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# AI1103 - Assignment 1

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### **PROBLEM**

2.12. In a school, there are 1000 students, out of which 430 are girls. It is known that out of 430, 10 percent of girls study in class XII. What is the probability that a student chosen randomly studies in Class XII given that the chosen student is a girl?

## **SOLUTION**

Total number of students: 1000 Total number of girls: 430

Total number of girls in Class XII: 10 % of total girls

$$= \frac{10}{100} \times 430 = 43 \tag{1}$$

Let  $X \in \{0, 1\}$  be the random variable such that 1 represents girl, 0 represents boy.

X	P(X)
1	430/1000
0	570/100

Let  $Y \in \{0,1\}$  be the random variable such that 1 represents chosen student is in Class XII, 0 represents chosen student is not in Class XII.

Y	P(Y)
1	$\frac{1}{2}$
0	$\frac{1}{2}$

Now,

$$P(Y=1|X=1) \tag{2}$$

$$= \frac{P(X=1|Y=1) \cdot P(Y=1)}{\sum_{i=0}^{1} P(X=1|Y=i) \cdot P(Y=i)}$$

$$= \frac{P(X=1|Y=1)P(Y=1)}{P(X=1|Y=0)P(Y=0) + P(X=1|Y=1)P(Y=1)}$$
(3)

TABLE III
PROBABILITY FOR DIFFERENT VALUES OF X,Y

Probability	Chosen Student	Value
P(X=1 Y=0)	girl not in Class XII	$\frac{387}{1000}$
P(X=1 Y=1)	girl in Class XII	$\frac{43}{1000}$

$$= \left[ \frac{\left(\frac{43}{1000} \times \frac{1}{2}\right)}{\left(\frac{387}{1000} \times \frac{1}{2}\right) + \left(\frac{43}{1000} \times \frac{1}{2}\right)} \right] \tag{4}$$

$$= \left[ \frac{\left(\frac{43}{1000}\right)}{\left(\frac{430}{1000}\right)} \right] \tag{5}$$

$$=\frac{1}{10}\tag{6}$$

Hence, the probability that a student chosen randomly studies in Class XII given that the chosen student is a girl is 0.1.