

i.e., extra info. is remained here & we can't recover it later.

### 3.) updation Anomaly:

Simple query  $\rightarrow$  [S-Id=4] change name from Amit to Amitpal.

update student

Set Sname = 'Amitpal'

where S-Id = 4

→ Code.

No problem here.

Now,

If we want to change the salary of faculty f<sub>1</sub> from 30k to 40k.

change salary of f<sub>1</sub> from 30k to 40k.

Now, how many times the f<sub>1</sub> repeats in table, the same no. of times updation query runs & changes them all from 30k to 40k.

Note! → There is only 1 faculty f<sub>1</sub>, then we salary <sup>must</sup> also changes 1 times. But, due to the column level duplicacy, it runs no. of times. Hence, it takes more time.

It is updation anomaly.

Now, Normalization removes Redundancy.

How?

- A simple 2NF may be, if we divide that table into multiple tables. Like,

<del>P.K.</del>	S-id	S-name
-----------------	------	--------

<del>P.K.</del>	C-id	C-name
-----------------	------	--------

<del>P.K.</del>	F-id	F-name	salary
-----------------	------	--------	--------

This can be 1 of the 2NF.

- Now, we don't get any anomaly in insertion, deletion, & update. There is no effect on others. Easy.

(21.)

First Normal Form :  $\rightarrow$  (1 NF)

EF Could  $\rightarrow$  Father of D.B.M.S.

- Table should not contain any multivalued attribute.

student

Roll No.	Name	Course
1	Sai	c/c++
2	Anurag	Tuna
3	Onkar	c/o BMS

$\rightarrow$  Not in 1st NF

Null means not available



Now, how to convert in 3rd NF? →

1st way

Roll no.	Name	Course
1	Sai	C
1	Sai	C++
2	Anurag	Tana
3	Omkar	C
3	Omkar	DBMS

primary key (P.K.) = Rollno. Course

(Combined, it is  
composite P.K.).

2nd way

Roll no.	Name	Course 1	Course 2
1	Sai	C	C++
2	Anurag	Tana	Null
3	Omkar	C	DBMS

P.K. = Rollno.

3rd way

Roll no.	Name
1	Sai
2	Anurag
3	Omkar

Base Table

Roll no.	Course
1	C
1	C++
2	Tana
3	C
3	DBMS

Referencing Table

P.K. = Roll no.

P.K. = Rollno Course

f.K. = Roll no.

22-

## Closure Method : →

helps

- To find all the Candidate keys in the Table.

Ex:-

Candidate key (C.K.)

 $R(ABCD)$ .FD of  $A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow D$ .

(Functional dependency).

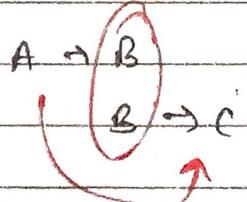
meaning of closure is that what 'A' can determine.

Here, A is determining B (from FD ①).

closure ↗  $A^+ = B$ 

sym.

$$A^+ = BCDA$$



(A can determine itself also).

Ex:- Roll no. can determine itself.

transitive.

Now,  $R(ABCD)$  has all 4 Attributes  
that are in  $A^+ = BCDA$ .

A can determine all the attributes of Table.  
This is the prop. of the Candidate key.

Now,

$$B^+ = BCD$$

Hence, B not determine A.

ii) B cannot be a C.R.

Q

$$C^+ = CD$$

$$D^+ = D$$

prime att. =  $\{A\}$

C<sub>7</sub>

Only A is C.R.

Non prime att. =  $\{B, C, D\}$ .

$$\boxed{Ck = \{A\}}$$

Note:

$$(AB)^+ = ABCD$$

(AB - itself)  
 $B \rightarrow C$   
 $C \rightarrow D$ )

Here,

AB can be a C.R.

But,

It is not a C.R.

So,

C.R. is always minimal.

In AB only A is C.R.

C<sub>8</sub> XAB is super key (S.K.).

AB  
 Super key

(A is Saath  
 adds anything  
 becomes S.K.)

AB is a super key.

Ex:

R(ABCD).

FD = {A → B, B → C, C → D, D → A}.

$$A^+ = ABCD$$

$$B^+ = BCDA$$

$$C^+ = CDAB$$

$$D^+ = DABC$$

i) C.R. =  $\{A, B, C, D\}$

all +.

prime Attribute! → are attribute which is used in making of the C.K.

Q. prime att. = {A, B, C, D}. (scr, all +  
are C.K.)

Q. Non-prime att. = { } → NULL.

Q. R(A B C D E).

$\Leftarrow FD = \{A \rightarrow B, BC \rightarrow D, E \rightarrow C, D \rightarrow A\}$ .

Now, we have to check that which attribute are coming on the right side. scr, Attributes on the right side, it will determine it at ~~not~~.

$$\begin{matrix} = B D C A \\ \underline{\underline{E}} = B D C A E \end{matrix}$$

(E will be ~~not~~ part).

Note: → Each & every candidate key must contain scr, E if present on left side, then only it is written in right side also.

जो att. Right side में नहीं आ रहा। यानि att. Left side में होने वाले हैं। तो Candidate key जाना भी उसे होगा वही होगा।

Now,

$$E^+ = EC \rightarrow (E \text{ alone is not candidate key but, it is used in natural C.K.})$$

Now, Start! →

With A!

$$A E^+, A B C D \rightarrow A \text{ & } A E$$

$$BE^+ = BECA$$

$$CE^+ = CE$$

$$DE^+ = DEABC$$

Q.

C.K. :  $\{AE, BE, DE\}$

\* Trick! - First, we got AE as C.K. So, check <sup>either</sup>  $(A \rightarrow E)$  are right side of FD.

$$FD: \{A \rightarrow B, BC \rightarrow D, C \rightarrow C, D \rightarrow A\}$$

So,

directly DE is also becomes your C.K., now check  $+D$ , it depends on 2. So, check them both prime Attrib. =  $\{A, B, D, E\}$

(Used in making C.K.).

$$\text{non-prime Attrib.} = \{C\}$$

23)

Functional Dependency :  $\rightarrow$  (F.D.)

is the method which describes the relationship b/w the attributes.

Determinant  $\rightarrow X \rightarrow Y$   $\rightarrow$  Dependent Attrib.

$X$  determines  $Y$  (or)  
 $Y$  is determined by  $X$ .

Ex:-

S-id  $\rightarrow$  Sname  $\rightarrow$  valid.

$$\begin{matrix} 1 & \rightarrow & \text{Ranjiit} \\ 2 & \rightarrow & \text{Ranjiit} \end{matrix}$$

} :- These 2 are diff.

Ex:-

$$1 \rightarrow \text{Ranjiit}$$

$$1 \rightarrow \text{Ranjiit}$$

} Same Student

Valid Case,

Ex: 1)  $x \rightarrow \text{Ranji}$   
 2)  $x \rightarrow \text{Karan}$

} Valid.

Ex: 1)  $x \rightarrow \text{Ranji}$   
 2)  $x \rightarrow \text{Karan}$

} Not Valid.

(A) F.D. are of 2 types: →

- 1.) Trivial F.D.
- 2.) Non-Trivial F.D.

Trivial F.D.: →

If

$$x \rightarrow \boxed{y}$$

then,

$y$  is subset of  $x$ .

These Trivial F.D. are valid. (Always True).

Ex:  $\frac{x}{\text{Sid}} \rightarrow \frac{y}{\text{Sid}}$

Note! →

$$x \rightarrow y$$

L.H.S  $\cap$  R.H.S  $\neq \emptyset$  (Never Null).

Ex: 1)

Sid Same  $\rightarrow$  Sid.

$\hookrightarrow$  Sid.

✓ Valid.

2.) Non-Trivial F.D.: →

If  
then,

$$x \rightarrow y$$

$y$  is not a subset of  $x$ .

i.e.

$$\boxed{x \cap y = \emptyset} \text{ (NULL)}$$

Ex:- $Sid \rightarrow Sname$  $Sid \rightarrow phone\ no.$  $Eid \rightarrow Locn$ 

(Now, for this we have to check cases.  
to find which is valid or not.)

#### ④ properties of F.O! →

1) Reflexivity: If  $y$  be subset of  $x$ . Trivial

then

$$x \rightarrow y \quad . \quad (Sid \rightarrow Sid)$$

#### 2) Augmentation:

If  $x \rightarrow y$ , then

$$x_2 \rightarrow y_2$$

$\left. \begin{array}{l} Sid \rightarrow Sname \\ Sid \rightarrow phone \rightarrow Sname \rightarrow phone \end{array} \right\}$

#### 3) Transitive: If

$$x \rightarrow y \quad \& \quad y \rightarrow z$$

then,

$$x \rightarrow z$$

$Sid \rightarrow Sname \quad \& \quad Sname \rightarrow City$   
 $Sid \rightarrow City$ .

#### 4) Union! -

$$If \quad x \rightarrow y \quad \& \quad x \rightarrow z$$

then

$$x \rightarrow yz$$

5.) Decomposition!

if

$$x \rightarrow yz$$

then

$$x \rightarrow y$$

and

$$x \rightarrow z$$

But,

$$xy \rightarrow z$$

$$y \rightarrow z \text{ & } y \rightarrow z$$

x

6.) Pseudo Transitive!

if

$$x \rightarrow y$$

$$w y \rightarrow z$$

then,

$$\underline{w} x \rightarrow z$$

7.) Composition!

$$\text{if } \underline{x} \rightarrow y \text{ & } \underline{z} \rightarrow w$$

then

$$\underline{xz} \rightarrow yw$$

(24.)

2nd Normal Form  $\rightarrow$  (2nd NF).

2 rules

- Table as Rel<sup>n</sup> must be in 1st NF.
- All the non-prime attributes should be fully functional dependent on Candidate Key (C.F.K) or (C.P.K).

(There should be no partial dependency in the Rel<sup>n</sup>).

Ex:

Part of  
CK

Non prime

AB

an

A  
(A part)

C  
(non-prime)

J+ is

partial depend

not 2nd NF

Ex!

## Customer

Customer - Id	Store - Id	Loca"
1	1	Delhi
1	3	Mumbai
2	1	Delhi
3	2	Bangalore
4	3	Mumbai

C.R. : Customer - Id Store Id

Prime attributes: C-Id

Store - Id.

Non prime: Loca"

Here, Loca" is only depend on Store - Id.  
i.e. partial dependency.

b/c,

(to be in 2nd NF it should depend on  
the both C-Id & S-Id (b/c both are PK)).

Now →

Convert it into 2nd NF →

Here, use make 2 Table.

C-Id	Store - Id
1	1
1	3
2	1
3	2
4	3

Store - Id	Loca"
1	Delhi
2	Bangalore
3	Mumbai

(here, it is fully dependent,  
b/c only 1 P.K. is here)

2nd NF

Q1:

 $R(ABCD\bar{E}\bar{F})$ FD: { $e \rightarrow f$ ,  $e \rightarrow A$ ,  $\bar{E}C \rightarrow D$ ,  $A \rightarrow B$ }

Sol: CK 2.

First, check Right hand side

Step 1:

f A D B

(Now, these attr are determined by some of the values.)

So,

On LHS, there must be CE.

CE = FADB

(C.R. जी की बनाएं) (इसे CE की तरीफ की)

Now,

 $E^+ = EC\bar{F}ADB$ 

(All 6 are present)

∴,  $E^+$  is C.R.Now, UX Trick

Either E or C must be present at the RHS of any F.D.

but

not, neither E nor C, no one is present.

So,

there is only 1 C.R. in this table.

i.e.,

 $\{C.R. = \{E\}\}$ 

Proof check

Step 1 to comp. here,

After finding C.R. = {E}

$$\begin{aligned} A^+ &= AB \\ B^+ &= B \\ C^+ &= CF \end{aligned} \quad \left. \right\}$$

i.e., proved.

proper subset is  
always less than  
a set.

$X \subset X \cup Y \rightarrow$  proper subset

$X \subseteq X \cup Y \rightarrow$  subset

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Page

Step 2 prime attributes: {E, C}

non-prime attributes: {A, B, D, F}.

Step 3: C.R. = {E, C}

What is proper subset of C.R.

↳ either 'E' or 'C'.

Now  
check!

F.D. = {C → F, E → A, EC → D, A → B}

(P.D.)

(either proper subset of C.R.)

for partial dependency check on LHS ↳ either 'C' or 'EC' (AND)  
check on RHS ↳ whether it is non-prime attr.

not in R.H.S.  
2nd NF

C → F

↳ partial dependency.

So,

Table is not in 2nd NF.

$C \rightarrow F$	<u>XPD3</u>	partial
$E \rightarrow A$	<u>XPD3</u>	.
$EC \rightarrow D$	<u>XPD3</u>	fully.
$A \rightarrow B$	<u>XPD3</u>	.

→ 1 st P.O.

∴ Given table  
is not in 2nd NF.

25-

3rd NF: →

Table or Rel must be in 2nd NF.

→ There should be no transitive dependency  
in table.

Non prime or Non-unique  
prime or unique.



Date: \_\_\_\_\_  
Page: \_\_\_\_\_

(3)

not sufficient cond'n.

(NPA)!

\* Mean, Non-prime attr. are attrs. Non-prime attr.  
determine it is the right).

(C.R. & Prime attr. (P.A.) at one right  $\Rightarrow$  determine NPA attr.).

Ex:-

<u>Rollno.</u>	State	City	C.R. = $\alpha$ Roll no.)
1	Punjab	Mohali	
2	Haryana	Ambala	F.D $\rightarrow$ $\alpha$ Roll no + state,
3	Punjab	Mohali	state $\rightarrow$ city )
4	Haryana	Ambala	
5	Bihar	Patna	

$\Rightarrow$  PA =  $\alpha$  Roll no. 3

$\Rightarrow$  NPA =  $\alpha$  state, city 3.

So,

here  $\underline{\text{Roll}} \rightarrow \underline{\text{State}}$  and  $\underline{\text{State}} \rightarrow \underline{\text{city}}$ .

It is Transitive dependency & we don't want that.  
so,

It is not in 3rd NF.

Ex:- R (ABCDEF)

FD: { AB  $\rightarrow$  C, C  $\rightarrow$  D }

$\Rightarrow$

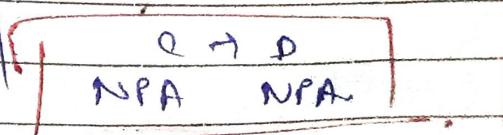
C.R. =  $\alpha$  AB3

PA =  $\alpha$  A, B3

NPA =  $\alpha$  C, D3

Transitive

$AB^+ = ABCDEF$



∴

It is not in 3rd NF.

C.R. + anything = S.R.

Super Key



Date: \_\_\_\_\_  
Page: \_\_\_\_\_

~~Ex:~~ R (AB CD).

FD: (AB  $\rightarrow$  CD, D  $\rightarrow$  A).

Soln: C.R.: {AB, DB}.

PA: {A, B, D}.

NPA: {C}.

(B not on RHS)

$$B^+ = B$$

$$AB^+ = ABCD$$

Now, A on RHS.

$$DB^+ = DBAC$$

is also C.R.

~~Ex:~~ Now, for each F.D.

LHS  $\rightarrow$  C.R. on S.R.

$$\text{RHS} \rightarrow \text{L.O.P.A.}$$

+ check only 1 bcz [OR].

FD: (AB  $\rightarrow$  CD, D  $\rightarrow$  A).

✓ ✓

Table is in 3rd NF.

bcz,

(NPA  $\rightarrow$  NPA') is not present here.

26.

BCNF. (Boyce Codd Normal Form):

→ also called as special case of 3rd NF.

~~Ex:~~,

~~Ex: If we have then 3rd NF  
L.O.P. Only 1 C.R.~~

Student

Roll-no	Name	Matric-id	Age
1	Ram	K0123	20
2	Warun	M034	21
3	Ram	K786	23
4	Rahul	D286	21

Table is in  
3rd NF  
already.

C.R. = Roll no., Name - Id 3.

$$f.D.: = \left\{ \begin{array}{l} \text{Roll no.} \rightarrow \text{name} \\ \text{Roll no.} \rightarrow \text{matrid} \\ \text{matrid} \rightarrow \text{age} \\ \text{matrid} \rightarrow \text{Roll no.} \end{array} \right\}$$

Note: LHS of each FD should be C.R. or S.R.

Here, 3NF's की (AR) अभी बनिए हुए हैं, जिसमें RHS के P.A. को नहीं भी आए चल जाता था).

Here,

we only want C.R. or S.R. in L.H.S. & RHS से कोई लेना देना नहीं।

Soln:-

So, check all the f.D. one by one.

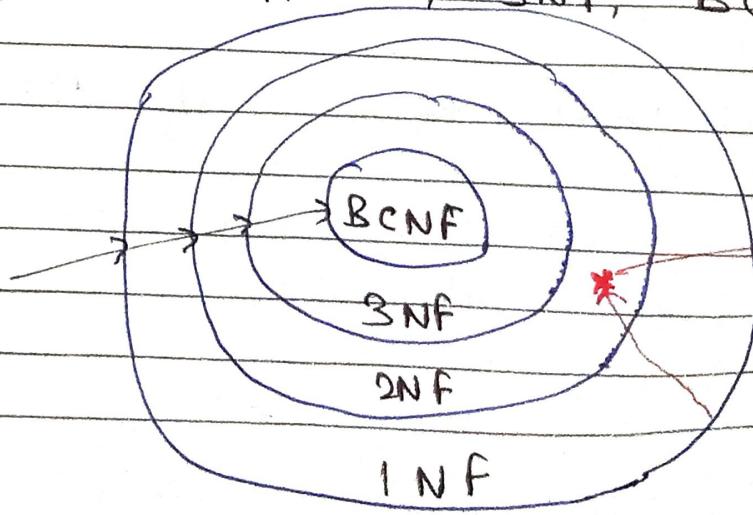
In all the 4 f.D, the LHS is C.R.

So,

It is in BCNF form.

∴

# Compare:- INF, 2NF, 3NF, BCNF :-



It is outside  
3NF &  
In 2NF &  
INF both.

TC

INF.

2NF = INF + cond'ns

3NF = 2NF + cond'ns

BCNF = 3NF + cond'ns

X

X

Join

2.7 Lossless & Lossy Decomposition!

We normalize table  $\rightarrow$  or we decompose table into INF, ... forms.

R

	A	B	C
1	2	1	
2	2	2	
3	3	2	

$\rightarrow R_1 (AB)$

$\rightarrow R_2 (BC)$

1 We divide this table into  $R_1$  &  $R_2$

2

B is common to both the Table.

$R_1$

	A	B
1	2	
2	2	
3	3	

$R_2$

	B	C
2	1	
2	2	
3	2	

2 find the value of C if the value of A = 1.

No

Now, for this we have to join  $R_1$  &  $R_2$  tables.

So,

Select R<sub>2</sub>. C from R<sub>2</sub> Natural Join R<sub>1</sub>  
where R<sub>1</sub>. A = '1'.

(1st row of Multiply all rows  
(at start of Table 2)).

Cross product:- If R<sub>1</sub> has x rows &  
R<sub>2</sub> has y rows }

then

there join has x.y rows - .

condin': Common ~~different~~ col<sup>m</sup> of both  
Tables (R<sub>1</sub> & R<sub>2</sub>) . here (B) has the  
same value in join Table.

Natural Join = Cross product + condin'.

Now,

	R <sub>1</sub>		R <sub>2</sub>		
	A	B	B	C	
{	1	2	2	1	✓
	1	2	2	2	✓
{	2	2	2	1	✓
	2	2	2	2	✓
{	3	3	2	+	
	3	3	2	2	
	3	3	3	2	✓

Now,

R<sub>1</sub>

(Note).  
Spurious of  
tuples.

A	B	C
1	2	1
1	2	2
2	2	1
2	2	2
3	3	2

table after  
Joining.

In original Table ( $R$ ), we have only 3 tuples (rows).

but,

After Joining, in  $R'$ , we have 5 tuples.

(contr)  
It is a flaw. It is called the **Lossy Decomposition**.

- Why lossy?

Here, we get 2 extra rows, then, why lossy.

Here,

We don't talk about rows. We call it lossy because of inconsistency. There is a problem in Database.

⇒ In original, for  $A=1$ ,  $C = 1$ .

but

In join table, for  $A=1$ ,  $\begin{cases} C = 1 \\ C = 2 \end{cases}$

① Why we get longer? ( $C_2$  tuples more)

∴ here, we take  $B$  as common in both Table, but

Criteria for Common: Common Attribute should be C.R. or S.R. of either  $R_1$  or  $R_2$  or both.

So, we have to C.R. or S.R. of original Table.

- 7)  $\rightarrow$  R has duplicacy in Table. We have to choose attr. 'A' for Right Ans. bcz, A is unique.  $\{1, 2, 3\}$ .

$R_1$	$C_{AB}$
$R_2$	$C_A$

We get 3 tuples  
also in joining table.

- # Cond'n for lossless Joining Decompositn  $\rightarrow$

1.)  $R_1 \cup R_2 = R$ ,

$AB \cup AC = ABC$ .

2.)  $R_1 \cap R_2 \neq \emptyset$

$AB \cap AC$

$A \neq \emptyset$

(C.R. of  
original table)

- 3.)  $R_1$  C.R. (or)  $R_2$  C.R. (or) Both

To take common attribute  $\rightarrow$

28. Fill normal forms with real life Examples  $\rightarrow$

	1st NF	2nd NF	3rd NF.
1	$\rightarrow$ No multivalued attribute.	$\rightarrow$ In 1st NF + No partial dependency.	$\rightarrow$ In 2nd NF. + $\rightarrow$ No Transitive dependency.
2	$\rightarrow$ only single valued.	* only full dependency.	$\rightarrow$ No, NP A. should determine N.F. A.

$(AB) \rightarrow C$

If A & B are 2 F.O.  
of a L, then both will  
use the Emplo. 'C'.

~~B CNF~~

In 3<sup>rd</sup> NF

+

LHS must be C.R. or S.K.

S.K.

$X \rightarrow Y$

4<sup>th</sup> N.F.

In BCNF

+

No multi valued dependency.

$X \rightarrow Y$

5<sup>th</sup> N.F.

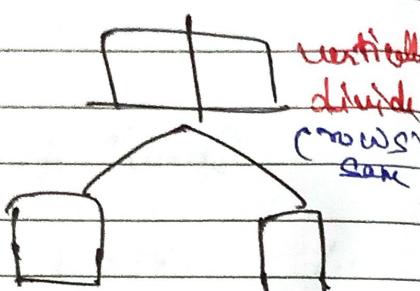
In 4<sup>th</sup> NF

+

lossless decomposition

Maren  $\rightarrow$  3 Phone no.  
 $\rightarrow$  3 Mail Id.

(Maren depends on multiple att. i.e., phone & mail)



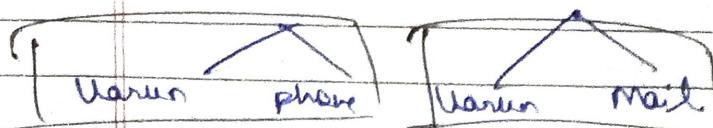
table

Maren	M <sub>1</sub>	E <sub>1</sub>
Maren	M <sub>1</sub>	E <sub>2</sub>
1	M <sub>1</sub>	E <sub>3</sub>
	M <sub>2</sub>	E <sub>1</sub>
	M <sub>2</sub>	E <sub>2</sub>

80,  
Match 2 table.

May be extra tuples  
Come - 80,  
make. C.R. as  
common attribute in  
both tables.

Very long.  
use also.  
don't able  
to form  
a key.



(Now, no multivalued dependency).

23.

Minimal Cover:  $\rightarrow$  (Irreducible).

Q: For the following functional dependencies, find the correct Minimal Cover  $\rightarrow$ .

$\{A \rightarrow B, C \rightarrow B, D \rightarrow ABC, AC \rightarrow D\}$ .

- a)  $A \rightarrow B, C \rightarrow B, D \rightarrow A, AC \rightarrow D$ .
- b)  $A \rightarrow B, C \rightarrow B, D \rightarrow C, AC \rightarrow D$ .
- c)  $A \rightarrow BC, D \rightarrow CA, AC \rightarrow D$ .
- d)  $A \rightarrow B, C \rightarrow B, D \rightarrow AC, AC \rightarrow D$ . *Ans*

*Soln:* Our RHS in F.D. must be single.

~~Step 1~~:  $\{A \rightarrow B, C \rightarrow B, D \rightarrow \underline{ABC}, AC \rightarrow D\}$ .

By "decomp" prop, separate them.

$A \rightarrow B, C \rightarrow B, D \rightarrow A, D \rightarrow B, D \rightarrow C, AC \rightarrow D$ .

~~Step 2~~: Remove the redundant F.D.  $\Rightarrow$

$\{A \rightarrow B, C \rightarrow B, D \rightarrow A, D \rightarrow B, D \rightarrow C, AC \rightarrow D\}$ .

Let  $\{A \rightarrow B\}$  ch. set RST, Now check the closure of A,

$$T^{A^+} = A \quad (\text{not all } +).$$

$A \rightarrow B$  is not redundant. We can't remove it.

→ Same check this for every F.D.  $\Rightarrow$

↳  $D \rightarrow B$  is redundant.

↳ Let  $(D \rightarrow B)$  ~~x~~ than,  $D^+ = DABCS$  (all +).

$T \text{ remove, } D \rightarrow B$

Now we will check ch. at which red. is, start at SETE & remove the F.D. 1.

Now, for

$$AC \rightarrow D \quad \times$$

$$AC^+ = ACB.$$

So,

also include

$$AC \rightarrow D$$

Now, we get

$$\{ A \rightarrow B, C \rightarrow B, D \rightarrow A, D \rightarrow C, AC \rightarrow D \}.$$

Step 3: Now, we only want 1 Atm in LHS.

Here,

$$AC \rightarrow D$$

Now, check by removing A. & then  
check closure of C

$$C^+ = CB$$

उदाहरणीय C<sup>+</sup> से यह 'A' गत नियत भावना है कि A का एक संकेत है। इसका उपर्युक्त अस्ति भावना है।

$$AC \rightarrow D \text{ की दृष्टि } ।$$

Same check w/ A, by removing C.

$$A^+ = AB.$$

So, can't remove C.

So,  $AC \rightarrow D$  can't be reduced.

So,

$$\{ A \rightarrow B, C \rightarrow B, D \rightarrow A, D \rightarrow C, AC \rightarrow D \}.$$

compose

$$\boxed{\{ A \rightarrow B, C \rightarrow B, D \rightarrow AC, AC \rightarrow D \}}.$$

Q.E.D.

(30)

Question on Normalization : →

Q1. R (ABCDEF), check the highest normal term?

F.D. !  $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow A\}$ .

Soln: Find all C.R.s in Rola<sup>n</sup>! →  
Step 1:

By closure method ! →

(B is not on RHS.) So, B compulsory.

$$B^+ = B \underline{\quad}, A^+ = \underline{A}.$$

-  $AB^+ = ABCDEF$  (Call +).

C,

(AB is C.R.)

Now, Check + A on RHS.  
we get,  $F \rightarrow A$

$$\text{F} \rightarrow \text{A}$$

C,

(FB is also C.R.)

Now, check F on RHS !

$$E \rightarrow F$$

C,

E B is also C.R.

Now, check E on RHS.

$$C \rightarrow D \text{ (E)}$$

C,

C B is also C.R.

Now check + C on RHS.

$AB \rightarrow C$

$AB$  is already on R.H.S.  
So, we get all C.R.

C.R. =  $\alpha AB, FB, CB, CB \beta$  + A.C.R.

Step 2: Write all prime attr. & N.P.A!  $\rightarrow$

P.A. = {A, B, C, E, F}

N.P.A = {D}

Step 3: Now, check FD!  $\rightarrow$

$\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow A\}$

Now,

Check 1-by-1.

Highest NF: 1NF, 2NF, 3NF, BCNF,

Redundancy  $\rightarrow$  decreases.

\* mean, When table is in BCNF, then redundancy is lowest. & in 1NF redundancy is highest.

\* So, to check highest NF, we start from BCNF!  $\rightarrow$ .

\* In BCNF, we know, all LHS of all FD's should be CR or SF.

of  $\underline{AB} \rightarrow C$ ,  $C \rightarrow DE$ ,  $E \rightarrow F$ ,  $F \rightarrow A$

|      x      |      x      |      x      |

↓

It is not in BCNF form.

→ Now, 3NF!

Check: → transitive dependency

(NPA  $\rightarrow$  NPA)

$LHS \rightarrow C.P. \text{ or } S.P.$ <small>TOP</small> $RHS \rightarrow \text{is a P.A.}$	<small>then</small> It is 3NF.
---	-----------------------------------

Now, 1st Cond'n is already checked in BCNF.

So, here check only 2nd cond'n that whether RHS is P.A. or not.

	$\underline{AB} \rightarrow C$	$C \rightarrow DE$	$E \rightarrow F$	$F \rightarrow A$
BCNF	✓	x	x	x
3NF	✓	x	✓	✓

∴ not in 3NF :)

→ Now, 2NF!

Same thing → if there is already a tick in 3NF, then we don't have to check that for 2NF. If already 2NF it will still check only for 'x' tick.

Check!

LHS is proper subset of C.R.  
RHS is non-prime attr.

for partial dependency i.e.,  
it true then not in 2nd NF.

$AB \rightarrow c$  |  $c \rightarrow de$  |  $e \rightarrow f$  |  $f \rightarrow A$ .

BCNF

✓

✗

✗

✗

3NF

✓

✗

✓

✓

2NF

✓

✗

✓

✓

1st NF

✓

✗

✓

✓

(bcz both  
cond'n true),  
 $f_1$  not in 2NF.

∴ Ans is 1st NF. why.

bcs

for 1st NF, that we don't want  
any multivalued attribute in the  
table. All attr. must be single (atomic).

Ex

Table  $\rightarrow$  R (ABCDEF)

all are general attr.

we can't tell them as atomic or  
multivalued by seeing them.

Table already 1st NF it is fixed.  
↳ (assume already).

1st NF.

Ans

proper subset is always less than a set.

SN

Date: \_\_\_\_\_  
Page: \_\_\_\_\_

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Q1-

Find out Normal Form of a Reln' : →  
(from 1NF - BCNF).

Q1:- R(ABCDEF),

FD's: {AB → C, C → D, C → E, E → F, F → A}

C.K. = {AB, FB, CB, CB}.

P.A. = {A, B, C, E, F}

NPA = {D}

Soln! Now, let us assume that R(ABCDEF) is already in 1st NF.

→ Check for 2nd NF: →

(Partial) P.D.  
(Depend.)

Cond'n  $\Rightarrow$  { LHS must be proper subset  
of any C.K.  
and  
RHS must be a Non-P.A. }

F.D's of AB → C, C → D, C → E, E → F, F → A }  
F & F      T & T      T & F      T & F      T & F  
FO      PD      FO      FO      FO

(full dependency).

∴ not in 2nd NF.

→ Make it in 2nd NF: →

We do it by decompose the table.  
(Divide into 2 parts).

## Condition

Common Attribute Must be C.R.

- 1.) Lossless Decomposi<sup>n</sup>
  - 2.) Dependency should be preserved.

Now, w<sup>t</sup> problem  $\in \mathbb{NP}$ , C-I-D, 3sat

Aleg one at, Aleg Table at GTI.

~~Notes~~

$$R(AB\overline{CD}EF)$$

Now, we have to make a common attr. b/w these 2 table! -

Criteria # common! - can be C.R. of any  $R_1 \Delta R_2$ .

Q. In  $R_2$  ( $C(D)$ )  
 $c \rightarrow d$   $c + d = c_0$  (call 2).  
 $c_1$   $\{c \text{ is C.L.}\}$

Make 'c' common in both  $R_1$  &  $R_2$ .

Now,  
~~again~~

$\ell (ABCD \& F)$

R ✓

$\rightarrow R_2$   
(c.d)

$\{ \overline{P_i}, AB \rightarrow C, C \rightarrow E, E \rightarrow F, F \rightarrow A \}$

$$f_2 \circ c \rightarrow \Delta^3$$

2nd NF

2nd NF.

$\{e\}$  itself  
is not its  
proper subset

Now!Check + 3NF! →

$\left. \begin{array}{l} \text{LHS must be C.R.} \\ \text{RHS be P.A.} \end{array} \right\} \rightarrow \text{3NF}$

so,

 $R_1$  $(ABCDEF)$  $\{AB \rightarrow C, C \rightarrow E, E \rightarrow F, F \rightarrow A\}$  $\checkmark \quad \checkmark \quad \checkmark \quad \checkmark$  $R_2$  $(CD)$  $\{C \rightarrow D\}$  $C.R. = \{AB, FB, EB, CB\}$  $PA = \{A, B, C, E, F\}$ . $C.R. = \{C\}$ . $PA = \{C\}$ .

1.

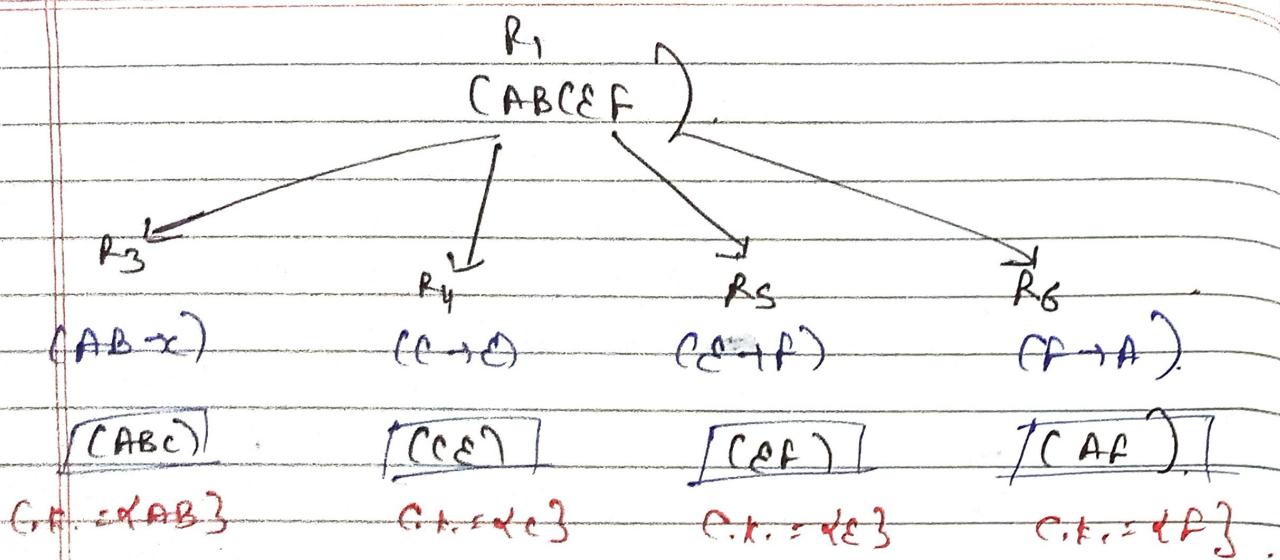
gt is 3rd NF.gt is also 3rd NF.Now!Check + BCNF! →Condition → L.H.S. must be a C.R. $R_1 \{AB \rightarrow C, C \rightarrow E, E \rightarrow F, F \rightarrow A\}$  $\checkmark \quad \times \quad \times \quad \times$ not in BCNF form. $R_2 \{C \rightarrow D\}$ gt is BCNF form.→ There is Redundancy.Now,Again Decompose  $R_1$ . $(ABCDEF)$ .Redundancy = 0%.(will problem ch2.2d, 3rd part. Any check!)

Normalisation's aim → To make redundancy 0%.

**3**

**3**

→ de-composes  
→ says: normalise

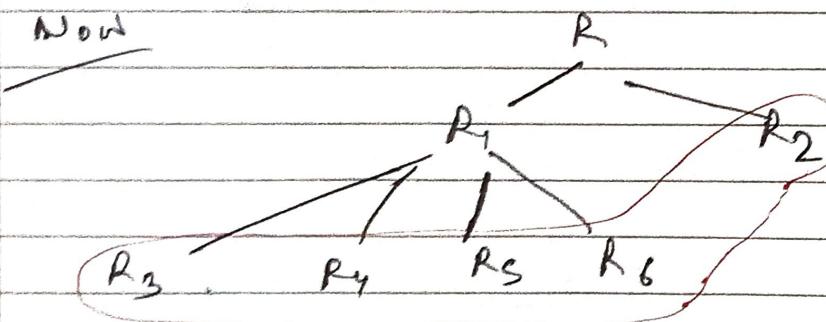


Now, these all 4 tables have C.K.

So,

These all 4 are in BCNF now.

→ (G, E, D, A) - common attr & (B, F) - common attr.



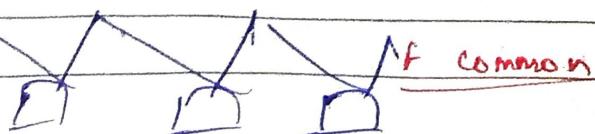
Now, In all these 5 tables,

Redundancy is 0%.

But, there are now multiple tables &  
if we join them again, it is complex.

Cnf) have to Join  $R_3$  &  $R_4$  (both have common (C))

$R_3$        $R_4$        $R_5$        $R_6$



→ But, John  $R_3$  &  $R_5$ .  
 $(ABC)$   $(CEF)$ .  
 There nothing is common.

We can't join them directly. So,  
 take help from  $R_4$ .

→ So, Combine  $R_3 \Delta R_4$ , let,  $R_3 R_4$   
 $(ABCE)$

Now,

We can combine it with  $R_5$  bcz both  
 have now 'E' as common att.

$R_3 R_4 R_5$   $(ABCEF)$ ,

→ E to calc. now

32.

## Normalisation Questions: →

→ If a reln is in BCNF, then it is in 2NF also

Q: If a Reln R has 8 att.  $(ABCDEFGH)$

$F = \emptyset$   $CH \rightarrow G$ ,  $A \rightarrow BC$ ,  $B \rightarrow CFH$ ,  $E \rightarrow A$ ,  $F \rightarrow EG$ ,

how many candidate keys in R.

a) 3

b) 4

c) 5

d) 6

Soln:

First, check on RHS, which att is absent.

D

→ So, now it comes with every.

$D^+ = D$

✓  $AD^+ = AD \cup BC \cup FHGSE$

(Call 8),

Now, check A on RHS,

so,

✓  $ED^+$  also a C.F.

Now, check E on RHS.

so,

✓  $FD^+$  also a C.F.

Now, check F on RHS.

so,

✓  $BD^+$  also a C.F.

Now, check B on RHS.

Now, completed,

so,

$\boxed{AD, ED, FD, BD} \rightarrow$  C.F. ✓

33.

Ques Explained on Normalisation: →

Scheme is a structure of a Table.

→ So, Scheme (or) Table  $\rightarrow$  same.

→ Non total F.D. means In which.

$\boxed{\text{LHS} \cap \text{RHS} = \emptyset} \rightarrow$  we have to  
check that it  
be valid or not.

→ Total F.D. are always valid.

~~Schema 1 :~~ Registration (roll.no, Courses)

Non-trivial F.D of roll no  $\rightarrow$  Courses ? :

Ans → We have to check that this table is in which form.

→ So, as always, start from higher form.

→ Check  $\rightarrow$  BCNF :-

condi<sup>n</sup> : LHS of every FD must be C.R. or S.R. or P.K.

and,

roll.no be already given as a C.R.

So,

LHS is a C.R. of F.D.

So,

Table is in BCNF form.

∴ also in 1st NF, 2nd NF & 3NF.

~~Schema 2 :~~ Registration (roll.no, Course\_id, email)

Non-trivial FD of roll no, Course\_id  $\rightarrow$  email  
email  $\rightarrow$  roll no.

Ans → C.R. = { rollno Course\_id } .

PA = { roll no, Co. ID } .

NPA = { email } .

→ Check BCNF  $\rightarrow$  1st FD. LHS is C.R.

but not in 2nd F.D.

not in BCNF form.

→ Check for 3NF! :

Condition: LHS must be a CK or PK  
[OR] -  
Ans must be a P.A.

Now, 1st FD is already valid,

2

2nd FD: email → roll no.

P.A.

F

T.

G.

(T)

It is in 3NF.

cyl.

Schema 3: Register ( Roll no., C-Id, marks, grade ).

Non-trivial FD: { of roll no., C-Id → marks, grade }  
marks → grade . }

Ans: C. t. = { roll no C-Id } .

PA = { roll no, C-Id } .

NPA = { marks, grade } .

→ check for BCNF!

1st FD → valid.

2nd FD → not valid.

∴

not in BCNF.

→ check for 3rd NF:

1st FD → already valid

2nd FD → marks → grade.

F

F

∴ not in 3rd NF.

- check & 2nd NF: →

condit.

LHS must be a proper subset of L.  
T AND

RHS must NPA.

$C_3$  for p.D.  $\rightarrow$  i.e., not in 2nd NF.

if both cond" are true.

+ Let FD  $\rightarrow$  already valid.

2nd PD → marks → grade  
f T

M f

$f_7$  not in partial dependency

Get to be in 2nd NF. Sum

Scheme 4: Register (roll no, C-Id, Credit)

Non-trivial FD of roll no; C-Id  $\rightarrow$  Credit  
C-Id  $\rightarrow$  Credit }  $\Rightarrow$

Ans. 1 C.R. = df ~~all no~~ (C - Id)

$$PA = \{ \text{all } n, c - \text{Id} \}$$

NPA = & credit 3.

→ check ~~if BCNF!~~

1st FD  $\rightarrow$  ✓

2nd FD  $\rightarrow$  x

}  $\Rightarrow$  not in BCNF.

→ Check # 3NF:-

1st FD → ✓

2nd to → C-Id → Credit  
f f

So, not in Bond NF.

Check + 2NF! →

Let  $f_D \rightarrow L$

2nd FD → C-Iol → Credit  
↑              ↑  
 $\text{F} + \text{F}$

∴ It is Partial Dependency (P.D.)

88

It is not in 2nd NF.

Table is in 1st NF.  
We already assume it).

—X—  
—X—

## 34. Cover & Equivalence of f.d. : →

If  $x$  covers  $y$        $y \leq x$   
 If  $y$  covers  $x$        $x \leq y$

∴ If both are true,  
 then,  $\{x = y\} \Rightarrow$  Equivalent.

$$\text{S! } x = \{A \cap B, B \rightarrow C\} \quad | \quad y = \{A \cap B, B \rightarrow C, A \rightarrow C\}, \quad C$$

i) x comes 4: - (4cx)

(इसमें 4 की FD. में LHS का closure लगे तोका x वाले में से 1).

Sect.

$$A^+ = ABC$$

$$B^+ = BC$$

$$Y = \{ A \rightarrow B, B \rightarrow C, A \rightarrow C \}.$$

$\Rightarrow$  all 3 covers in these closure forms.

i)

$$X \text{ covers } Y. \quad \checkmark$$

ii)

$$Y \text{ covers } X: \rightarrow$$

$$X = \{ A \rightarrow B, B \rightarrow C \}.$$

$$A^+ = ABC$$

$$B^+ = BC$$

( $X$  not closure)  
 $Y$  not cover

$\Leftarrow$

$$Y \text{ also covers } X. \quad \checkmark$$

$\Leftarrow$

both symbols cancels each other & become equivalent.

$$X \not\equiv Y \quad Y \not\equiv X$$

$$X \equiv Y$$

$$\Leftrightarrow$$

ex. Q:  $X = \{ AB \rightarrow CD, B \rightarrow C, C \rightarrow D \}$ .

$\Leftarrow$

$$Y = \{ AB \rightarrow C, AB \rightarrow D, C \rightarrow D \}.$$

$\Rightarrow$  i)

$$X \text{ covers } Y: \rightarrow$$

$$Y = \{ AB \rightarrow C, AB \rightarrow D, C \rightarrow D \}.$$

$$AB^+ = ABCD,$$

$$C^+ = CD$$

$\Rightarrow$  True

ii)  $Y$  covers  $X$ ?

$$X = \{AB \rightarrow CD, B \rightarrow C, C \rightarrow D\}.$$

✓      ✗      ✓

$$\underline{AB^+ = ABCD}, \underline{B^+ = B}, \underline{C^+ = CD} \quad (\text{from } Y).$$

✗      ✗      ✓

∴  $Y$  not covers  $X$ .

It becomes false.

∴

$$\boxed{X \neq Y} \quad \text{oh.}$$

$$\boxed{X \supseteq Y} \quad & \boxed{Y \supseteq X}.$$

✓, true.

✗, false.

∴

(35)

### Dependency Preserving Decomposition ↗

Def'n: ↗ (i.e., any table  $R(ABCDO)$ )

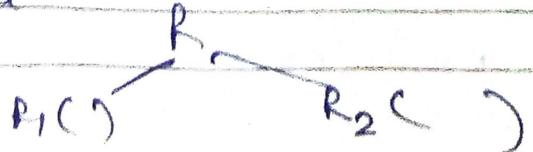
& also some F.D.,  $\{FD(A \rightarrow B, B \rightarrow C)\}$

Now,

we find closure & then find c.t., &  
then we also find hidden dependencies! ↗  
like.

$FD^+ \models A \rightarrow C$  } by Transitive  
prop.  
and,

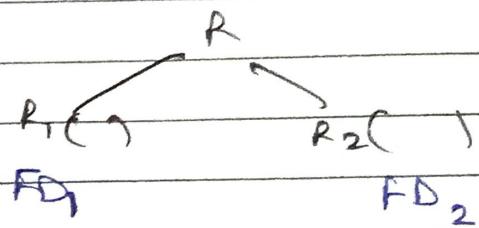
→ In normalisa<sup>n</sup>, we do decompis<sup>n</sup>,  
then, we divide



∴ We distribute attr. of R in  $R_1, R_2, R_3$

union of attr. of  $R_1 \cup R_2$ , must be equal to the attr. of R.

Now, F.D. also divides, i.e.



Now,

Check! - Dependency should be preserved,

(Can't this F.D. lost or get extra st, which preserve both 2nd & 1st).

i.e.

$$FD_1 \cup FD_2 = FD^*$$

(original F.D.  
are equal)

Q: Let R (ABCD) with F.D.

$A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow B$  3.

R is decomposed into  $R_1 (AB), R_2 (BC), R_3 (BD)$

$R_1 (AB)$	$R_2 (BC)$	$R_3 (BD)$
$A \rightarrow A$	$B \rightarrow C$ ✓	$B \rightarrow D$ ✓
$B \rightarrow B$	$C \rightarrow B$ ✓	$D \rightarrow B$ ✓
$A \rightarrow B$ ✓		
$B \rightarrow A$ ✗		

$B^* = BCD$

(don't have A).