



## Mass Transfer Coefficient

Pierre Le Cloirec

Ecole Nationale Supérieure de Chimie de Rennes

11 allée de Beaulieu, CS 50837

35708 Rennes cedex 07, France

Tel 33 (0) 2 23 23 80 00 e-mail Pierre.Le-Cloirec@ensc-rennes.fr







### General equation

$$N_{A} = \frac{N_{A}}{N_{A} + N_{B}} \frac{C D_{AB}}{z} Ln \left[ \frac{N_{A} / ((N_{A} + N_{B}) - C_{A_{2}} / C)}{N_{A} / ((N_{A} + N_{B}) - C_{A_{1}} / C)} \right]$$

For liquid

$$\mathbf{x}_{\mathbf{A}} = \frac{\mathbf{C}_{\mathbf{A}}}{\mathbf{C}}$$

For gas

$$\mathbf{y}_{\mathbf{A}} = \frac{\mathbf{C}_{\mathbf{A}}}{\mathbf{C}} = \frac{\mathbf{P}_{\mathbf{A}}}{\mathbf{P}_{\mathbf{T}}}$$

$$\mathbf{N_A} = \frac{\mathbf{N_A}}{\mathbf{N_A} + \mathbf{N_B}} \mathbf{F} \mathbf{Ln} \left[ \frac{\mathbf{N_A} / (\mathbf{N_A} + \mathbf{N_B}) - \mathbf{C_{A_2}} / \mathbf{C})}{\mathbf{N_A} / (\mathbf{N_A} + \mathbf{N_B}) - \mathbf{C_{A_1}} / \mathbf{C})} \right]$$

F: mass tranfer coefficient







# Specific™case A diffusing B immobile

### For gas

$$\mathbf{N}_{\mathbf{B}} = \mathbf{0} \qquad \qquad \frac{\mathbf{N}_{\mathbf{A}}}{\mathbf{N}_{\mathbf{A}} + \mathbf{N}}$$

$$\mathbf{N}_{\mathbf{A}} = \frac{\mathbf{D}_{\mathbf{AB}}}{\mathbf{RTz}} \frac{\mathbf{P}_{\mathbf{T}}}{\mathbf{P}_{\mathbf{B}}} (\mathbf{P}_{\mathbf{A1}} - \mathbf{P}_{\mathbf{A2}})$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{G}} \left( \mathbf{P}_{\mathbf{A}1} - \mathbf{P}_{\mathbf{A}2} \right)$$







# Specific case A diffusing B immobile

### For gas

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{G}} \left( \mathbf{P}_{\mathbf{A}1} - \mathbf{P}_{\mathbf{A}2} \right)$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{y}} (\mathbf{y}_{\mathbf{A}1} - \mathbf{y}_{\mathbf{A}2})$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{c}} \left( \mathbf{C}_{\mathbf{A}1} - \mathbf{C}_{\mathbf{A}2} \right)$$







# Specific™case A diffusing B immobile

For liquid

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{L}} \left( \mathbf{C}_{\mathbf{A}1} - \mathbf{C}_{\mathbf{A}2} \right)$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{x}} \left( \mathbf{x}_{\mathbf{A}1} - \mathbf{x}_{\mathbf{A}2} \right)$$







# A diffusing B diffusing at countercurrent equimolarly

$$N_A = -N_B$$

$$\mathbf{N}_{\mathbf{A}} = \frac{\mathbf{D}_{\mathbf{A}\mathbf{B}}}{\mathbf{R}\mathbf{T}\mathbf{z}} (\mathbf{P}_{\mathbf{A}\mathbf{1}} - \mathbf{P}_{\mathbf{A}\mathbf{2}})$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{G}}^{'} \left( \mathbf{P}_{\mathbf{A}1} - \mathbf{P}_{\mathbf{A}2} \right)$$







# A diffusing B diffusing at countercurrent equimolarly

For gas

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{G}}^{'} \left( \mathbf{P}_{\mathbf{A}1} - \mathbf{P}_{\mathbf{A}2} \right)$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{y}}' \left( \mathbf{y}_{\mathbf{A}1} - \mathbf{y}_{\mathbf{A}2} \right)$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{C}}' \left( \mathbf{C}_{\mathbf{A}1} - \mathbf{C}_{\mathbf{A}2} \right)$$







# A diffusing B diffusing at countercurrent equimolarly

For liquid

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{L}}^{'} \left( \mathbf{C}_{\mathbf{A}1} - \mathbf{C}_{\mathbf{A}2} \right)$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{x}}' \left( \mathbf{x}_{\mathbf{A}1} - \mathbf{x}_{\mathbf{A}2} \right)$$







#### Remark 1

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K} \left( \mathbf{C}_{\mathbf{A}1} - \mathbf{C}_{\mathbf{A}2} \right)$$

$$\mathbf{q} = \mathbf{h} \big( \mathbf{T}_1 - \mathbf{T}_2 \big)$$

#### Remark 2

F is different as a function of the operating conditions

$$F = \frac{D_{AB}}{z}$$

$$F = \frac{D_{AB}P_{T}}{RTz}$$

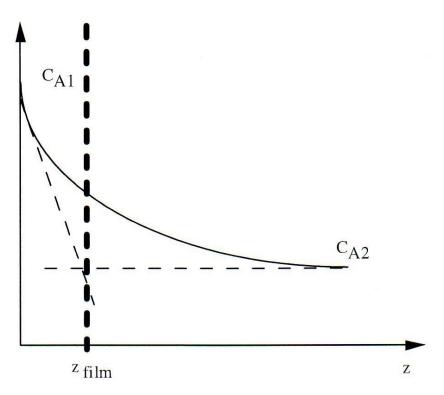
$$F = \frac{D_{AB}P_{T}}{RTz}$$







# Film theory



$$z \sim \frac{L}{\sqrt{\frac{V.L}{\nu}}} = \frac{L}{\sqrt{Re}}$$

$$\mathbf{N}_{\mathbf{A}} = \mathbf{K}_{\mathbf{L}} \left( \mathbf{C}_{\mathbf{A}1} - \mathbf{C}_{\mathbf{A}2} \right)$$

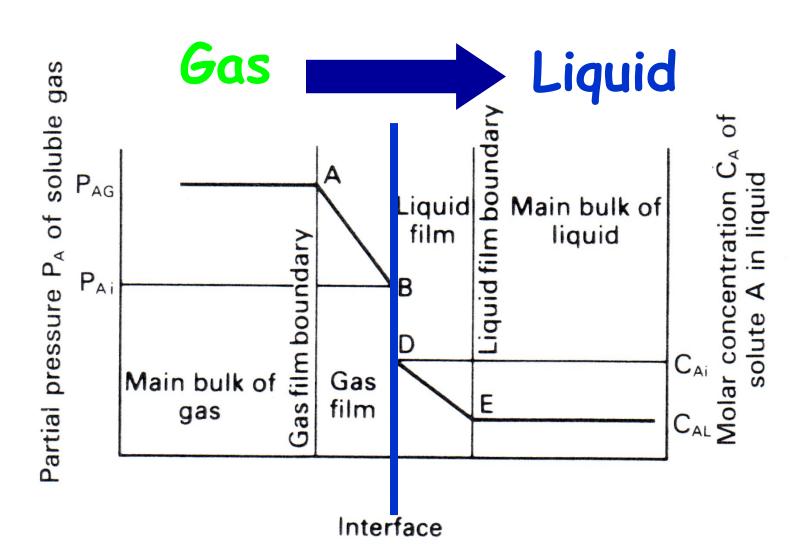
$$\mathbf{K}_{\mathrm{L}} = \mathbf{f}(\mathbf{D}^{\mathrm{n}})$$

$$K_L \approx 0.8 - 0.9$$





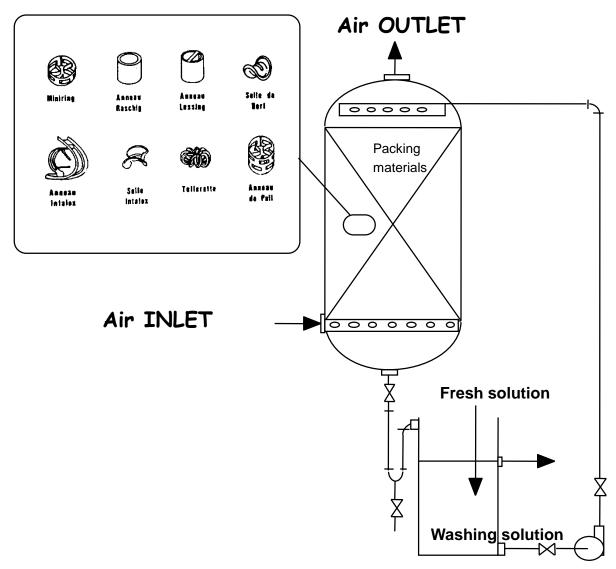
## Double Film Theory

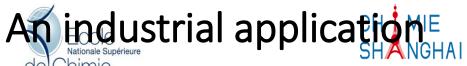
























### How to determine the mass transfer coefficients?

- 1. To define adimensionnel number (operating conditions)
- 2. To determine empirical (statistical) relations between the adimensionnel numbers







### To define adimensionnel number (operating conditions)

Reynolds

Sherwood

Schmitt

Stanton

 $J_D$ 

$$Re = \frac{dU\rho}{\mu}$$

$$\mathbf{Sh} = \frac{\mathbf{K}_{\mathbf{x}}\mathbf{l}}{\mathbf{D}_{\mathbf{AB}}}$$

$$Sc = \frac{\mu}{\rho D_{AB}}$$

$$\mathbf{St} = \frac{\mathbf{Sh}}{\mathbf{ReSc}}$$

$$\mathbf{J}_{\mathrm{D}} = \mathrm{St}(\mathrm{Sc})^{1/3}$$







### To determine empirical (statistical) relations between the adimensionnel numbers

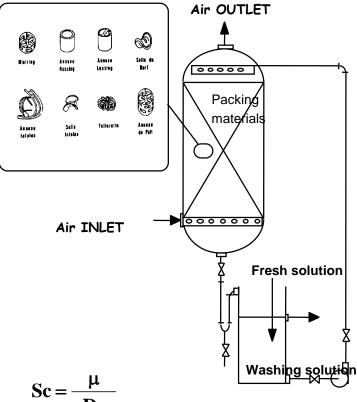
### Example: Packed fixed bed

$Re = 90 - 4\ 000$ $Sc = 0.6$	$\mathbf{J}_{\mathrm{D}} = \frac{2.06}{\varepsilon} \mathbf{R} \mathrm{e}^{-0.575}$
$Re = 5\ 000 - 10\ 300$ $Sc = 0.6$	$\mathbf{J}_{\mathrm{D}} = \frac{20.4}{\varepsilon}  \mathrm{Re}^{-0.815}$
Re = 0.0016 - 55 Sc = 168 - 70 600	$\mathbf{J}_{\mathrm{D}} = \frac{1.09}{\varepsilon} \mathrm{Re}^{-\frac{2}{3}}$
Re = 5 - 1 500 Sc = 168 - 70 600	$\mathbf{J}_{\mathrm{D}} = \frac{0.25}{\varepsilon} \mathbf{R} \mathrm{e}^{-0.31}$

$$\mathbf{J}_{\mathrm{D}} = \mathrm{St}(\mathrm{Sc})^{1/3}$$

$$Re = \frac{dU\rho}{\mu}$$

$$\mathbf{Sh} = \frac{\mathbf{K}_{\mathbf{x}}\mathbf{l}}{\mathbf{D}_{\mathbf{AB}}}$$



$$Sc = \frac{\mu}{\rho D_{AB}}$$







# To determine empirical (statistical) relations between the adimensionnel numbers

### Example: fluid and spherical particle

$$Sh = \left(4,0+1,21Pe^{2/3}\right)^{1/2}$$

$$Re = \frac{dU\rho}{\mu}$$
  $Sc = \frac{\mu}{\rho D_{SL}}$   $Sh = \frac{kd}{D_{SL}}$ 

$$Pe = \frac{dU}{D_{SL}} = \frac{dU\rho}{\mu} \frac{\mu}{\rho D_{SL}} = Re Sc$$







#### **BIBLIOGRAPHIE**

- ·Hirschfleder J.O., Bird R.B., Spotz E.L. (1949), Chem. Rev, 44, 205
- Perry R.H., Green D.W (1984), Perry's Chemical Engineers' Handbook, McGraw Hill, New York, NY, USA, 6<sup>th</sup> Edition
- •Treybal R.E. (1981), Mass transfer operations, Chemical Engineering Series, McGrawHill, USA
- ·Wilke C.R., Chang P. (1955), AIChE J., 1, 264
- ·Lieto J. (1998), Le génie chimique à l'usage des chimistes, Tec & Doc, Lavoisier, Paris