Math 2153	Name:	Kunrad Gozun	
Midterm 1	OSU Username (name.nn):	90201.4	
Autumn 2025	Recitation Instructor:	Linus Ge	20
	Recitation Time:		

Instructions

- You have 50 minutes to complete this exam.
- This exam consists of 9 problems and 10 pages, including this cover sheet. Page 9 may be used for extra workspace and Page 10 has some formulas.
- If you wish to have any work on the extra workspace page considered for credit, indicate in the problem that there is additional work on the extra workspace page and clearly label to which problem the work belongs on the extra page.
- Please write clearly and make sure to justify your answers and show all relevant work! Correct answers with no supporting work may receive no credit. Your solutions should only use concepts and techniques covered in this course (up to this point in the course) or prerequisite courses.
- · Give exact answers unless instructed to do otherwise.
- Calculators of any kind are not permitted. No devices are permitted. Be sure all devices, including cell phones, smart
 watches, or other devices with internet capabilities are put away. You are not permitted to communicate with other
 people while taking this exam.

Improper Markings: Incomplete bubbles, x's, checkmarks, and other markings will not be recognized. Do not use these marks to indicate correct or incorrect answers.

- Acceptable Marking for selected answers:
- Acceptable Marking for unselected answers:
- Unacceptable Markings: (X) (•)
- 1. Fill in the circle next to the correct response. There is no partial credit and you do not need to show any work for this problem.

Q1: [2 pts each] Identity the following:

- a. マ・ロ+マ
- Scalar
- (B) Vector
- (C) Undefined

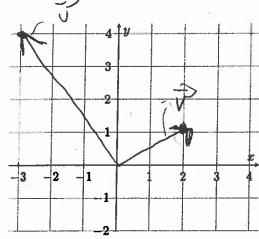
- b. $\overrightarrow{\mathbf{v}} \times \overrightarrow{\mathbf{u}} \times \overrightarrow{\mathbf{w}}$
- (A) Scalar
- (C) Undefined

Q2: True or False [2 pts each] Determine whether each statement below is true or false.

- If \overrightarrow{u} and \overrightarrow{v} are unit vectors, then $\overrightarrow{u} \times \overrightarrow{v}$ is a unit vector.
- If $\overrightarrow{\mathbf{u}}$ is a vector then $\overrightarrow{\mathbf{u}} \cdot \overrightarrow{\mathbf{u}} = |\overrightarrow{\mathbf{u}}|^2$. **(T)**
- The lines x = 3 + t, y = 4 + 2t, z = 2 t and x = 2t, y = 4t, z = t are parallel.
- It is possible for non-parallel lines to be non-intersecting in \mathbb{R}^3 . **(F)**
- If f_{xy} and f_{yx} are continuous then $f_{xy} = f_{yx}$. **(F)**
- If $\overrightarrow{u} \neq 0$ and $\overrightarrow{u} + \overrightarrow{v} = 0$, then \overrightarrow{u} and \overrightarrow{v} are parallel.

$$(2+4)-(1+2)j$$

2. [8 pts] Let $\vec{u} = -3\vec{i} + 4\vec{j}$ and $\vec{v} = 2\vec{i} + \vec{j}$. Sketch these vectors and compute $\text{proj}_{\vec{v}}\vec{u}$ and $\text{scal}_{\vec{v}}\vec{u}$.



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3. [8 pts] Find the parametric equation of the line segment joining (2,4,8) and (7,5,3).

4. [7 pts] Find both the parametric and vector equation of the line passing through (1, -3, 4) and parallel to the line x = 3 + 4t, y = 5 - t, z = 7.

$$\begin{array}{lll}
U_1 = (4, -1, 0) \\
U_2 = (3 - 1, 5 - -3, 7 - 4) \\
U_2 = (2, 5, 3) = |U_1 \times U_2| & |4 - 1 & 0| \\
V_2 = (2, 5, 3) = |U_1 \times U_2| & |2 & 5 & 3| \\
X = 1 - 3 + & |2 - 3 - 12 + & |2 - 3 \cap - 125 + 22 & |2 - 3 \cap - 125 + 22 & |2
\end{array}$$

5. [10 pts] Explain why the following limit does not exist at (0,0).

$$\lim_{(x,y)\to(0,0)} \frac{4x^2y}{3+xy^2}$$

$$\frac{1}{(x_{0},y_{0})} = \frac{4x^{2}y}{(x_{0},y_{0})} = \frac{4x^{2}(mx)}{x_{0}^{3}+x_{0}^{2}} = \frac{4x^{3}m}{x_{0}^{3}}$$

$$= \frac{1}{(x_{0},mx_{0})} = \frac{4x^{3}m^{2}}{x_{0}^{3}} = \frac{4x^{3}m^{2}}{x_{0}^{3}}$$

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6. [10 points] Find the area of a parallelogram with vertices (1,2,3),(1,0,6), and (4,2,4).

85 36

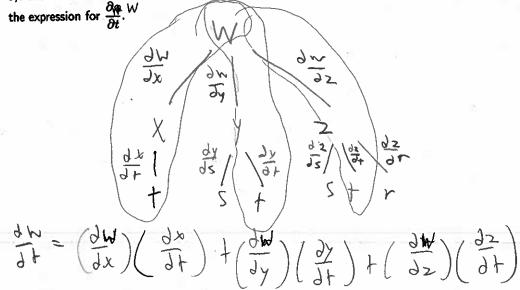
$$\overrightarrow{AB} = 20, -2, 3$$

$$= (-2-0) - (0-9) + (0-6)$$

$$= |-2^{2} + 9^{2} + 6^{2}|$$

$$= |-2^{2} + 9^{2} + 6^{2}|$$

7. a. [8 pts] Given that w = F(x, y, z), and x is a function of t and y is a function of s, t and z is a function of s, t and t. Sketch a Chain Rule tree diagram with branches labeled with the appropriate derivatives. Then write



b. [10 pts] Using chain rule find the following derivatives:

 z_s and z_t where $z = \sin(2x + y), x = s^2 - t^2$, and $y = s^2 + t^2$.

$$\frac{d^{2}}{ds} / \frac{d^{2}}{dy} = 2\cos(2x+y) \frac{d^{2}}{dy} = 2d$$

$$\frac{d^{3}}{ds} / \frac{dy}{dy} = -2d$$

$$\frac{d^{3}}{ds} / \frac{dy}{dy} = -2d$$

$$\frac{d^{2}}{ds} = (2\cos(2x+y))(-2d) + (\cos(2x+y))(2d)$$

$$= (2\cos(2(x+y))(-2d) + (\cos(2(x+y))(2d)$$

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8. [8 pts] Draw 3 level curves for the following function. Label the appropriate z values.

$$z = x + 2 - y^2; [-3, 3] \times [-5, 5]$$

$$\partial = \chi + 2 - \gamma^2$$

$$\gamma^2 = \chi + 2$$

$$x = 2$$
 $y^2 = \sqrt{4}$
 $y = 0$ $y^2 = \sqrt{2}$

9. [15 pts] Find a plane which contains the points (1,2,3), (-2,0,4), and (2,-1,-2). You may use the fact that these points are noncollinear. Write your answer in the form ax + by + cz = d.

$$AB = (2-2-1, 0-2, 4-3) \times (-3, -2, 1)$$

$$AB \times AC = 2-1, -1-2, -2-3) \times (-3, -3, -3)$$

$$AB \times AC = 2-1, -1-2, -2-3) \times (-3, -2, 1)$$

$$137 - 149 + 116$$

$$13(x-1) - 14(y-2) + 11(2-3) = 0$$

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 Extra Workspace

FORMULA SHEET

You may use the following results on the exam.

Some Values for the Trigonometric Functions

