is given by `rest(1)` and `init(1)`, respectively  
`rest([1,2,3,4])` is [2,3,4],  
`init([1,2,3,4])` is [1,2,3]
- Modify `SortedListInsert`

Procedure SortedListInsert(l,x)

```
newList = []
inserted = False

foreach z in l {
  if (not(inserted)) {
    if (last(x) < last(z)) {
      newList = newList ++ [x]
      inserted = True
    }
  }
  newList = newList ++ [z]
}

if (not(inserted)) {
  newList = newList ++ [x]
}

return(newList)
```

End SortedListInsert

Navigation icons

- `InsertionSort` uses updated `SortedListInsert`

```
sortedMathsList =
  InsertionSort(mathsList)

sortedPhysicsList =
  InsertionSort(physicsList)
```

- Assign grades to a sorted list by quartile
  - `length(l)` returns number of elements in `l`
  - Compute quartile boundaries based on class size

```

Procedure SimpleGradeAssignment(l)
  classSize = length(l)
  q4 = classSize/4
  q3 = classSize/2
  q2 = 3*classSize/4

```

- Assign grades to a sorted list by quartile
  - `length(l)` returns number of elements in `l`
  - Compute quartile boundaries based on class size
  - Initialize list for each grade

```

Procedure SimpleGradeAssignment(l)
  q4 = ..., q3 = ..., q2 = ...
  gradeA = []
  gradeB = []
  gradeC = []
  gradeD = []

```

- Assign grades to a sorted list by quartile
  - `length(l)` returns number of elements in `l`
  - Compute quartile boundaries based on class size
  - Initialize list for each grade
  - Assign grades based on the position in the list
- `SimpleGradeAssignment` returns a list containing four lists, for the four grades

```

Procedure SimpleGradeAssignment(l)
  q4 = ..., q3 = ..., q2 = ...
  gradeA = [], ..., gradeD = []
  position = 0
  foreach x in l {
    if (position > q2) {
      gradeA = gradeA ++ [first(x)]
    }
    if (position > q3 and position <= q2) {
      gradeB = gradeB ++ [first(x)]
    }
    if (position > q4 and position <= q3) {
      gradeC = gradeC ++ [first(x)]
    }
    if (position <= q4) {
      gradeD = gradeD ++ [first(x)]
    }
    position = position + 1
  }
  return([gradeA,gradeB,gradeC,gradeD])
End SimpleGradeAssignment

```

- Assign grades corresponding to Maths and Physics marks
- Unpack the four lists into four separate lists

```
mathsGrades =  
    SimpleGradeAssignment(sortedMathsList)  
physicsGrades =  
    SimpleGradeAssignment(sortedPhysicsList)  
  
mathsAGrades = first(mathsGrades)  
mathsBGrades = first(rest(mathsGrades))  
mathsCGrades = last(init(mathsGrades))  
mathsDGrades = last(mathsGrades)  
  
physicsAGrades = first(physicsGrades)  
physicsBGrades = first(rest(physicsGrades))  
physicsCGrades = last(init(physicsGrades))  
physicsDGrades = last(physicsGrades)
```

## Test the hypothesis

- Check how many students with A in Maths confirm the hypothesis
  - `exitloop` prematurely terminates a `foreach` loop

```
confirm = []
reject = []
foreach x in mathsAGrades {
  found = False
  foreach y in physicsAGrades {
    if (x == y) {
      confirm = confirm ++ [x]
      found = True
      exitloop
    }
  }
  if (not(found)) {
    reject = reject ++ [x]
  }
}
```

- Check how many students with A in Maths confirm the hypothesis
  - `exitloop` prematurely terminates a `foreach` loop
- Check how many students with B in Maths confirm the hypothesis
- Finally check `length(confirm)` against `length(confirm)+length(reject)` to decide if the hypothesis holds

```
foreach x in mathsBGrades {
  found = False
  foreach y in physicsAGrades {
    if (x == y) {
      confirm = confirm ++ [x]
      found = True, exitloop
    }
  }
  if (not(found)) {
    foreach y in physicsBGrades {
      if (x == y) {
        confirm = confirm ++ [x]
        found = True, exitloop
      }
    }
  }
  if (not(found)) {
    reject = reject ++ [x]
  }
}
```

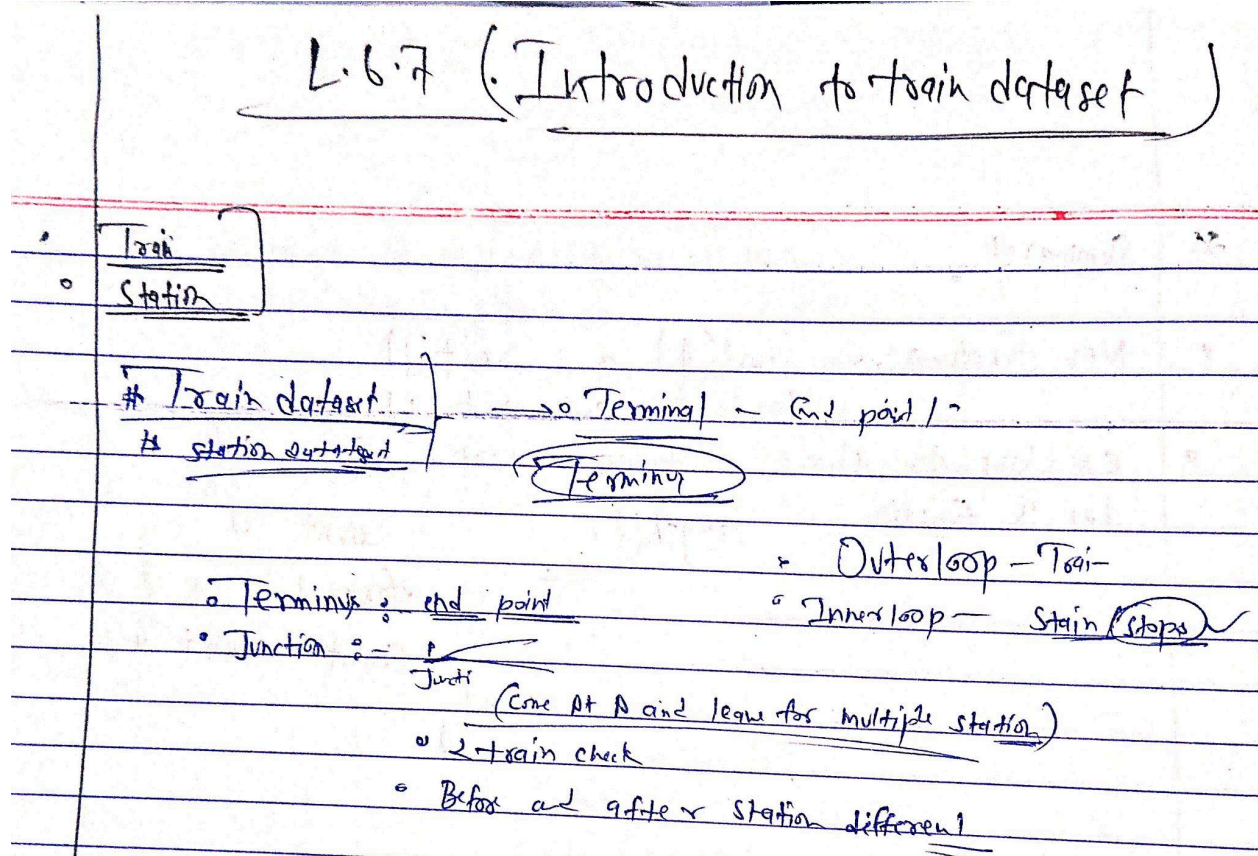
## Summary

- Sorting was used to identify quartiles for grade assignment
- Need to modify the comparison function based on the items in the list
- `length(l)` returns number of elements in `l`
- New functions to extract first and last items of a list
  - `first(l)` and `rest(l)`
  - `last(l)` and `init(l)`
- `exitloop` to abort a `foreach` loop

QN : 11

# Lecture 7 : Introduction to train dataset

Dataset in 1st week PDF



QN : 2,5,6

PA : 3,4,5,6,8,9,10

GA: 3,4,7