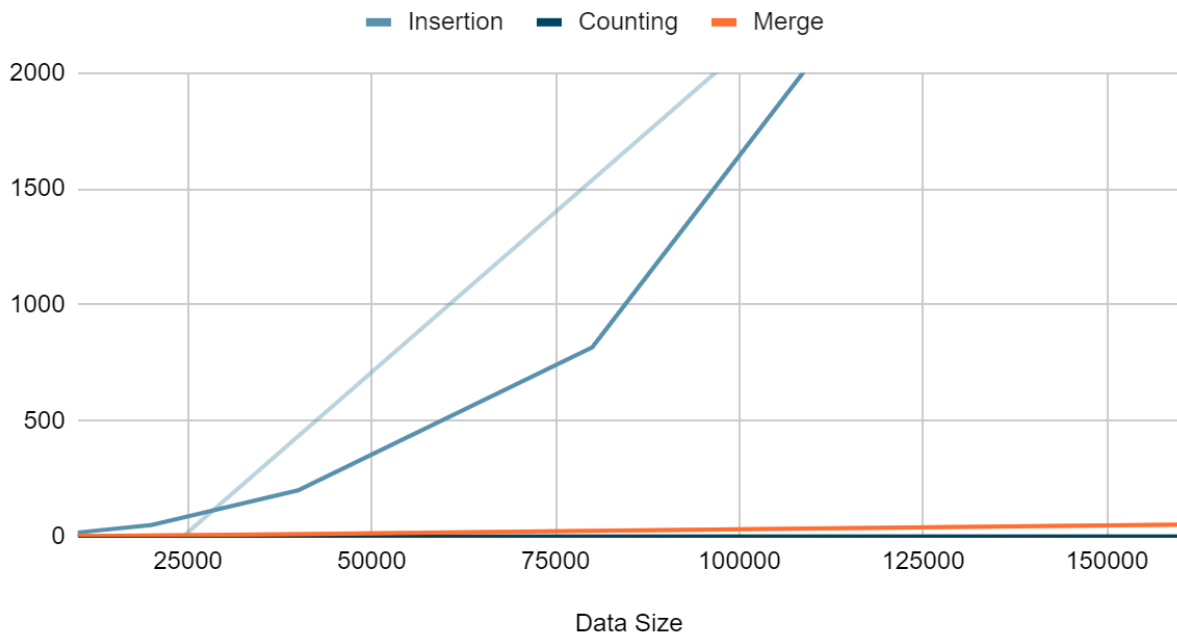


Task 1

Insertion, Counting and Merge

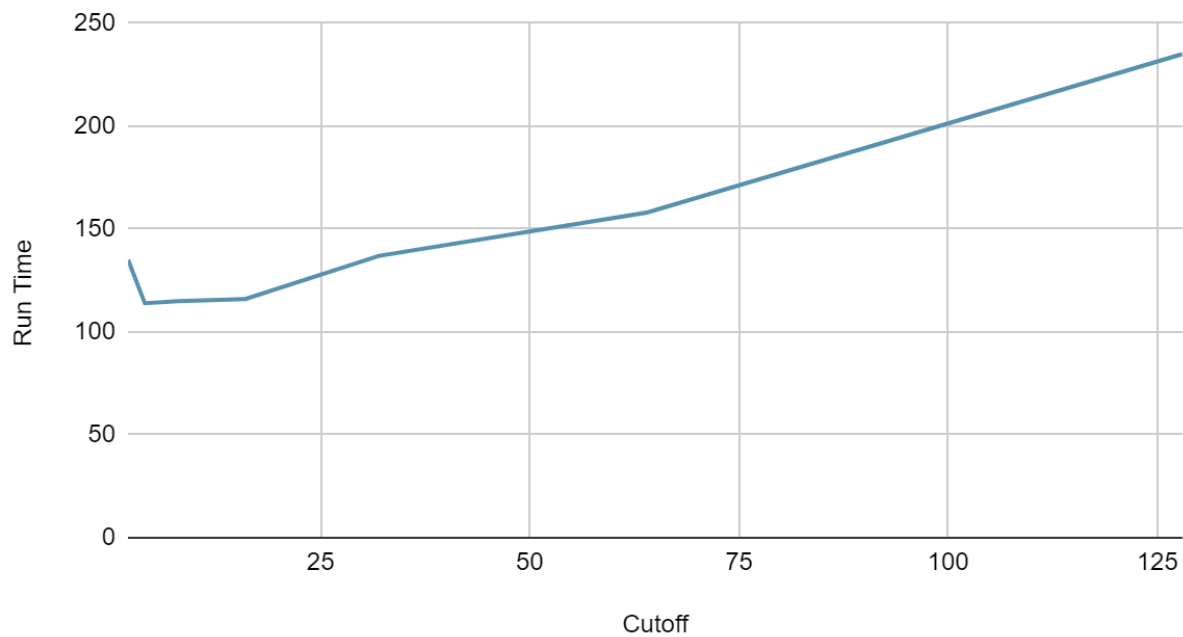


Conclusion:

The Insertion sort grows so much faster than the other two sorting methods, since the complexity of Insertion sort is $O(n^2)$ and the complexity of counting is $O(n)$ and merge sort is $O(n \log(n))$.

Task 2:

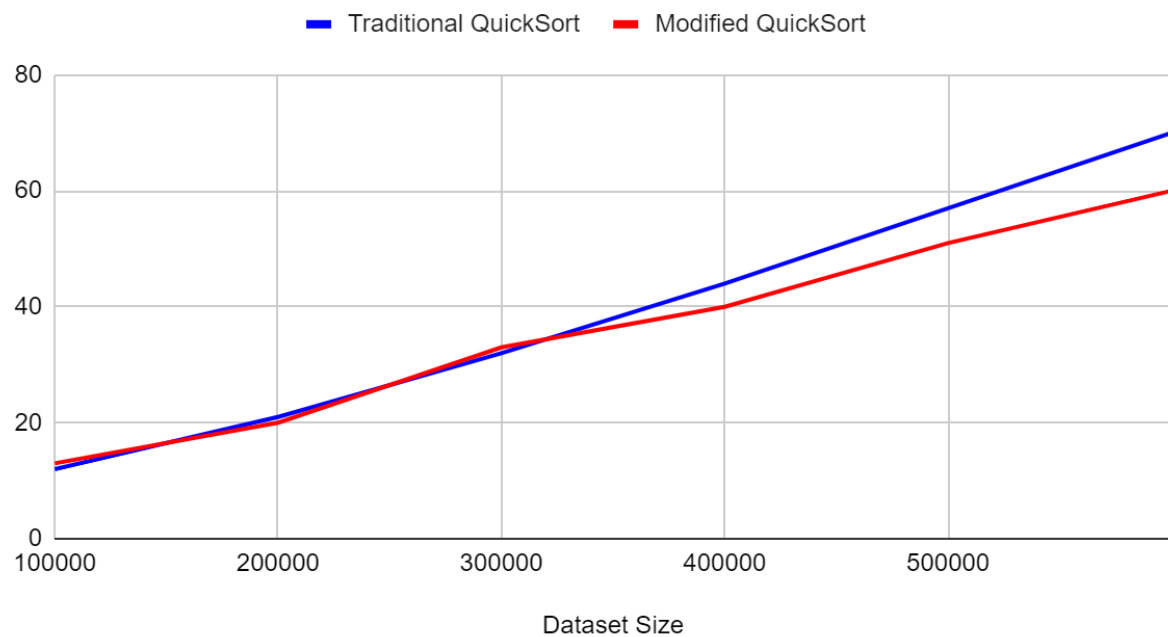
Run Time vs. Cutoff



The best cutoff is at 4.

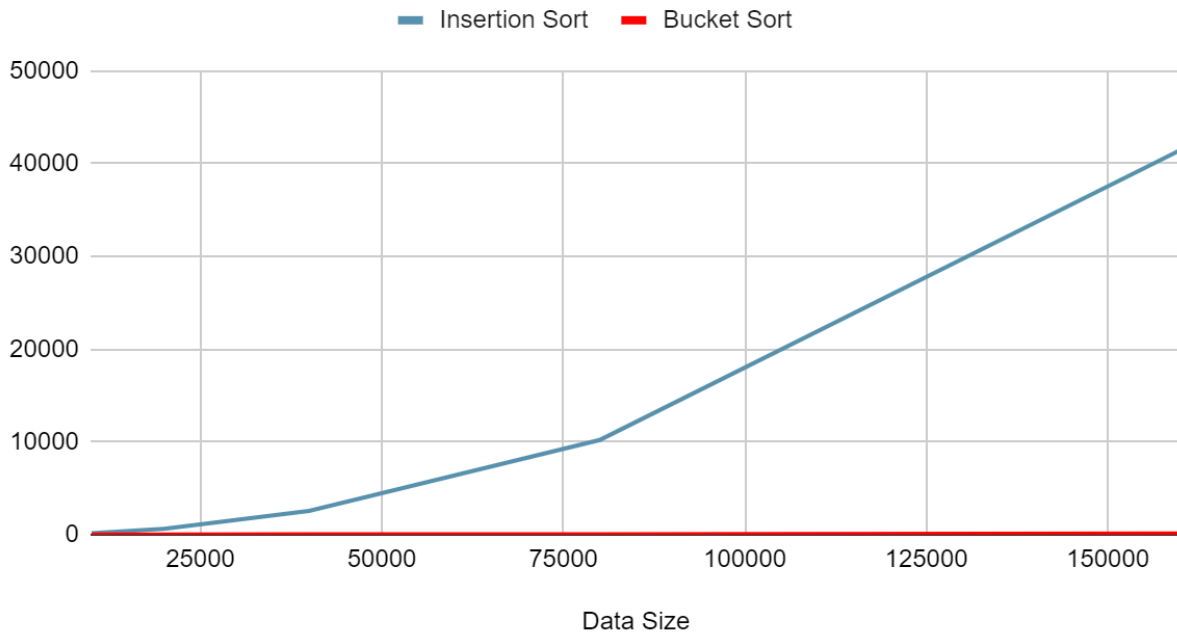
Task 3:

Traditional QuickSort and Modified QuickSort



Task 4:

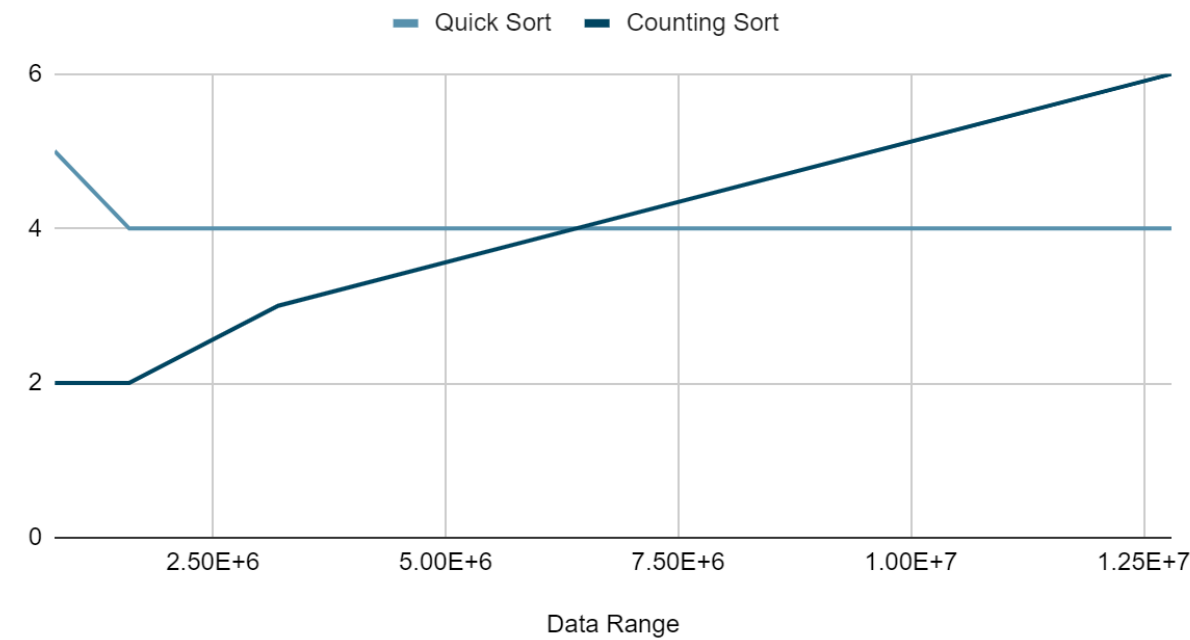
Insertion Sort and Bucket Sort



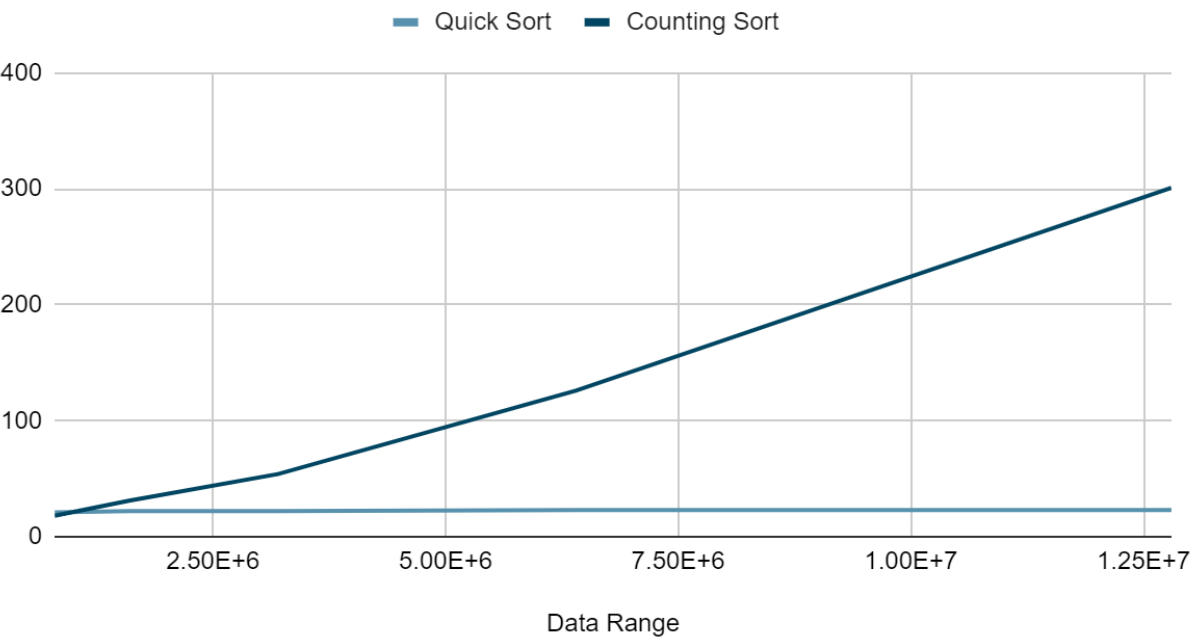
Since the complexity of insertion sort is $O(n^2)$ which is so much greater than bucket sort ($O(n)$). When n increases, the blue line increments so much more than the red line.

Task 5:

Size 50000, Quick Sort and Counting Sort



Size 200000, Quick Sort and Counting Sort



The range of data is completely uncorrelated to the running time of quick sort, since it treats every element as a byte. However, the running time of counting sort increases dramatically as the range of data increases. It is because the counting sort needs to create a new array with length of the maximum value of array.