# World Final Template

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# 1 Polynomials

```
namespace polynomial {
    template <typename T>
     class dft {
       static const bool use_fast_trans = true;
       static void trans(std::vector<T>& p) {
         assert(__builtin_popcount(p.size()) == 1);
10
         if constexpr (use_fast_trans) {
11
          dif(p);
12
        } else {
13
          bit_reverse(p);
          dit(p);
14
15
16
17
       static void inv_trans(std::vector<T>& p) {
19
         assert(__builtin_popcount(p.size()) == 1);
20
         if constexpr (use_fast_trans) {
21
          dit(p);
22
        } else {
23
          trans(p);
^{24}
         reverse(p.begin() + 1, p.end());
25
26
        T inv = T(p.size()).inv();
27
         for (T& x : p) x *= inv;
28
29
30
       // should call dit after dif
       static void dit(std::vector<T>& p) {
32
        for (int len = 1; len < p.size(); len <<= 1) {</pre>
```

```
33
           auto sub_w = get_subw(len * 2);
34
           for (auto sub_p = p.begin(); sub_p != p.end(); sub_p += 2 * len)
35
             for (int i = 0; i < len; ++i) {</pre>
               T u = sub_p[i], v = sub_p[i + len] * sub_w[i];
               sub_p[i] = u + v;
38
               sub_p[i + len] = u - v;
39
41
43
       static void dif(std::vector<T>& p) {
44
         for (int len = p.size() / 2; len >= 1; len >>= 1) {
45
           auto sub_w = get_subw(len * 2);
46
           for (auto sub_p = p.begin(); sub_p != p.end(); sub_p += 2 * len)
47
             for (int i = 0; i < len; ++i) {</pre>
48
               T _sub_pi = sub_p[i];
49
               sub_p[i] += sub_p[i + len];
50
               sub_p[i + len] = (_sub_pi - sub_p[i + len]) * sub_w[i];
51
52
53
54
       typename std::vector<T>::iterator static get_subw(int len) {
56
57
         static std::vector<T> w = {0, 1};
         static const T primitive_root = T::primitive_root();
59
         while (w.size() <= len) {</pre>
          T e[] = {1, primitive_root.pow((T::modulus() - 1) / w.size())};
           w.resize(w.size() * 2);
           for (int i = w.size() / 2; i < w.size(); ++i) w[i] = w[i / 2] * e[i & 1];
63
64
         return w.begin() + len;
65
66
    };
     // poly.h
     template <typename T>
     class poly : public std::vector<T> {
71
72
       using std::vector<T>::vector;
73
       poly(std::string s) {
75
         for (int i = 0; i < s.size();) {</pre>
76
           auto scan_num = [&]() -> long long {
77
             int sgn = 1;
78
             if (s[i] == '-') sgn = -1, ++i;
79
             if (s[i] == '+') sgn = 1, ++i;
             if (i == s.size() || !std::isdigit(s[i])) return sgn;
81
             long long num = 0;
82
             while (i < s.size() && std::isdigit(s[i]))</pre>
83
               num = num * 10 + s[i++] - '0';
             return sgn * num;
```

```
85
 86
            auto add_item = [&](size_t exponent, T coeff) {
 87
             if (exponent >= this->size()) this->resize(exponent + 1);
 88
             this->at(exponent) = coeff;
 89
 90
           T coeff = scan_num();
 91
            if (i == s.size() || s[i] != 'x')
 92
              add_item(0, coeff);
 93
            else {
94
              size_t exponent = 1;
 95
              if (s[++i] == '^') {
 96
97
                exponent = scan_num();
 98
99
              add_item(exponent, coeff);
100
101
         }
102
       }
103
104
        int deg() const { return this->size() - 1; }
105
        poly operator-() const {
106
         poly ans = *this;
107
         for (auto& x : ans) x = -x;
108
         return ans:
109
110
        T operator()(const T& x) const {
111
112
          for (int i = this \rightarrow size() - 1; i \ge 0; --i) ans = ans * x + this \rightarrow at(i);
113
114
        T operator[](int idx) const {
115
116
         if (0 <= idx && idx < this->size()) return this->at(idx);
117
         return 0;
118
119
        T& operator[](int idx) {
120
         if (idx >= this->size()) this->resize(idx + 1);
121
         return this->at(idx);
122
123
        poly rev() const {
124
125
         poly res(*this);
          std::reverse(res.begin(), res.end());
126
127
          return res;
128
       }
129
        poly mulxk(size_t k) const {
130
131
         poly res = *this;
132
         res.insert(res.begin(), k, 0);
133
         return res:
134
135
        poly divxk(size_t k) const {
136
         if (this->size() <= k) return {};
```

```
137
          return poly(this->begin() + k, this->end());
138
139
        poly modxk(size_t k) const {
          k = std::min(k, this->size());
140
          return poly(this->begin(), this->begin() + k);
141
142
       }-
143
144
        poly& operator *= (poly p) {
145
          if (this->empty() || p.empty()) return *this = {};
146
          constexpr int small_size = 128;
          if (this->size() < small_size || p.size() < small_size) {</pre>
147
148
           poly<T> t(this->size() + p.size() - 1);
149
           for (int i = 0; i < this->size(); i++)
150
              for (int j = 0; j < p.size(); j++) t[i + j] += this->at(i) * p[j];
151
           return *this = t:
152
153
          int len = 1 << (std::__lg(this->deg() + p.deg()) + 1);
          this->resize(len);
154
          p.resize(len);
155
156
          dft<T>::trans(*this);
157
          dft<T>::trans(p);
158
          for (int i = 0; i < len; ++i) this->at(i) *= p[i];
159
          dft<T>::inv_trans(*this);
160
          return this->normalize():
161
162
163
        poly& operator+=(const poly& p) {
164
          this->resize(std::max(this->size(), p.size()));
165
          for (int i = 0; i < this->size(); ++i) this->at(i) += p[i];
166
          return this->normalize();
167
168
        poly& operator -= (const poly& p) {
169
          this->resize(std::max(this->size(), p.size()));
170
          for (int i = 0; i < this->size(); ++i) this->at(i) -= p[i];
171
          return this->normalize();
172
173
        poly& operator/=(const poly& p) {
174
          if (this->size() < p.size()) return *this = {};</pre>
175
          int len = this->size() - p.size() + 1;
176
          return *this = (this->rev().modxk(len) * p.rev().inv(len))
177
                             .modxk(len)
178
                             .rev()
179
                             .normalize();
180
        poly& operator%=(const poly& p) {
181
182
         return *this = (*this - (*this / p) * p).normalize();
183
184
        poly& operator*=(const T& x) {
185
          for (int i = 0; i < this->size(); ++i) this->at(i) *= x;
186
          return *this;
187
188
        poly& operator/=(const T& x) { return *this *= x.inv(); }
```

1 POLYNOMIALS

```
189
        poly operator*(const poly& p) const { return poly(*this) *= p; }
        poly operator+(const poly& p) const { return poly(*this) += p; }
190
        poly operator-(const poly& p) const { return poly(*this) -= p; }
191
        poly operator/(const poly& p) const { return poly(*this) /= p; }
192
        poly operator%(const poly& p) const { return poly(*this) %= p; }
193
194
        poly operator*(const T& x) const { return poly(*this) *= x; }
195
        poly operator/(const T& x) const { return poly(*this) /= x; }
196
197
        // (quotient, remainder)
198
        std::pair<poly, poly> divmod(const poly& p) const {
199
         poly d = *this / p;
         return std::make_pair(d, (*this - d * p).normalize());
200
201
202
203
        poly deriv() const {
204
         if (this->empty()) return {};
          poly res(this->size() - 1);
205
          for (int i = 0; i < this->size() - 1; ++i) {
206
           res[i] = this->at(i + 1) * (i + 1);
207
208
209
         return res;
210
       }
211
        poly integr(T c = 0) const {
212
         polv res(this->size() + 1):
213
         for (int i = 0; i < this->size(); ++i) {
214
           res[i + 1] = this->at(i) / (i + 1);
215
216
         res[0] = c;
217
          return res;
218
219
220
        // \mod x^k
221
        poly inv(int k = -1) const {
222
         if (!~k) k = this->size();
223
         poly res = {this->front().inv()};
224
         for (int len = 2; len < k * 2; len <<= 1) {
           res = (res * (poly{2} - this->modxk(len) * res)).modxk(len);
225
226
227
         return res.modxk(k);
228
^{229}
        // \mod x^k
230
        poly sqrt(int k = -1) const {
^{231}
232
         if (!~k) k = this->size();
233
          poly res = {this->at(0).sqrt()};
234
         for (int len = 2; len < k * 2; len <<= 1) {
235
           res = (res + (this->modxk(len) * res.inv(len)).modxk(len)) / 2;
236
         }
237
         return res.modxk(k);
^{238}
239
240
        // mod x^k, a0=1 should hold
```

```
241
        poly log(int k = -1) const {
242
          assert(this->at(0) == 1);
243
          if (!~k) k = this->size();
244
          return (this->deriv() * this->inv(k)).integr().modxk(k);
245
       // mod x^k, a0=0 should hold
246
247
        poly exp(int k = -1) const {
248
          assert(this->at(0) == 0);
249
          if (!~k) k = this->size();
250
          poly res = {1};
251
          for (int len = 2; len < k * 2; len <<= 1) {
252
           res = (res * (poly{1} - res.log(len) + this->modxk(len))).modxk(len);
253
254
          return res.modxk(k);
255
256
       // p^c \mod x^k
       poly pow(int c, int k = -1) const {
         if (!~k) k = this->size();
258
          int i = 0:
259
          while (i < this->size() && !this->at(i)) ++i;
261
          if (i == this->size() || 1LL * i * c >= k) return {};
262
          T ai = this->at(i);
263
          poly f = this->divxk(i) * ai.inv();
264
          return (f.log(k - i * c) * c).exp(k - i * c).mulxk(i * c) * ai.pow(c);
265
266
267
        // evaluate and interpolate
268
        struct product_tree {
269
270
          std::unique_ptrcproduct_tree> lson = nullptr, rson = nullptr;
271
          poly product;
272
          product_tree(int 1, int r) : 1(1), r(r) {}
273
274
          static std::unique_ptrproduct_tree> build(
275
              const std::vector<T>& xs, std::function<poly(T)> get_poly) {
276
            std::function<std::unique_ptr<pre>cproduct_tree>(int, int)> build =
277
                [&](int 1, int r) {
278
                  auto rt = std::make_uniquecproduct_tree>(1, r);
279
                  if (1 == r) {
280
                    rt->product = get_poly(xs[1]);
281
                  } else {
                    int mid = (1 + r) >> 1;
282
283
                    rt->lson = build(1, mid);
284
                    rt->rson = build(mid + 1, r);
285
                    rt->product = rt->lson->product * rt->rson->product;
286
287
                  return rt;
288
                };
289
            return build(0, xs.size() - 1);
290
291
       };
292
```

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```
293
        poly mulT(poly p) const {
294
         if (p.empty()) return {};
295
         return ((*this) * p.rev()).divxk(p.size() - 1);
296
297
298
        std::vector<T> evaluate(std::vector<T> xs) const {
299
         if (this->empty()) return std::vector<T>(xs.size());
300
          std::unique_ptrcproduct_tree> rt = product_tree::build(xs, [&](T x) {
301
           return poly{1, -x};
302
303
         return evaluate_internal(xs, rt);
304
305
306
        static poly interpolate(std::vector<T> xs, std::vector<T> ys) {
307
          assert(xs.size() == ys.size());
308
          if (xs.empty()) return {};
          std::unique_ptrcproduct_tree> rt = product_tree::build(xs, [&](T x) {
309
310
           return poly{1, -x};
311
312
          std::vector<T> coef = rt->product.rev().deriv().evaluate_internal(xs, rt);
313
          for (int i = 0; i < ys.size(); ++i) coef[i] = ys[i] * coef[i].inv();</pre>
314
          std::function<poly(product_tree*)> solve = [&](product_tree* rt) {
315
           if (rt->1 == rt->r) {
316
             return poly{coef[rt->1]};
317
           } else {
318
             return solve(rt->lson.get()) * rt->rson->product.rev() +
319
                     solve(rt->rson.get()) * rt->lson->product.rev();
320
           }
321
         };
322
         return solve(rt.get());
       }
323
324
325
       // a0=0 must hold
326
        poly cos(int k = -1) const {
327
         assert(this->at(0) == 0);
328
         if (!~k) k = this->size();
329
         T i = T::root().pow((T::modulus() - 1) / 4);
330
         poly x = *this * i;
         return (x.exp(k) + (-x).exp(k)) / 2;
331
332
333
       // a0=0 must hold
334
335
       poly sin(int k = -1) const {
336
         assert(this->at(0) == 0);
337
         if (!~k) k = this->size();
338
         T i = T::root().pow((T::modulus() - 1) / 4);
339
         poly x = *this * i;
340
         return (x.exp(k) - (-x).exp(k)) / (i * 2);
341
       }
342
343
        // a0=0 must hold
        poly tan(int k = -1) const { return this->sin(k) / this->cos(k); }
344
```

```
345
346
        poly acos(int k = -1) const {
347
          const poly& x = *this;
          return (-x.deriv() * (poly{1} - x * x).sqrt().inv()).integr();
348
349
        poly asin(int k = -1) const {
350
351
          const poly& x = *this;
352
          return (x.deriv() * (poly{1} - x * x).sqrt().inv()).integr();
353
       };
354
        poly atan(int k = -1) const {
355
          const poly& x = *this;
356
          return (x.deriv() * (poly{1} + x * x).inv()).integr();
357
358
359
        friend std::ostream& operator<<(std::ostream& os, poly p) {</pre>
360
          os << "{";
          for (auto x : p) os << x() << " ";
361
362
          os << "}";
363
          return os;
364
365
366
       private:
367
        poly& normalize() {
368
          while (this->size() && !this->back()) this->pop_back();
          return *this;
369
370
371
372
        std::vector<T> evaluate_internal(std::vector<T>& xs,
373
                                         std::unique_ptrrproduct_tree>& rt) const {
374
          std::vector<T> res(xs.size());
          xs.resize(std::max(xs.size(), this->size()));
375
376
          std::function<void(product_tree*, poly)> solve = [&](product_tree* rt,
377
                                                               poly p) {
378
           p = p.modxk(rt->r - rt->l + 1);
379
            if (rt->1 == rt->r) {
380
             if (rt->1 < res.size()) res[rt->1] = p.front();
381
           } else {
382
              solve(rt->lson.get(), p.mulT(rt->rson->product));
383
              solve(rt->rson.get(), p.mulT(rt->lson->product));
384
385
          solve(rt.get(), this->mulT(rt->product.inv(xs.size())));
386
387
          return res;
388
       }
389
390
391
     } // namespace polynomial
392
     using poly = polynomial::poly<zint>;
```

1 POLYNOMIALS

### 2 Strings

```
3
    namespace lyndon {
    std::vector<int> getfactorization(const std::string &s) {
      std::vector<int> right_ends;
      for (int i = 0; i < s.length();) {</pre>
       int j = i, k = i + 1;
9
       for (; k < s.length() && s[j] <= s[k]; j++, k++)
10
        if (s[j] < s[k]) j = i - 1;</pre>
11
        while (i <= j) i += k - j, right_ends.push_back(i);</pre>
12
13
      return right_ends;
14
15
16
    } // namespace lyndon
17
18
    19
20
    template <size_t alphabet_size = 26>
21
    class palindrome_automaton {
22
     public:
23
      struct node {
24
        std::array<int, alphabet_size> to;
25
        int link, len, count;
26
27
        explicit node(int len = 0) : len(len), link(-1), count(0) { to.fill(0); }
28
        explicit node(int len, int link) : len(len), link(link), count(0) {
29
         to.fill(0);
30
       }
      };
31
32
33
      palindrome_automaton() {
34
        int even_rt = newnode(0);
35
        int odd_rt = newnode(-1);
36
        nodes[even_rt].link = odd_rt;
37
        nodes[odd_rt].link = even_rt;
38
        last = even_rt;
39
40
41
      void extend(char c) {
42
        text.push_back(c);
43
        int i = text.size() - 1;
44
        auto getlink = [&](int u) {
45
         while (i - nodes[u].len - 1 < 0 || text[i - nodes[u].len - 1] != c) {</pre>
46
           u = nodes[u].link;
47
         }
48
         return u;
49
        };
```

```
50
         int w = c - 'a';
51
         int u = getlink(last);
 52
         if (!nodes[u].to[w]) {
53
           int v = newnode(nodes[u].len + 2, nodes[getlink(nodes[u].link)].to[w]);
54
           nodes[u].to[w] = v;
55
56
         last = nodes[u].to[w];
57
         ++nodes[last].count; // should be accomulated later from fail link tree
58
59
60
       std::string to_string() const {
61
         std::ostringstream os;
62
         std::function<void(int, std::string)> travel = [&](int k, std::string s) {
 63
           os << k << ": " << s << " ~ " << nodes[k].count << "\n";
64
 65
           for (int c = 0; c < alphabet_size; ++c)</pre>
             travel(nodes[k].to[c], std::string(1, c + 'a') + s + (char)(c + 'a'));
67
         };
68
         for (int c = 0; c < alphabet_size; ++c)</pre>
69
           travel(nodes[0].to[c], std::string(2, c + 'a'));
70
         for (int c = 0; c < alphabet_size; ++c)</pre>
71
           travel(nodes[1].to[c], std::string(1, c + 'a'));
72
         return os.str();
73
74
75
      private:
76
       int last:
77
       std::string text;
       std::vector<node> nodes;
79
80
       template <typename... Args>
 81
       int newnode(Args... args) {
 82
         int res = nodes.size();
 83
         nodes.push_back(node{args...});
 84
         return res;
 85
 86
 87
 88
      89
 90
     template <typename Container = std::vector<int>>
     struct SuffixArray {
91
92
       int n;
93
       Container s;
       // lc[0]=0 is meaningless
94
95
       std::vector<int> sa, rk, lc;
 96
       SuffixArray(const Container& s)
97
          : s(s), n(s.size()), sa(s.size()), rk(s.size()), lc(s.size()) {
98
         std::iota(sa.begin(), sa.end(), 0);
99
         std::sort(sa.begin(), sa.end(), [&](int a, int b) { return s[a] < s[b]; });
100
         rk[sa[0]] = 0;
101
         for (int i = 1; i < n; ++i)
```

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```
102
            rk[sa[i]] = rk[sa[i - 1]] + (s[sa[i]] != s[sa[i - 1]]);
103
          std::vector<int> tmp, cnt(n);
104
          tmp.reserve(n);
          for (int k = 1; rk[sa[n - 1]] < n - 1; k *= 2) {
105
106
107
           for (int i = 0; i < k; ++i) tmp.push_back(n - k + i);</pre>
108
           for (auto i : sa)
109
             if (i >= k) tmp.push_back(i - k);
110
           cnt.assign(n, 0);
           for (int i = 0; i < n; ++i) ++cnt[rk[i]];</pre>
111
            for (int i = 1; i < n; ++i) cnt[i] += cnt[i - 1];</pre>
112
113
           for (int i = n - 1; i >= 0; --i) sa[--cnt[rk[tmp[i]]]] = tmp[i];
114
            std::swap(rk, tmp);
115
            rk[sa[0]] = 0;
116
           for (int i = 1; i < n; ++i) {
             rk[sa[i]] = rk[sa[i - 1]];
117
118
              if (tmp[sa[i - 1]] < tmp[sa[i]] || sa[i - 1] + k == n ||</pre>
119
                  tmp[sa[i - 1] + k] < tmp[sa[i] + k])
                ++rk[sa[i]];
120
121
           }
         }
122
          for (int i = 0, j = 0; i < n; ++i) {
123
124
           if (!rk[i]) {
125
             j = 0;
           } else {
126
127
             if (j) --j;
128
              int k = sa[rk[i] - 1];
129
              while (i + j < n & k + j < n & k s[i + j] == s[k + j]) ++j;
130
              lc[rk[i]] = j;
131
132
133
134
135
      template <typename Container = std::vector<int>>
137
     class LongestCommonPrefix {
138
139
        LongestCommonPrefix(SuffixArray < Container > * sa) : sa(sa), st(sa -> lc) {}
140
141
        int lcp(int i, int j) {
142
         assert(0 <= i && i <= sa->n);
          assert(0 <= j && j <= sa->n);
143
         if (i == sa->n || j == sa->n) return 0;
144
145
          if (i == j) return sa->n - i;
          int 1 = sa->rk[i], r = sa->rk[i];
146
147
         if (1 > r) std::swap(1, r);
148
         return st.queryMin(l + 1, r);
149
       }
150
151
       private:
152
        SuffixArray < Container > * sa;
        SparseTable < int > st;
153
```

```
154
155
156
      157
     template <size_t alphabet_size = 26>
159
     class suffix_automaton {
160
      public:
161
       struct node {
         std::array<int, alphabet_size> to;
162
163
         int link, len, count;
164
165
         explicit node(int len = 0) : len(len), link(-1), count(0) { to.fill(-1); }
166
         explicit node(int len, int link, const std::array<int, alphabet_size>& to)
167
             : len(len), link(link), to(to), count(0) {}
168
       };
169
170
       suffix_automaton() : nodes() { newnode(); }
171
172
       explicit suffix_automaton(const std::string& s) : suffix_automaton() {
173
174
175
176
       void insert(const std::string& s) {
177
         nodes.reserve(size() + s.size() * 2):
         int last = 0;
178
179
         for (int i = 0; i < s.size(); ++i) {</pre>
180
           last = extend(last, s[i] - 'a');
181
      }
182
183
184
       int extend(int k. int c) {
         if (~nodes[k].to[c] && nodes[nodes[k].to[c]].len == nodes[k].len + 1) {
185
186
           return nodes[k].to[c];
187
188
         int leaf = newnode(nodes[k].len + 1);
         for (; ~k && !~nodes[k].to[c]; k = nodes[k].link) nodes[k].to[c] = leaf;
189
         if (!~k) {
190
191
           nodes[leaf].link = 0;
         } else {
192
193
           int p = nodes[k].to[c];
194
           if (nodes[k].len + 1 == nodes[p].len) {
195
             nodes[leaf].link = p;
196
197
             int np = newnode(nodes[k].len + 1, nodes[p].link, nodes[p].to);
             nodes[p].link = nodes[leaf].link = np;
198
199
             for (; ~k && nodes[k].to[c] == p; k = nodes[k].link)
200
               nodes[k].to[c] = np;
201
           }
202
         }
203
         return leaf;
204
205
```

2 STRINGS

```
206
        void build_ancestors() {
          for (int i = 1; i < size(); ++i) ancestors[i] = {nodes[i].link};</pre>
207
208
          for (int j = 1; (1 << j) < size(); ++j) {</pre>
           for (int i = 0; i < size(); ++i)
209
210
              if (~ancestors[i][i - 1]) {
211
                ancestors[i][j] = ancestors[ancestors[i][j - 1]][j - 1];
212
              } else {
213
                ancestors[i][j] = -1;
214
215
         }
216
217
218
        std::vector<int> mark_count(const std::string& s) {
^{219}
          std::vector<int> ends;
220
          int k = 0:
^{221}
          for (char c : s) {
222
           k = nodes[k].to[c - 'a'];
223
            assert(~k);
224
            ends.push_back(k);
225
            ++nodes[k].count;
226
227
          return ends;
228
229
^{230}
        void addup_count() {
231
          std::vector<int> ids(size()), bucket(size());
232
          for (int i = 0; i < size(); ++i) ++bucket[nodes[i].len];</pre>
233
          for (int i = 1; i < bucket.size(); ++i) bucket[i] += bucket[i - 1];</pre>
234
          for (int i = 0; i < size(); ++i) ids[--bucket[nodes[i].len]] = i;</pre>
          for (int i = size() - 1; i; --i)
235
236
            nodes[nodes[ids[i]].link].count += nodes[ids[i]].count;
237
       }-
238
239
        const node& operator[](int v) const { return nodes[v]; }
240
        int maxlen(int v) const { return nodes[v].len; }
^{241}
242
^{243}
        int minlen(int v) const { return v ? nodes[nodes[v].link].len + 1 : 0; }
244
245
        int size() const { return nodes.size(); }
^{246}
        std::string to_string() const {
247
248
          std::ostringstream os;
249
          std::function < void(int, std::string) > travel = [&](int k, std::string s) {
250
            if (!~k) return;
            os << k << ": " << s << " ~ " << nodes[k].count << "\n";
251
252
            for (int c = 0; c < alphabet_size; ++c)</pre>
253
              travel(nodes[k].to[c], s + (char)(c + 'a'));
254
         };
255
          travel(0, "");
256
          return os.str();
257
```

```
258
259
      private:
260
       std::vector<node> nodes;
261
       std::vector<std::vector<int>> ancestors;
262
263
       template <typename... Args>
264
       int newnode(Args... args) {
265
         int res = nodes.size();
266
         nodes.push_back(node{args...});
267
         return res;
268
269
270
271
      //*********************** A Cauto *************************
272
273
     int go[maxtri][26], sum, count[maxtri], d[maxtri], fail[maxtri];
     void make_tri(int k) {
275
         fo(i,0,nb-1) {
276
             int index=sb[i]-'a';
277
             if (!go[k][index]) go[k][index]=++sum;
278
             k=go[k][index];
279
         }
280
         count[k]++;
281
282
     void make_fail() {
283
         int i=0, j=0;
284
         fo(p,0,25) if (go[0][p]) d[++j]=go[0][p];
285
         while (i++<j) {
286
             int now=d[i];
             fo(p,0,25) if (go[now][p]) {
287
288
                int son=go[now][p];
289
                fail[son]=go[fail[now]][p];
290
                 count[son]+=count[fail[son]];
291
                d[++j]=son;
292
             } else go[now][p]=go[fail[now]][p];
293
294
     void find(int k) { //sa中出现了多少次sb
295
296
         fo(i,1,n) ans+=count[k=go[k][sa[i]-'a']];
297
298
     300
301
     int f[2*maxn];
     void manacher()
302
303
     ·
304
         int lim=0, mid=0;
305
         fo(i,1,m) // m=2*n+1
306
307
             f[i]= (i<=lim) ?min(f[mid*2-i],lim-i+1) :1;
308
             while (i-f[i]>0 && i+f[i]<=m && s[i-f[i]]==s[i+f[i]]) f[i]++;
309
             if (i+f[i]-1>lim) lim=i+f[i]-1, mid=i;
```

2 STRINGS

```
310
311
312
     313
314
315
     int next[maxn],ex[maxn];
316
     void exkmp() {
317
        next[1]=nb;
        int k=0;
318
319
        fo(i,2,nb) {
            int lim=k+next[k]-1, L=next[i-k+1];
320
321
            if (i+L<=lim) next[i]=L; else {</pre>
322
               next[i]=max(lim-i+1,0);
323
               while (i+next[i] <= nb && sb[i+next[i]] == sb[1+next[i]]) next[i] ++;</pre>
324
325
           }
326
        }
327
328
        k=1;
329
        fo(i,1,na) {
330
            int lim=k+ex[k]-1, L=next[i-k+1];
331
            if (i+L<=lim) ex[i]=L; else {</pre>
332
               ex[i]=max(lim-i+1,0);
333
               while (i+ex[i] <= na && 1+ex[i] <= nb && sa[i+ex[i]] == sb[1+ex[i]]) ex[i] ++;
334
               k=i;
335
336
337
338
339
     340
341
342
     int min_representation(int *s,int len) { // index from 0
343
        int i=0, j=1;
344
        while (i<len && j<len) {
345
            int k=0;
346
            for(; k<len && s[(i+k)%len]==s[(j+k)%len]; k++);</pre>
347
            if (k==len) break;
            (s[(i+k)\%len] < s[(j+k)\%len]) ?j+=k+1 :i+=k+1;
348
349
            i+=(i==j);
350
351
        return min(i,j);
352 }
```

## 3 Geometry

```
1 namespace geometry2d {
2
```

```
constexpr long double eps = 1e-7;
     constexpr long double pi = std::acos(-1);
     int fsign(long double x) { return (x > eps) - (x < -eps); }</pre>
     long double sqr(long double x) { return x * x; }
 9
     //Ax^2+Bx+c=0
10
     std::vector<long double > solveEquationP2(long double A, long double B,
                                               long double C) {
11
       long double delta = B * B - 4 * A * C;
12
       if (fsign(delta) < 0) return {};</pre>
13
       if (fsign(delta) == 0) return {-0.5 * B / A};
14
15
       long double sqrt_delta = std::sqrt(delta);
16
       long double x1 = -0.5 * (B - sqrt_delta) / A,
17
                   x2 = -0.5 * (B + sqrt_delta) / A;
18
       if (fsign(x1 - x2) > 0) std::swap(x1, x2);
19
       return {x1, x2};
20
21
22
23
     struct Point3D {
24
       long double x, y, z;
25
26
       explicit Point3D(long double x = 0, long double y = 0, long double z = 0)
27
           : x(x), y(y), z(z) {}
28
29
       explicit Point3D(const Point& p);
30
31
       Point3D operator-(const Point3D& p) const {
32
         return Point3D(x - p.x, y - p.y, z - p.z);
33
34
       long double innerProd(const Point3D& p) const {
35
         return x * p.x + y * p.y + z * p.z;
36
37
       Point3D crossProd(const Point3D& p) const {
         return Point3D(y * p.z - z * p.y, -x * p.z + z * p.x, x * p.y - y * p.x);
38
39
40
     };
41
42
     struct Point {
43
       long double x, y;
       explicit Point(long double x = 0, long double y = 0) : x(x), y(y) {}
44
       Point operator+(const Point& p) const { return Point(x + p.x, y + p.y); }
45
46
       Point operator-(const Point& p) const { return Point(x - p.x, y - p.y); }
       Point operator/(const long double& 1) const { return Point(x / 1, y / 1); }
47
48
       Point operator*(const long double& 1) const { return Point(x * 1, y * 1); }
49
       Point unit() const {
50
         long double 1 = len();
51
         assert(fsign(1) > 0);
52
         return *this / 1;
53
       long double crossProd(const Point& p) const { return x * p.y - y * p.x; }
```

8

3 GEOMETRY

```
long double innerProd(const Point& p) const { return x * p.x + y * p.y; }
        long double lenSqr() const { return sqr(x) + sqr(y); }
 56
 57
        long double len() const { return std::sqrt(lenSqr()); }
        long double distanceSqr(const Point& p) const {
 58
 59
          return sqr(x - p.x) + sqr(y - p.y);
 60
 61
        long double distance(const Point& p) const {
 62
         return std::sqrt(distanceSqr(p));
 63
        long double angleWith(const Point& p) const {
 64
         return std::atan2(crossProd(p), innerProd(p));
 65
 66
 67
        // return (-pi, pi]
        long double angle() const { return std::atan2(y, x); }
 69
        int angleSign() const {
 70
         if (!y) return fsign(x) < 0;</pre>
          return fsign(y);
 71
 72
 73
        Point rotate90() const { return Point(-y, x); }
 74
 75
        static long double crossProd(const Point& o, const Point& a, const Point& b) {
         return (a - o).crossProd(b - o);
 76
 77
 78
        static long double innerProd(const Point& o. const Point& a. const Point& b) {
 79
          return (a - o).innerProd(b - o);
 80
 81
 82
        friend std::ostream& operator<<(std::ostream& os, Point p) {</pre>
 83
         return os << "(" << p.x << "," << p.y << ")";
 84
 85
 86
        friend bool operator == (const Point& lhs, const Point& rhs) {
 87
         return !fsign(lhs.x - rhs.x) && !fsign(lhs.y - rhs.y);
 88
 89
 90
        struct HorizontalComparer {
 91
         bool operator()(const Point& lhs, const Point& rhs) const {
 92
           return lhs.x < rhs.x || (lhs.x == rhs.x && lhs.y < rhs.y);
 93
 94
        };
 95
        struct PolarComparer {
 96
 97
          bool operator()(const Point& lhs, const Point& rhs) const {
98
            int angleSign_diff = lhs.angleSign() - rhs.angleSign();
            if (angleSign_diff) return angleSign_diff < 0;</pre>
 99
100
            int crossProd_sign = fsign(lhs.crossProd(rhs));
101
            if (crossProd_sign) return crossProd_sign > 0;
102
            return lhs.lenSqr() < rhs.lenSqr();</pre>
103
104
        };
105
106
```

```
107
      Point3D::Point3D(const Point& p) : Point3D(p.x, p.y, p.x * p.x + p.y * p.y) {}
108
109
      struct Line {
110
       Point pivot, unit_direction;
111
        Line(Point pivot, Point direction)
112
            : pivot(pivot), unit_direction(direction.unit()) {}
113
        long double angle() const { return unit_direction.angle(); }
        // 1: on the left
        // 0: in the line
115
        // -1: on the right
        int side(const Point& p) {
          return fsign(unit_direction.crossProd(p - pivot));
118
119
120
        bool isParallel(const Line& 1) {
121
          return fsign(unit_direction.crossProd(l.unit_direction)) == 0;
122
123
        bool isSame(const Line& 1) {
124
          return isParallel(1) &&
125
                 fsign(unit_direction.crossProd(l.pivot - pivot)) == 0;
126
127
        bool isSameDirection(const Line& 1) {
          return isParallel(1) &&
128
129
                 fsign(unit_direction.innerProd(l.unit_direction)) > 0;
130
        Point intersection(const Line& 1) {
131
132
          assert(!isParallel(1));
133
          return pivot + unit_direction *
134
                             (l.unit_direction.crossProd(l.pivot - pivot)) /
135
                             1.unit_direction.crossProd(unit_direction);
136
137
138
        friend std::ostream& operator << (std::ostream& os, Line 1) {
139
          return os << "(" << l.pivot << "," << l.unit_direction << ")";
140
141
142
143
      struct Segment {
144
        Point a, b;
        Segment(Point a, Point b) : a(a), b(b) {}
145
146
        bool hasIntersection(const Segment& s) const {
147
          return fsign(Point::crossProd(a, b, s.a)) *
148
                         fsign(Point::crossProd(a, b, s.b)) <
149
150
                 fsign(Point::crossProd(s.a, s.b, a)) *
151
                         fsign(Point::crossProd(s.a, s.b, b)) <
152
                     0:
153
154
        bool isPointIn(const Point& p) const {
155
          return fsign(Point::innerProd(p, a, b)) <= 0 &&
156
                 fsign(Point::crossProd(p, a, b)) == 0;
157
158
```

```
159
        Point lerp(const long double& ratio) const { return a + (b - a) * ratio; }
160
161
       friend std::ostream& operator << (std::ostream& os, Segment s) {
         return os << "(" << s.a << "," << s.b << ")";
162
163
164 };
165
166
     struct Polygon {
167
        static bool isConvexInCCW(const std::vector<Point>& p) {
168
          for (int i = 0; i < p.size(); ++i) {</pre>
           int l = (i + p.size() - 1) % p.size();
169
170
           int r = (i + 1) % p.size();
171
           if (Point::crossProd(p[i], p[1], p[r]) > 0) return false;
172
173
          return true:
174
175
        static std::vector<int> convexHullId(const std::vector<Point>& p) {
          if (p.size() == 0) return {};
176
          if (p.size() == 1) return {0};
177
178
          std::vector<int> ids(p.size());
179
          std::iota(ids.begin(), ids.end(), 0);
180
          sort(ids.begin(), ids.end(),
181
               [&, comp = Point::HorizontalComparer()](int i, int j) {
182
                 return comp(p[i], p[j]);
               });
183
184
          std::vector<int> res;
185
          for (int i : ids) {
186
            while (res.size() > 1 &&
187
                  fsign(Point::crossProd(p[res.end()[-2]], p[res.end()[-1]],
                                         p[i])) <= 0)
188
189
             res.pop_back();
190
           res.push_back(i);
191
         }
192
          ids.pop_back();
193
          std::reverse(ids.begin(), ids.end());
194
          int lower_size = res.size();
195
          for (int i : ids) {
196
            while (res.size() > lower_size &&
                  fsign(Point::crossProd(p[res.end()[-2]], p[res.end()[-1]],
197
198
                                         p[i])) <= 0)
199
             res.pop_back();
           res.push_back(i);
200
201
202
          res.pop_back();
203
          return res;
204
205
        static std::vector<Point> convexHullPoint(const std::vector<Point>& p) {
206
          std::vector<int> ids = convexHullId(p);
207
          std::vector<Point> res:
208
          for (int i : ids) res.push_back(p[i]);
209
          return res;
210
```

```
211
212
        // should be guaranteed that convex is a convex hull in cww
213
        static bool isPointInConvexCCW(const Point& p,
214
                                       const std::vector<Point>& convex) {
215
          assert(Polygon::isConvexInCCW(convex));
216
          for (int i = 0; i < convex.size(); ++i) {</pre>
217
            Point a = convex[i];
218
            Point b = convex[(i + 1) % convex.size()];
219
           if (Point::crossProd(a, b, p) < 0) return false;</pre>
220
221
          return true;
222
223
     };
224
225
     struct Circle {
226
        Point o;
        long double r;
        Circle() : Circle(Point(0, 0), 0) {}
228
        Circle(Point o, long double r) : o(o), r(r) {}
229
        Point pointInDirection(long double angle) {
231
          return Point(o.x + r * std::cos(angle), o.y + r * std::sin(angle));
232
233
234
        std::vector<Point> intersection(const Line& 1) const {
235
          long double A = 1;
236
          long double B = 1.unit_direction.innerProd(1.pivot - o) * 2;
237
          long double C = o.distanceSqr(l.pivot) - sqr(r);
238
          std::vector<long double> roots = solveEquationP2(A, B, C);
239
          std::vector<Point> intersects;
240
          for (long double x : roots)
241
            intersects.push_back(1.pivot + 1.unit_direction * x);
242
          return intersects;
243
244
        std::vector<Point> intersection(const Segment& s) const {
245
          std::vector<Point> line_intersects = intersection(Line(s.a, s.b - s.a));
246
          std::vector<Point> intersects;
247
          for (const Point& p : line_intersects)
248
           if (s.isPointIn(p)) {
249
              intersects.push_back(p);
250
251
          return intersects;
252
253
254
        // triangle oab
255
        long double overlapAreaWithTriangle(const Point& a, const Point& b) const {
256
          if (!fsign(Point::crossProd(o, a, b))) return 0;
257
          std::vector<Point> key_points;
258
          key_points.push_back(a);
259
          for (const Point& p : intersection(Segment(a, b))) key_points.push_back(p);
260
          key_points.push_back(b);
261
          long double res = 0;
262
          for (int i = 1; i < key_points.size(); ++i) {</pre>
```

```
263
            Point mid_point = (key_points[i - 1] + key_points[i]) / 2;
            Point ray1 = key_points[i - 1] - o;
264
265
            Point ray2 = key_points[i] - o;
            if (o.distanceSqr(mid_point) <= sqr(r)) {</pre>
266
267
              res += std::abs(ray1.crossProd(ray2));
268
           } else {
269
              res += sqr(r) * std::abs(ray1.angleWith(ray2));
270
^{271}
         }
272
          dbg(a, b, key_points, res);
273
         return 0.5 * res;
274
275
276
        long double overlapAreaWithPolygon(const std::vector<Point>& p) const {
277
         long double res = 0;
^{278}
          for (int i = 0; i < p.size(); ++i) {</pre>
279
           int j = (i + 1) % p.size();
280
            res += overlapAreaWithTriangle(p[i], p[j]) *
281
                   fsign(Point::crossProd(o, p[i], p[j]));
282
283
          dbg(res);
284
         return res;
285
286
287
        // 1: outside
288
        // 0: edge
289
        // -1: inside
        // equal to solving following determinant (a,b,c is counter-clockwise)
290
        // | ax, ay, ax^2+ay^2, 1 |
        // | bx, by, bx^2+by^2, 1 |
292
293
        // | cx, cy, cx^2+cy^2, 1 |
294
        // | px, py, px^2+py^2, 1 |
295
        static int side(const Point& a, Point b, Point c, const Point& p) {
296
         if (fsign(Point::crossProd(a, b, c)) < 0) std::swap(b, c);</pre>
297
         Point3D a3(a), b3(b), c3(c), p3(p);
298
         b3 = b3 - a3;
299
          c3 = c3 - a3:
300
          p3 = p3 - a3;
         Point3D f = b3.crossProd(c3);
301
302
          return fsign(p3.innerProd(f));
303
304
305
        friend std::ostream& operator<<(std::ostream& os, const Circle& c) {
306
          return os << "(" << c.o << "," << c.r << ")";
307
308
     };
309
310
     // return the intersection convex in ccw, should be guaranteed that the
      // intersection is finite.
311
312
     struct HalfPlaneIntersection {
313
        static std::vector<Point> solve(std::vector<Line> lines) {
314
          sort(lines.begin(), lines.end(),
```

```
315
                [comp = Point::PolarComparer()](auto 11, auto 12) {
316
                 if (11.isSameDirection(12)) {
317
                    return 11.side(12.pivot) < 0;</pre>
318
319
                    return comp(11.unit_direction, 12.unit_direction);
320
               });
321
322
323
          std::deque<Line> key_lines;
324
          std::deque<Point> key_points;
          for (int i = 0; i < lines.size(); ++i) {</pre>
325
326
            if (i > 0 && lines[i - 1].isSameDirection(lines[i])) continue;
327
            while (key_points.size() && lines[i].side(key_points.back()) <= 0) {</pre>
328
               key_lines.pop_back();
329
               key_points.pop_back();
330
331
             while (key_points.size() && lines[i].side(key_points.front()) <= 0) {</pre>
332
              key_lines.pop_front();
333
               key_points.pop_front();
334
335
            if (key_lines.size()) {
336
              // since it's guaranteed that the intersection is finite, therefore must
337
338
              if (lines[i].isParallel(key_lines.back())) return {};
339
              key_points.push_back(lines[i].intersection(key_lines.back()));
340
341
            key_lines.push_back(lines[i]);
342
343
344
          while (key_points.size() &&
345
                 key_lines.front().side(key_points.back()) <= 0) {</pre>
346
            key_lines.pop_back();
347
            key_points.pop_back();
348
349
350
          if (key_lines.size() <= 2) return {};</pre>
351
352
          std::vector<Point> convex;
353
          for (int i = 0; i < key_lines.size(); ++i)</pre>
354
            convex.emplace_back(
355
                \label{lines} \verb|key_lines[i]|.intersection(key_lines[(i + 1) % key_lines.size()])); \\
356
          return convex;
357
358
     };
359
360
      struct Triangulation {
361
        struct Edge {
362
363
          std::list<Edge>::iterator rev;
364
          Edge(int v = 0) : v(v) {}
365
366
        // delaunay triangulation
```

```
367
        // should be guaranteed that all points are pairwise distinct
368
        static std::vector<std::pair<int, int>> nearest(const std::vector<Point>& p) {
369
          std::vector<std::list<Edge>> neighbor(p.size());
370
          std::vector<int> id(p.size());
          std::iota(id.begin(), id.end(), 0);
371
372
          std::sort(id.begin(), id.end(),
373
                    [&, comp = Point::HorizontalComparer()](int i, int j) {
374
                      return comp(p[i], p[j]);
375
                    });
376
          auto addedge = [&](int u, int v) {
377
378
            neighbor[u].push_front(v);
379
            neighbor[v].push_front(u);
380
            neighbor[u].front().rev = neighbor[v].begin();
381
            neighbor[v].front().rev = neighbor[u].begin();
382
          };
383
          std::function<void(int, int)> divide = [&](int 1, int r) {
384
            if (r - 1 + 1 <= 3) {
385
              for (int i = 1; i <= r; ++i)</pre>
386
                for (int j = 1; j < i; ++j) addedge(id[i], id[j]);</pre>
387
              return;
388
            }
389
390
            int mid = (1 + r) >> 1:
391
            divide(1, mid);
392
            divide(mid + 1, r);
393
394
            auto get_base_LR_edge = [&]() {
395
              std::vector<int> stk;
396
              for (int i = 1; i <= r; ++i) {
397
                while (stk.size() >= 2 &&
398
                       fsign(Point::crossProd(p[id[stk.end()[-2]]],
399
                                              p[id[stk.end()[-1]]], p[id[i]])) < 0)
400
                  stk.pop_back();
401
                stk.push_back(i);
402
403
              for (int i = 1; i < stk.size(); ++i)</pre>
404
                if (stk[i - 1] <= mid && stk[i] > mid)
405
                  return std::make_pair(id[stk[i - 1]], id[stk[i]]);
406
            };
407
            auto [ld, rd] = get_base_LR_edge();
408
409
410
            while (true) {
411
              addedge(ld, rd);
412
              Point ptL = p[ld], ptR = p[rd];
413
              int ch = -1, side = -1;
414
              for (auto it = neighbor[ld].begin(); it != neighbor[ld].end(); ++it) {
415
                if (fsign(Point::crossProd(ptL, ptR, p[it->v])) > 0 &&
416
                    (!~ch || Circle::side(ptL, ptR, p[ch], p[it->v]) < 0)) {
417
                  ch = it -> v;
418
                  side = 0;
```

```
419
420
421
              for (auto it = neighbor[rd].begin(); it != neighbor[rd].end(); ++it) {
422
                if (fsign(Point::crossProd(ptR, p[it->v], ptL)) > 0 &&
423
                    (!~ch || Circle::side(ptL, ptR, p[ch], p[it->v]) < 0)) {
424
                  ch = it -> v:
425
                   side = 1;
426
427
428
              if (!~ch) break;
              assert(side == 0 || side == 1);
429
430
              if (!side) {
431
                for (auto it = neighbor[ld].begin(); it != neighbor[ld].end();) {
432
                  if (Segment(ptL, p[it->v]).hasIntersection(Segment(ptR, p[ch]))) {
433
                    neighbor[it->v].erase(it->rev);
434
                    neighbor[ld].erase(it++);
435
                  } else {
436
                    ++it;
437
438
439
                ld = ch;
              } else {
440
441
                for (auto it = neighbor[rd].begin(); it != neighbor[rd].end();) {
442
                  if (Segment(ptR, p[it->v]).hasIntersection(Segment(ptL, p[ch]))) {
                    neighbor[it->v].erase(it->rev);
443
444
                    neighbor[rd].erase(it++);
445
                  } else {
446
                    ++it;
447
448
449
                rd = ch:
450
451
           }
452
          };
453
454
          divide(0, p.size() - 1);
455
456
          std::vector<std::pair<int, int>> edges;
457
          for (int u = 0; u < p.size(); ++u)</pre>
458
            for (auto e : neighbor[u])
459
              if (u < e.v) edges.emplace_back(u, e.v);</pre>
460
          return edges;
461
       }
462
        // should be quaranteed that p is strictly convex
463
464
        static std::vector<std::pair<int, int>> furthest(
465
            const std::vector<Point>& p) {
466
          assert(Polygon::isConvexInCCW(p));
467
          std::vector<std::pair<int, int>> edges;
468
          if (p.size() < 3) {</pre>
469
            for (int i = 0; i < p.size(); ++i)</pre>
470
              for (int j = 0; j < i; ++j) {</pre>
```

```
471
                edges.emplace_back(i, j);
472
473
            return edges;
474
          }
475
476
          std::vector<std::list<Edge>> neighbor(p.size());
477
          std::vector<int> ids(p.size());
478
          std::iota(ids.begin(), ids.end(), 0);
479
480
          // calculate cw, ccw
          std::vector<int> cw(p.size()), ccw(p.size());
481
482
          for (int i = 0; i < p.size(); ++i) {</pre>
483
            cw[i] = (i + p.size() - 1) % p.size();
484
            ccw[i] = (i + 1) % p.size();
485
486
          std::random_shuffle(ids.begin(), ids.end());
487
          for (int i = ids.size() - 1; i >= 2; --i) {
488
            int u = ids[i];
            std::tie(ccw[cw[u]], cw[ccw[u]]) = std::make_pair(ccw[u], cw[u]);
489
490
491
492
          std::vector<std::list<Edge>> lines(p.size());
493
          auto bind_rev_edge = [&](std::list<Edge>::iterator lhs,
494
                                   std::list<Edge>::iterator rhs) {
495
            lhs->rev = rhs;
496
            rhs->rev = lhs;
497
         };
498
499
          bind_rev_edge(neighbor[ids[0]].emplace(neighbor[ids[0]].begin(), ids[1]),
500
                        neighbor[ids[1]].emplace(neighbor[ids[1]].begin(), ids[0]));
501
502
          for (int i = 2; i < ids.size(); ++i) {</pre>
503
            int u = ids[i];
504
            int cur = ccw[u];
505
            auto cur_iter = neighbor[cur].begin();
506
            while (1) {
              while (cur_iter != neighbor[cur].end()) {
507
508
                auto next_iter = std::next(cur_iter);
                if (next_iter == neighbor[cur].end()) {
509
510
                  if (cur != cw[u]) break;
511
512
                  if (Circle::side(p[cur], p[cur_iter->v], p[next_iter->v], p[u]) < 0)</pre>
513
                    break:
514
               }-
                neighbor[cur].erase(cur_iter++);
515
516
517
              bind_rev_edge(neighbor[u].emplace(neighbor[u].begin(), cur),
518
                            neighbor[cur].emplace(cur_iter, u));
519
              if (cur == cw[u]) break:
520
              std::tie(cur, cur_iter) =
521
                  std::make_pair(cur_iter->v, std::next(cur_iter->rev));
522
```

```
523
524
525
          for (int u = 0; u < p.size(); ++u)</pre>
526
           for (auto e : neighbor[u])
527
              if (u < e.v) edges.emplace_back(u, e.v);</pre>
528
          return edges;
529
       }
530
      };
531
532
      struct PlanarGraphDuality {
533
        struct DirectionalEdge {
534
          int v, id = -1;
535
          Point direction;
536
537
          DirectionalEdge(int v, Point direction) : v(v), direction(direction) {}
538
        };
539
        // return all points' id in each faces and the edges between faces
540
541
        static std::pair<std::vector<std::vector<int>>,
542
                         std::vector<std::pair<int, int>>>
543
        solve(const std::vector<Point>& p,
544
              const std::vector<std::pair<int, int>>& edges) {
545
          std::vector<DirectionalEdge> directional_edges;
546
          directional_edges.reserve(edges.size() * 2);
547
          std::vector<std::vector<int>> out_edges(p.size());
548
          for (auto [u, v] : edges) {
549
            out_edges[u].push_back(directional_edges.size());
550
            directional_edges.emplace_back(v, p[v] - p[u]);
551
            out_edges[v].push_back(directional_edges.size());
552
            directional_edges.emplace_back(u, p[u] - p[v]);
553
            directional_edges.end()[-1].rev = out_edges[u].back();
554
            directional_edges.end()[-2].rev = out_edges[v].back();
555
556
          const auto comp = [&, t_comp = Point::PolarComparer()](int lhs, int rhs) {
557
            return t_comp(directional_edges[lhs].direction,
558
                          directional_edges[rhs].direction);
559
560
          for (int u = 0; u < p.size(); ++u)</pre>
561
            std::sort(out_edges[u].begin(), out_edges[u].end(), comp);
562
          std::vector<std::vector<int>> faces;
563
          for (int u = 0; u < p.size(); ++u) {</pre>
564
            for (int e_id : out_edges[u]) {
565
              if (~directional_edges[e_id].id) continue;
566
              std::vector<int> pids;
567
              for (int cur_e_id = e_id;;) {
568
                if (~directional_edges[cur_e_id].id) break;
569
                directional_edges[cur_e_id].id = faces.size();
570
                int v = directional_edges[cur_e_id].v;
571
                pids.push_back(v);
572
                auto it = std::lower_bound(out_edges[v].begin(), out_edges[v].end(),
573
                                            directional_edges[cur_e_id].rev, comp);
574
                assert(*it == directional_edges[cur_e_id].rev);
```

```
575
                if (it == out_edges[v].begin())
576
                  cur_e_id = out_edges[v].back();
577
578
                  cur_e_id = *std::prev(it);
579
580
              faces.push_back(pids);
581
           }
582
         }
583
          std::vector<std::pair<int, int>> face_edges;
584
          for (int u = 0; u < p.size(); ++u)</pre>
585
           for (int e_id : out_edges[u]) {
586
             int rev_id = directional_edges[e_id].rev;
587
             if (e_id < rev_id) continue;</pre>
588
              face_edges.emplace_back(directional_edges[e_id].id,
589
                                      directional_edges[rev_id].id);
590
          return std::make_pair(faces, face_edges);
591
592
       }-
593
     };
594
595
      struct Voronoi {
        static constexpr long double kBoundaryInf = 50000;
596
597
598
        // should be guaranteed that
        // 1. all points are pairwise distinct
599
600
        // 2. boundary had better to be a convex
601
        // 3. all points are inside boundary
602
        static std::vector<std::vector<Point>> nearest(
603
            const std::vector<Point>& p,
604
            const std::vector<Line>& boundary = {
605
                Line(Point(-kBoundaryInf, -kBoundaryInf), Point(1, 0)),
606
                Line(Point(kBoundaryInf, -kBoundaryInf), Point(0, 1)),
607
                Line(Point(kBoundaryInf, kBoundaryInf), Point(-1, 0)),
608
                Line(Point(-kBoundaryInf, kBoundaryInf), Point(0, -1)),
609
           }) {
610
          // p0 in the left
611
          auto bisector = [&](const Point& p0, const Point& p1) {
612
            auto dir = (p1 - p0).rotate90();
            auto mid = (p0 + p1) / 2;
613
614
            return Line(mid, dir);
615
          };
          auto edges = Triangulation::nearest(p);
616
617
          std::vector<std::vector<Line>> limit(p.size(), boundary);
618
          for (auto [i, j] : edges) {
619
           limit[i].push_back(bisector(p[i], p[j]));
620
           limit[j].push_back(bisector(p[j], p[i]));
621
         1
622
          std::vector<std::vector<Point>> regions(p.size());
623
          for (int i = 0; i < p.size(); ++i) {</pre>
624
           regions[i] = HalfPlaneIntersection::solve(limit[i]);
625
626
          return regions;
```

```
627
628
629
       // should be quaranteed that
       // 1. p is strictly convex
630
       // 2. boundary had better to be a convex
631
632
       // 3. all points are inside boundary
633
       static std::vector<std::vector<Point>> furthest(
634
           const std::vector<Point>& p,
635
           const std::vector<Line>& boundary = {
636
               Line(Point(-kBoundaryInf, -kBoundaryInf), Point(1, 0)),
637
               Line(Point(kBoundaryInf, -kBoundaryInf), Point(0, 1)),
638
               Line(Point(kBoundaryInf, kBoundaryInf), Point(-1, 0)),
639
               Line(Point(-kBoundaryInf, kBoundaryInf), Point(0, -1)),
640
         // p0 in the right
641
642
         auto bisector = [&](const Point& p0, const Point& p1) {
643
           auto dir = (p0 - p1).rotate90();
644
           auto mid = (p0 + p1) / 2;
           return Line(mid, dir);
645
646
647
         auto edges = Triangulation::furthest(p);
648
         std::vector<std::vector<Line>> limit(p.size(), boundary);
649
         for (auto [i, j] : edges) {
650
           limit[i].push_back(bisector(p[i], p[j]));
651
           limit[j].push_back(bisector(p[j], p[i]));
652
653
         std::vector<std::vector<Point>> regions(p.size());
654
         for (int i = 0; i < p.size(); ++i) {</pre>
655
           regions[i] = HalfPlaneIntersection::solve(limit[i]);
656
657
         return regions;
658
659
660
661
     } // namespace geometry2d
662
      663
664
665
       // Area[i] 表示覆盖次数大于等于i的面积, 复杂度 O(n^2logn)
666
      struct P {
667
       ouble x, y;
       ()\{\{\}(double _x, double _y) \{ x = _x, y = _y; \}
       operator+(const P& b) const { return P(x + b.x, y + b.y); }
669
670
       operator-(const P& b) const { return P(x - b.x, y - b.y); }
       operator*(double b) const { return P(x * b, y * b); }
671
672
       operator/(double b) const { return P(x / b, y / b); }
673
       double det(const P& b) const { return x * b.y - y * b.x; }
       P rot90() const { return P(-y, x); }
       P unit() { return *this / abs(); }
676
       double abs() { return hypot(x, y); }
677 }:
    struct Circle {
```

```
679
680
        double r;
681
        bool contain(const Circle& v, const int& c) const { return sgn(r - (o - v.o).abs() - v.r) > c; }
        bool disjuct(const Circle& v, const int& c) const { // 0严格, -1不严格
         return sgn((o - v.o).abs() - r - v.r) > c;
683
684
      3-
685 };
686
     //求圆与圆的交点,包含相切,假设无重圆
     bool isCC(Circle a, Circle b, P& p1, P& p2) {
       if (a.contain(b, 0) || b.contain(a, 0) || a.disjuct(b, 0)) return 0;
689
       double s1 = (a.o - b.o).abs();
       double s2 = (a.r * a.r - b.r * b.r) / s1;
690
691
       double aa = (s1 + s2) / 2, bb = (s1 - s2) / 2;
       P mm = (b.o - a.o) * (aa / (aa + bb)) + a.o;
       double h = sgrt(max(0.0, a.r * a.r - aa * aa)):
693
       P vv = (b.o - a.o).unit().rot90() * h;
       p1 = mm + vv, p2 = mm - vv;
696
       return 1;
697 }
698
     struct EV {
699
       Pp;
700
       double ang
702
       EV() {}
       EV(const P& _p, double _ang, int _add) { p = _p, ang = _ang, add = _add; }
703
        bool operator<(const EV& a) const { return ang < a.ang; }</pre>
705
    } eve[N * 2];
706
     int E, cnt, C, i, j;
     Circle c[N];
     bool g[N][N], overlap[N][N];
     double Area[N]:
709
     int cX[N], cY[N], cR[N];
      bool contain(int i, int j) {
711
       return (sgn(c[i].r - c[j].r) > 0 || sgn(c[i].r - c[j].r) == 0 && i < j) && c[i].contain(c[j], -1);
712
713 }
714 int main() {
715
       scanf(" % d" , &C);
       for (i = 0; i < C; i++) {
716
         scanf(" % d % d % d", &cX[i], &cY[i], &cR[i]);
717
718
         c[i].o = P(cX[i], cY[i]);
719
         c[i].r = cR[i];
720
721
       for (i = 0; i <= C; i++) Area[i] = 0;
722
       for (i = 0; i < C; i++)
723
         for (j = 0; j < C; j++) overlap[i][j] = contain(i, j);</pre>
       for (i = 0: i < C: i++)
724
        for (j = 0; j < C; j++) g[i][j] = !(overlap[i][j] || overlap[j][i] || c[i].disjuct(c[j], -1));</pre>
725
726
727
        E = 0:
728
         cnt = 1;
729
         for (j = 0; j < C; j++)
730
          if (j != i && overlap[j][i]) cnt++;
```

```
731
          for (j = 0; j < C; j++)
            if (i != j && g[i][j]) {
732
733
              P aa, bb;
734
              isCC(c[i], c[j], aa, bb);
735
              double A = atan2(aa.y - c[i].o.y, aa.x - c[i].o.x);
736
              double B = atan2(bb.y - c[i].o.y, bb.x - c[i].o.x);
737
              eve[E++] = EV(bb, B, 1);
738
              eve[E++] = EV(aa, A, -1);
739
              if (B > A) cnt++;
740
741
          if (E == 0)
            Area[cnt] += PI * c[i].r * c[i].r;
742
743
744
            sort(eve, eve + E);
745
            eve[E] = eve[O].
746
            for (j = 0; j < E; j++) {
747
              cnt += eve[j].add;
748
              Area[cnt] += eve[j].p.det(eve[j + 1].p) * 0.5;
749
              double theta = eve[j + 1].ang - eve[j].ang;
              if (theta < 0) theta += PI * 2;
751
              Area[cnt] += theta * c[i].r * c[i].r * 0.5 - sin(theta) * c[i].r * c[i].r * 0.5;
752
753
754
755
        for (i = 1; i <= C; i++) printf(" % d % .3f\n", i, Area[i] - Area[i + 1]);</pre>
756
```

# 4 Math and Number Theory

**杨表** 标准杨表钩长公式:  $\frac{n!}{\prod hook(i,j)}$ , 其中 hook(i,j) = |(i,j)下方| + |(i,j)右方| + 自己;

半标准杨表(非严格递增)钩长公式:  $\prod_{(i,j)} \frac{n+j-i}{hook(i,j)}$ 

不交的 k 个上升子序列长度之和最大  $\Leftrightarrow$  上升杨表前 k 层长度和(不降子序列  $\Leftrightarrow$  半标准杨表)。序列依次插入杨表,若能放第 1 行末尾则放,否则取第 1 行大于当前数的最小的一个,取出,插入第 2 行。

整数拆分 五边形数: 
$$\phi(x) = \prod_{i=1}^{\infty} (1-x^i) = 1 + \sum_{i=1}^{\infty} (-1)^i x^{\frac{i(3i\pm1)}{2}}$$
 整数拆分:  $F(x) = \prod_{i=1}^{\infty} (1+x^i+x^{2i}+\cdots) = \prod_{i=1}^{\infty} \frac{1}{1-x^i}$   $\phi(x)$  与  $F(x)$  互为逆多项式 递推:  $F(n) = F(n-1) + F(n-2) - F(n-5) - F(n-7) \cdots$ 

单位根反演  $[i \bmod k = 0] = \frac{1}{k} \sum_{j=0}^{k-1} \omega^{ij}$ , $\omega$  为 k 次单位根

二项式反演  $a_n = \sum_{i=0}^n \binom{n}{i} b_i \Rightarrow b_n = \sum_{i=0}^n \binom{n}{i} (-1)^{n-i} a_i$ 

Fibonacci 通项:  $f_n = \frac{1}{\sqrt{5}} \left[ \left( \frac{1+\sqrt{5}}{2} \right)^n - \left( \frac{1-\sqrt{5}}{2} \right)^n \right]$ 

- 1. 相邻两项互质
- 2.  $f_{m+n} = f_{m-1}f_n + f_m f_{n+1}$
- 3.  $(f_{m+n}, f_n) = (f_m, f_n), (f_n, f_m) = f_{(n,m)}$
- 4.  $\sum_{i=0}^{n} f_i = f_{n+2} 1$ ,  $\sum_{i=0}^{n} f_i^2 = f_n f_{n+1}$
- 5.  $f_n^2 = (-1)^{n-1} + f_{n-1}f_{n+1}$

斯特林数 第一类: 将p个物品排成k个非空循环排列

$$S(p,k) = (p-1)S(p-1,k) + S(p-1,k-1)$$

$$S(p,0) = 0$$
,  $S(p,p) = 1$ ,  $S(0,0) = 1$ 

第二类:将p个物品划分成k个非空集合(无编号盒子)

$$S(p,k) = kS(p-1,k) + S(p-1,k-1)$$

$$S(p,0) = 0, S(p,p) = 1, S(0,0) = 1$$

$$S(n,m) = \frac{1}{m!} \sum_{k=0}^{m} (-1)^k \binom{m}{k} (m-k)^n = \sum_{k=0}^{m} \frac{(-1)^k (m-k)^n}{k! (m-k)!}$$
$$x^k = \sum_{i=1}^{k} S(k,i) \cdot i! \cdot C(x,i)$$

二次剩余 ①  $x^2 \equiv n \pmod{p}$ 

有解 iff  $n^{\frac{p-1}{2}} \equiv 1 \pmod{p}$ 

解: 随机 a 使得  $w = a^2 - n$  非二次剩余,则  $x = \pm (a + \sqrt{w})^{\frac{p+1}{2}}$ 

 $2 ax^2 + bx \equiv c \pmod{p}$ 

解: 配方得  $(2ax + b)^2 \equiv b^2 - 4ac \pmod{p}$ , 解  $+ \exp \operatorname{cd}$ 

线性逆元  $i^{-1} = -\lfloor \frac{p}{i} \rfloor \cdot (p \pmod{i})^{-1}$ 

powerful number 定义: 所含质因子次数全部大于 1 的数,这样的数只有 $\sqrt{n}$  个,可以暴力求。

积性函数求和  $\sum_{i=1}^{n} F(i)$ ,找一个积性函数 G 使得 G(p) = F(p),则  $H = \frac{F}{G}$  只在 powerful number 下有非 0 值。

$$\sum_{i=1}^{n} F(i) = \sum_{i=1}^{n} H(i) \sum_{j=1}^{\lfloor \frac{n}{i} \rfloor} G(j) = \sum_{i \in \text{powerful num}} H(i) S_{G}(\lfloor \frac{n}{i} \rfloor)$$

min25 数组  $g(n,j) = \sum_{i=1}^{n} [i \in P \lor minp_i > p_j] f(i)$  $S(n,j) = \sum_{i=1}^{n} [minp_i \ge p_j] f(i)$ 

幼	数	个	数	耒	

長	n	10	1ez	$1e_3$	164	teo	160	re/
	d(n)	4	12	32	64	128	240	448
	n	1e8	1e9	1e10	1e11	1e12	1e13	1e14
	d(n)	768	1344	2304	4032	6720	10752	17280
	n	1e15	1e16	1e17	1e18			
	d(n)	26880	41472	64512	103680			

#### 整数拆分数

	n	10	20	30	40	50
ι	p(n)	42	627	5604	37338	204226
	n	60	70	80	90	100
	p(n)	966467	4087968	15796476	56634173	190569292

```
10
                                                                                                   62
                                                                                                              if (n==pr[i]) return 1;
                                                                                                              if (n%pr[i]==0) return 0;
                                                                                                  63
11
12 LL mo;
                                                                                                  64
13 LL Pow(LL x, LL y) {} // mod mo
                                                                                                   65
                                                                                                           int d=0; LL s=n-1;
14 LL count(LL n, LL p) {return (n) ?(n/p+count(n/p,p)) :0 ;}
                                                                                                           for(; !(s&1); s>>=1, d++);
15 LL Fc(LL n, LL j) {
                                                                                                  67
                                                                                                           fo(i,0,8) if (!Miller_Rabin(d,s,pr[i],n)) return 0;
16
        if (!n) return 1;
                                                                                                   68
                                                                                                           return 1;
17
        LL re=Fc(n/p[j],j) *mi(fac[j],n/mo)%mo;
                                                                                                   69
        fo(i,1,n%mo) if (i%p[j]) re=re*i%mo;
                                                                                                  70
18
                                                                                                       19
        return re;
                                                                                                  71
20 }
                                                                                                  72
21
                                                                                                  73
                                                                                                       inline LL ran_f(LL x,LL c,LL n) {return (mul(x,x,n)+c)%n;}
22
    LL C(LL n, LL m, LL p) {
                                // compute C(n+m,n). M=n+m.
                                                                                                  74
                                                                                                       LL pollard_rho(LL n) {
23
        // preprocess: Prime(P); Pre();
                                                                                                  75
                                                                                                          for(LL c=rand()*rand()%n; ; c=rand()*rand()%n) {
24
        LL ans=0:
                                                                                                  76
                                                                                                              LL x=rand()*rand()%n, y=x;
25
        fo(j,1,p0) {
                                                                                                  77
                                                                                                              for(LL i=0, k=1; ; i++) {
26
           LL nump=count(M,p[j])-count(m,p[j])-count(n,p[j]);
                                                                                                  78
                                                                                                                  x=ran_f(x,c,n);
27
           LL phi=pk[j]-pk[j]/p[j];
                                                                                                   79
                                                                                                                  LL t=__gcd(abs(x-y),n);
                                                                                                   80
28
                                                                                                                  if (t==n) break;
29
           LL a=(nump>=num[j]) ?0 :Fc(M,j)*Pow(Fc(n,j),phi-1)%mo*Pow(Fc(m,j),phi-1)%mo*Pow(p[j],nump)%mo :81
                                                                                                                      else if (t>1) return t;
30
            (ans+=a *(P/pk[j])%P *Pow(P/pk[j],phi-1)%P)%=P;
                                                                                                   82
                                                                                                                  if (i==k) y=x, k<<=1;</pre>
                                                                                                   83
31
       }
32
                                                                                                   84
                                                                                                          }
33
                                                                                                   85
        return ans:
34
                                                                                                   86
35
                                                                                                       36
     88
37
                                                                                                   89
                                                                                                       struct FGH{
    int pr[9]={2,3,5,7,11,13,17,19,23};
                                                                                                       }; // f=\sum_{i=0}^n (a*i+b)/c, g=\sum_{i=0}^n i*(a*i+b)/c, h=\sum_{i=0}^n ((a*i+b)/c)^2
39
    LL mul(LL x,LL y,LL mo) {
                                                                                                  91
40
        I.I. re=0.
                                                                                                  92
41
        for(; y; y>>=1, x=(x+x)%mo) if (y&1) re=(re+x)%mo;
                                                                                                   93
                                                                                                       FGH calc(LL a, LL b, LL c, LL n) {
42
        return re;
                                                                                                  94
                                                                                                           LL ac=a/c, bc=b/c, sum1=n*(n+1)%mo*inv2%mo, sum2=n*(n+1)%mo*(2*n+1)%mo*inv6%mo;
43 }
                                                                                                   95
                                                                                                          if (!a) return (FGH){(n+1)*bc%mo, sum1*bc%mo, (n+1)*bc%mo*bc%mo};
44
    LL Pow(LL x,LL y,LL mo) {
                                                                                                  96
                                                                                                          if (a>=c || b>=c) {
45
                                                                                                  97
                                                                                                              FGH nxt=calc(a%c,b%c,c,n);
46
        for(; y; y>>=1, x=mul(x,x,mo)) if (y&1) re=mul(re,x,mo);
                                                                                                  98
                                                                                                              LL f=(nxt.f+ac*sum1+(n+1)*bc)%mo;
47
        return re;
                                                                                                  99
                                                                                                              LL g=(nxt.g+ac*sum2+sum1*bc)%mo;
48
                                                                                                  100
                                                                                                              LL h=(nxt.h+sum2*ac/mo*ac/mo+(n+1)*bc/mo*bc/mo+2*ac*nxt.g/mo+2*bc*nxt.f/mo+n*(n+1)/mo*ac/mo*bc/
49
    bool Miller_Rabin(int d,LL s,LL a,LL n) {
                                                                                                                    mo)%mo;
50
        a=Pow(a,s,n);
                                                                                                 101
                                                                                                              return (FGH){f,g,h};
        if (a==1) return 1;
                                                                                                  102
                                                                                                          } else {
51
52
        fo(i,1,d) {
                                                                                                 103
                                                                                                              LL m=(a*n+b)/c;
53
           if (a==n-1) return 1;
                                                                                                 104
                                                                                                              FGH nxt=calc(c,c-b-1,a,m-1);
           if (a==1) return 0;
54
                                                                                                  105
55
                                                                                                 106
                                                                                                              LL f=(m*n-nxt.f+mo)%mo:
           a=mul(a,a,n);
56
       }
                                                                                                  107
                                                                                                              LL g=((n+1)*n%mo*m-nxt.f-nxt.h+mo+mo)%mo*inv2%mo;
57
        return 0;
                                                                                                  108
                                                                                                              LL h=((m+1)*n%mo*m-nxt.g-nxt.g-f-nxt.f-nxt.f+mo*5)%mo;
58
                                                                                                  109
                                                                                                              return (FGH){f,g,h};
59
    bool isprime(LL n) {
                                                                                                 110
60
        if (n<2) return 0;
                                                                                                 111
        fo(i,0,8) {
                                                                                                 112
61
```

```
113
114
      115
     // f(n,k) 表示把 n 拆成 k 个数的积的方案数
116
     LL mw[2*maxsqrtn],g[2*maxsqrtn];
     int w0,id1[maxsqrtn],id2[maxsqrtn];
     LL min25_g(LL n) {
120
121
         for(LL i=1, j; i<=n; i=j+1) {</pre>
122
             j=n/(n/i);
123
             mw[++w0]=n/i;
             if (mw[w0]<=sqrtn) id1[mw[w0]]=w0; else id2[j]=w0;</pre>
124
125
             g[w0]=mw[w0]-1;
126
127
         fo(j,1,Np[sqrtn])
128
             for(int i=1; i<=w0 && (LL)p[j]*p[j]<=mw[i]; i++) {</pre>
                 int id=(mw[i]/p[j]<=sqrtn) ?id1[mw[i]/p[j]] :id2[n/(mw[i]/p[j])];</pre>
129
                 (g[i]-=g[id]-(j-1))%=mo;
130
            }
131
132
133
     LL min25_S(LL x, int j, int k) {
134
         if (x<=1 || p[j]>x) return 0;
135
         int id=(x<=sqrtn) ?id1[x] :id2[n/x];</pre>
136
         LL re=(g[id]-(j-1))*k;
137
         for(int i=j; i<=Np[sqrtn] && (LL)p[i]*p[i]<=x; i++) {</pre>
138
             LL pe=p[i];
139
             for(int e=1; pe*p[i] <= x; e++, pe*=p[i])</pre>
                 (re+=min25_S(x/pe,i+1,k)*C[e+k-1][k-1]+C[e+k][k-1])%=mo;
140
141
         }
142
         return re;
143 }
```

#### 5 Others

有向图最大费用循环流 思路: 先让正权边全部流满,再调整做法:

- 1. 先强制流掉所有正权边(并加入答案)
- 2. 然后流量盈余的点连向汇点,源点连向流量亏损的点
- 3. 答案减去 MCMF

无源汇上下界网络流 记  $d_i$  为点 i 的入流减出流,附加网络如下:

1. 原图每条边 (u, v, l, r), 连边 (u, v, r - l)

- 2. 若  $d_i > 0$ ,则  $(ss, i, d_i)$
- 3. 若  $d_i < 0$ ,则  $(i, tt, -d_i)$
- 4. 当且仅当 ss,tt 满流时有可行解

最大权闭合子图 答案 = 所有正点权的和 - 如下最小割:

- 1. 原图每条边 (u,v), 连边 (u,v,inf)
- 2. 超级源连向正点权,负点权连向超级汇

Segment Tree Beats 维护区间最小值、区间次小值以及最小值出现的次数;将操作 (x,y) 抽象为  $a_i := min(a_i + x,y)$ ; 若 TL 允许,写成矩阵形式转移最简单。

BEST 定理 图 G 从点 s 出发的欧拉路径数 =  $ts(G) \prod (deg(v) - 1)!$ ,其中 ts(G) 表示以 s 为根的外向树个数(入度矩阵 — 邻接矩阵,求 det)。 前提:每个点出度入度相同。

```
int ga[maxp]:
     int get(int x) {return (ga[x]==x) ?x :ga[x]=get(ga[x]) ;}
    int d[maxp], di, dj, sum, pt[maxp], pf[maxp], clr[maxp], nowT, bz[maxp];
     int lca(int x,int y) {
           for(nowT++, x=get(x), y=get(y); bz[x]!=nowT; ) {
                  bz[x]=nowT;
                  x=get(pf[pt[x]]);
                  swap(x,y);
           }
13
           return x;
14
15
     void shrink(int x,int y,int rt) {
           for(; get(x)!=rt; x=pf[y]) {
16
17
                  pf[x]=y;
18
                  y=pt[x];
19
                  if (clr[y]==1) clr[ d[++dj]=y ]=0;
20
                  ga[x]=ga[y]=rt;
21
22 }
    bool Blossom(int st) {
24
           fo(i,1,sum) ga[i]=i;
25
           memset(clr,255,sizeof(clr)); clr[st]=0;
```

18 5 others

```
26
             d[1]=st;
27
             for(di=1, dj=1; di<=dj; di++) {</pre>
28
                     int now=d[di];
                     for(int p=f1[now]; p; p=next[p]) if (clr[go[p]]==-1) {
29
30
                             clr[go[p]]=1;
31
                             pf[go[p]]=now;
32
                             if (!pt[go[p]]) {
33
                                     for(int x=now, y=go[p], t; x; y=t, x=pf[y]) {
34
                                             t=pt[x];
35
                                             pt[x]=y, pt[y]=x;
36
37
                                     return 1;
38
                             } else {
39
                                     d[++dj]=pt[go[p]];
40
                                     clr[pt[go[p]]]=0;
41
42
                    } else if (clr[go[p]]==0 && get(go[p])!=get(now)) {
43
                             int rt=lca(go[p],now);
44
                             shrink(go[p],now,rt);
45
                             shrink(now,go[p],rt);
46
47
             }
48
             return 0;
49
50
51
     //******************************** dominator tree (from CTL) *******************
52
53
     const int maxn = 310000;
54
     const int maxm = 1050000;
55
56
     int n,m,s;
57
     int sdom[maxn],idom[maxn];
58
     vector<int>V[maxn];
59
     vector < int > g[maxn], e[maxn];
60
61
     int dfn[maxn],To[maxn],id,par[maxn];
62
    void build(int u){
63
         To[dfn[u]=++id]=u;
         for (auto v:g[u]) if (!dfn[v]) par[v]=u,build(v);
64
65
66
     int fa[maxn],fas[maxn];
67
     void find(int x)
68
69
70
         if(fa[x]==x) return;
         find(fa[x]);
71
         if(dfn[sdom[fas[fa[x]]]] < dfn[sdom[fas[x]]]) fas[x] = fas[fa[x]];</pre>
72
73
         fa[x]=fa[fa[x]];
74 }
75
    int ans[maxn];
76
77 int main(){
```

```
78
         scanf("%d%d%d",&n,&m,&s);
 79
         int nn=n;
 80
         rep(i,1,m) {
 81
             int x,y;
 82
             scanf("%d%d",&x,&y);
 83
             e[n+i].push_back(x); e[y].push_back(n+i);
 84
             g[x].push_back(n+i); g[n+i].push_back(y);
 85
 86
         n+=m;
 87
         build(s);
         rep(i,1,n) fa[i]=i,fas[i]=i,sdom[i]=idom[i]=i;
 88
 89
         per(i,id,1){
 90
             int x=To[i],&semi=sdom[x];
 91
             for(auto y:e[x]) if (dfn[y]){
 92
                 find(y);
 93
                 if(dfn[semi]>dfn[sdom[fas[y]]]) semi=sdom[fas[y]];
 94
 95
             for(auto y:V[x]){
 96
                 find(y);
 97
                 if(dfn[sdom[fas[y]]]<i) idom[y]=fas[y];</pre>
 98
                 else idom[y]=x;
 99
             }
100
             V[semi].push_back(x);
101
             for (auto y:g[x]) if (par[y]==x) fa[y]=x;
102
103
         rep(i,1,id){
104
             int x=To[i];
105
             if(idom[x]!=sdom[x]) idom[x]=idom[idom[x]];
106
107
         per(i,id,2){
108
             int x=To[i];
             if (1<=x&&x<=n&&idom[x]>nn) ans[idom[x]-nn]=1;
109
110
         }
111
         int cnt=0;
112
         rep(i,1,m) if (!ans[i]) cnt++;
113
         printf("%d\n",cnt);
114
         rep(i,1,m) if (!ans[i]) printf("%d ",i);
115
         return 0;
116
117
118
      119
120
      int num,st[maxn];
      bool vis[maxn];
      void find(int k)
122
123
    -{
124
         vis[k]=1;
125
         st[++num]=k;
126
         for(int p=f1[k]; p; p=nxt[p]) if (!vis[go[p]]) find(go[p]);
127
128
129
     int bj[maxn],sum,nowh[maxn],d[maxn],bz[maxn],bzcnt;
```

19 5 OTHERS

```
// maxflow here, 稀疏图 dinic, else isap
     void bfs(int s)
131
132
         bz[ d[1]=s ]=++bzcnt;
133
134
         for(int i=1, j=1; i<=j; i++)
135
136
             for(int p=f1[d[i]]; p; p=nxt[p]) if (val2[p] && bz[go[p]]!=bzcnt)
137
                 bz[ d[++j]=go[p] ]=bzcnt;
138
         }
139
140
     int st1[maxn];
141
142
     vector<pair<int,int>> e[maxn];
143
     void Mincut(int 1,int r)
144
145
         memcpy(val2,val,sizeof(val));
146
         sum=st[r];
147
         int flow=0;
148
149
         while (Dinic_bfs(st[1])) flow+=Dinic_dfs(st[1],inf);
150
         e[st[1]].push_back(make_pair(sum,flow)), e[sum].push_back(make_pair(st[1],flow));
151
152
         bfs(st[1]);
153
         int newr=1-1, newl=r+1:
154
         fo(i,1,r) if (bz[st[i]]==bzcnt) st1[++newr]=st[i]; else st1[--newl]=st[i];
155
         fo(i,1,r) st[i]=st1[i];
156
157
         if (l<newr) Mincut(l,newr);</pre>
158
         if (newl<r) Mincut(newl,r);</pre>
159 }
160
161
     int main()
162
163
         fo(i,1,n) if (!vis[i] && f1[i])
164
165
             num=0;
166
             find(i);
167
             Mincut(1, num);
168
169
170
     171
172
173
     LL lx[maxn], ly[maxn], slack[maxn];
     int f[maxn],pre[maxn];
174
     bool vis[maxn]:
175
     LL KM(int nl,int nr)
176
177
178
         fo(i,1,nl)
179
             fo(j,1,nr) lx[i]=max(lx[i],mp[i][j]);
180
         fo(i,1,nl)
181
         {
```

```
182
             memset(slack,127,sizeof(LL)*(nr+1));
             memset(vis,0,sizeof(bool)*(nr+1));
183
184
             f[0]=i;
185
             int py=0, nextpy;
186
             for(; f[py]; py=nextpy)
187
188
                 int px=f[py];
189
                 LL d=inf;
                 vis[py]=1;
190
                 fo(j,1,nr) if (!vis[j])
191
192
193
                     if (lx[px]+ly[j]-mp[px][j]<slack[j]) slack[j]=lx[px]+ly[j]-mp[px][j], pre[j]=py;</pre>
194
                     if (slack[j]<d) d=slack[j], nextpy=j;</pre>
195
196
                 fo(j,0,nr) if (vis[j]) lx[f[j]]-=d, ly[j]+=d;
197
                     else slack[j]-=d;
198
199
             for(; py; py=pre[py]) f[py]=f[pre[py]];
200
201
         LL re=0;
202
         fo(i,1,nl) re+=lx[i];
203
         fo(j,1,nr) re+=ly[j];
204
         return re;
205
206
207
      208
209
     //倍增
     int deep[maxn],fa[maxn][MX+1];
     int lca(int x,int y) {
211
212
         if (deep[x]<deep[y]) swap(x,y);</pre>
213
214
             while (deep[fa[x][i]]>=deep[y]) x=fa[x][i];
215
         if (x==y) return x;
216
         fd(i,MX,0)
             while (fa[x][i]!=fa[y][i]) x=fa[x][i], y=fa[y][i];
217
218
         return fa[x][0];
219
220
221
^{222}
     int totq,goq[2*maxm],num[2*maxm],nextq[2*maxm],fq[maxn];
      void inq(int x,int y,int z) {
223
         goq[++totq]=y;
224
225
         num[totq]=z;
226
         nextq[totq]=fq[x];
227
         fq[x]=totq;
228 }
     int lca[maxm],fa[maxn];
230
     bool bz[maxn];
231
      int get(int x) {
232
         if (fa[x]==x) return x;
233
         return fa[x]=get(fa[x]);
```

20 5 others

```
234
235
     void tarjan(int k,int last) { //ordinary
236
          fa[k]=k;
          for(int p=f1[k]; p; p=next[p]) if (go[p]!=last) {
237
238
              tarjan(go[p],k);
239
             fa[go[p]]=k;
240
         }
241
          bz[k]=1;
242
          for(int p=fq[k]; p; p=nextq[p])
243
              if (bz[goq[p]]) lca[num[p]]=get(goq[p]); else inq(goq[p],k,num[p]);
244
245
246
     void tarjan(int k,int last) { //支持维护值
247
248
          for(int p=f1[k]; p; p=next[p]) if (go[p]!=last) {
249
              tarjan(go[p],k);
250
             f[go[p]]+=val[p];
251
             fa[go[p]]=k;
         }-
252
253
          bz[k]=1;
          for(int p=fq[k]; p; p=nextq[p]) if (bz[goq[p]]) {
254
255
             int t=get(goq[p]);
256
             ans[num[p]]=valq[p]+f[goq[p]];
257
              if (t!=k) inq(t,k,f[goq[p]],num[p]); else lca[num[p]]=t;
258
         } else inq(goq[p],k,0,num[p]);
259
260
261
      int fa[2*maxn][MX+5], deep[maxn], ap[2*maxn], fir[2*maxn], Log[2*maxn], er[MX+5];
263
264
          fo(i,1,ap[0]) fa[i][0]=ap[i], Log[i]=log(i)/log(2);
265
          fo(i,0,MX) er[i]=1<<i;
266
         fo(j,1,MX)
267
             fo(i,1,ap[0]) {
268
                  fa[i][j]=fa[i][j-1];
                  if (i+er[j-1] <= ap[0] && deep[fa[i+er[j-1]][j-1]] < deep[fa[i][j]])</pre>
269
270
                      fa[i][j]=fa[i+er[j-1]][j-1];
             }-
271
272
273
     int lca(int x,int y) {
274
          x=fir[x], y=fir[y];
275
          if (x>y) swap(x,y);
276
          int t=Log[y-x+1];
277
          return (deep[fa[x][t]] < deep[fa[y-er[t]+1][t]]) ?fa[x][t] :fa[y-er[t]+1][t] ;</pre>
278
279
      void dfs_pre(int k,int last) {
280
281
          deep[k]=deep[last]+1;
282
          ap[++ap[0]]=k, fir[k]=ap[0];
283
          for(int p=f1[k]; p; p=next[p]) if (go[p]!=last) {
284
              dfs_pre(go[p],k);
285
              ap[++ap[0]]=k;
```

```
286
287
288
     289
290
291
     struct node{
292
         int val,1,r,fa,dis;
293
     };
294
     node lt[maxn];
295
     int tot,ga[maxn];
297
     int New(int val=0)
298
299
         lt[++tot]=(node){val,0,0,0,0};
300
         ga[tot]=tot;
301
         return tot;
302
     int merge(int a, int b)
303
304
305
        if (!a) return b;
306
         if (!b) return a;
         if (lt[a].val>lt[b].val || lt[a].val==lt[b].val && a>b) swap(a,b);
307
308
         lt[a].r=merge(lt[a].r,b);
309
         lt[lt[a].r].fa=a:
         ga[lt[a].r]=a;
310
311
         if (lt[lt[a].r].dis>lt[lt[a].l].dis) swap(lt[a].l,lt[a].r);
312
         lt[a].dis=(lt[a].r==0) ?0 :lt[lt[a].r].dis+1;
313
314
     int top(int x) {return (ga[x]==x) ?x :ga[x]=top(ga[x]) ;}
315
316
     void pop(int x)
317
318
         int t=merge(lt[x].1,lt[x].r);
319
         lt[t].fa=lt[x].fa;
320
         ga[x]=(top(x)==x) ?t :top(x);
321
         ga[t]=ga[x];
322
         for(int i=lt[x].fa; i; i=lt[i].fa) if (lt[lt[i].l].dis<lt[lt[i].r].dis)</pre>
323
324
            swap(lt[i].1,lt[i].r);
325
            lt[i].dis=lt[lt[i].r].dis+1;
326
         } else break;
327
         lt[x].fa=-1;
328
329
     void push(int x,int val)
330
331
         merge(top(x),New(val));
332
333
334
     // init : lt [0]. dis=-1;
335
336
      337
```

21 5 others

```
//isap+gap+当前弧
      int bj[maxsum],gap[maxsum],sum,nowh[maxsum],d[maxsum];
339
340
      void init_Maxflow() {
          memset(bj,0,sizeof(bj));
341
          memset(gap,0,sizeof(gap)); gap[0]=sum+1;
342
343
          memcpy(nowh,f1,sizeof(nowh));
344
          d[1]=sum;
345
          for(int i=1, j=1; i<=j; i++) {</pre>
              for(int p=f1[d[i]]; p; p=e[p].nxt) if (e[p].go!=sum && !bj[e[p].go]) {
346
347
                  bj[e[p].go]=bj[d[i]]+1;
                  gap[0]--, gap[bj[e[p].go]]++;
348
349
                  d[++j]=e[p].go;
350
351
352
353
     int Maxflow(int k,int flow) {
          if (k==sum) return flow;
354
355
          int re=0;
          for(int &p=nowh[k]; p; p=e[p].nxt) if (e[p].val && bj[k]==bj[e[p].go]+1) {
356
357
              int fl=Maxflow(e[p].go, (flow-re<e[p].val) ?(flow-re) :e[p].val);</pre>
358
              e[p].val-=fl;
359
              e[(p&1) ?p+1 :p-1 ].val+=fl;
360
361
              if (re==flow || bj[0]>sum) return re;
362
363
          nowh[k]=f1[k];
364
          if ((--gap[bj[k]])==0) bj[0]=sum+1; else bj[k]++;
365
          gap[bj[k]]++;
366
          return re;
367 }
      //dinic+当前弧
368
369
      bool Dinic_bfs(int s) {
370
          memset(bj,255,sizeof(bj));
371
          memcpy(nowh,f1,sizeof(nowh));
372
         bj[ d[1]=s ]=0;
373
          for(int i=1, j=1; i<=j; i++) {</pre>
374
              for(int p=f1[d[i]]; p; p=e[p].nxt) if (e[p].val && bj[e[p].go]==-1) {
375
                  bj[e[p].go]=bj[d[i]]+1;
376
                  d[++j]=e[p].go;
377
             }
378
          return bj[sum]!=-1;
379
380
     1
381
      int Dinic_dfs(int k,int flow) {
          if (k==sum) return flow;
382
383
          int re=0:
          for(int &p=nowh[k]; p; p=e[p].nxt) if (e[p].val && bj[k]+1==bj[e[p].go]) {
384
385
              int fl=Dinic_dfs(e[p].go, (flow-re<e[p].val) ?(flow-re) :e[p].val);</pre>
386
              e[p].val-=fl;
387
              e[(p&1) ?p+1 :p-1 ].val+=fl;
388
              re+=fl:
389
              if (re==flow) return re;
```

```
390
391
         return re;
392
393
     394
395
396
     int bz[maxn],tim,pt[maxn];
397
     bool Hung(int x,int tim) {
398
         if (bz[x]==tim) return 0;
         bz[x]=tim;
399
400
         random_shuffle(e[x].begin(),e[x].end());
401
         for(int go:e[x]) {
402
            int k=pt[go];
403
            pt[k]=0, pt[x]=go, pt[go]=x;
404
            if (!k || Hung(k,tim)) return 1;
405
            pt[k]=go, pt[go]=k, pt[x]=0;
406
407
        return 0;
408 }
409
     int main() {
410
         fo(i,1,n) pmt[i]=i;
        random_shuffle(pmt+1,pmt+1+n);
411
412
         int tim=0, cnt=0;
413
         fo(i,1,5)
            fo(i,1,n) if (!pt[pmt[i]]) Hung(pmt[i],++tim);
414
415
416
417
     418
     //广义(任意路径都是圆方交替)
419
     int sum,dfn[maxn],low[maxn],z[maxn],z0,num[2*maxn],nn;
     vector<int> e[2*maxn];
422
     void tarjan(int k,int last) {
423
         dfn[k]=low[k]=++sum;
424
         z[++z0]=k;
         for(int p=f1[k]; p; p=nxt[p]) if (bh[p]!=last) {
425
426
            if (!dfn[go[p]]) {
427
                tarjan(go[p],bh[p]);
428
                low[k]=min(low[k],low[go[p]]);
429
430
                if (low[go[p]]>=dfn[k]) {
431
                   num[++nn]=1;
432
                   e[nn].push_back(k), e[k].push_back(nn);
433
                   do {
434
435
                       e[nn].push_back(z[z0]), e[z[z0]].push_back(nn);
436
                   } while (z[z0--]!=go[p]);
437
438
            } else low[k]=min(low[k],dfn[go[p]]);
439
440
441
```

22 5 OTHERS

```
442
     443
                                                                                          21
444
    int p0,p[2*maxn],z[maxn],z0;
                                                                                          22
                                                                                          23
    bool cmpP(const int &a,const int &b) {return dfn[a] <dfn[b];}
445
     void make_vtree() {
                                                                                          24
446
447
        tot=0:
                                                                                          25
448
        sort(p+1,p+1+p0,cmpP);
                                                                                          26
449
        int t=p0;
                                                                                          27
                                                                                          28
450
        fo(i,1,t-1) p[++p0]=lca(p[i],p[i+1]);
                                                                                          29
451
        sort(p+1,p+1+p0,cmpP);
        f1[z[z0=1]=1]=0;
                                                                                           30
452
453
        p[0]=1;
                                                                                          31
454
        fo(i,1,p0) if (p[i]!=p[i-1]) {
                                                                                          32
455
           for(; z0 && (dfn[p[i]] < dfn[z[z0]] || en[z[z0]] < dfn[p[i]]); z0--) ins(z[z0-1],z[z0]);</pre>
                                                                                           33
456
           f1[ z[++z0]=p[i] ]=0;
                                                                                          34
457
                                                                                           35
458
        fo(i,1,z0-1) ins(z[i],z[i+1]);
                                                                                           36
459
    }
                                                                                          37
                                                                                          38
460
461
     39
462
                                                                                           40
    //乘法取模黑科技 Claris
                                                                                           41
463
464
    LL mul(LL a, LL b, LL n) {return(a*b-(LL)(a/(long double)n*b+1e-3)*n+n)%n;}
                                                                                           42
465
                                                                                          43
     //split a string by whitespace
                                                                                           44
466
467
     vector<string> split_str(string str) {
                                                                                           45
468
        vector<string> result;
                                                                                           46
                                                                                           47
469
        istringstream iss(str);
470
                                                                                           48
        while ( getline( iss, s, ' ' ) ) result.push_back(s);
                                                                                           49
471
472
        return result:
                                                                                          50
473 }
                                                                                          51
                                                                                          52
                                                                                          53
                                                                                          54
     55
 3 // 操作 (l1,r1,l2,r2,v) 可视为在时间 l1, 对 [l2,r2]+=v, 在时间 l2+1, 对 [l2,r2]-=v,
                                                                                          56
 4 // 询问 (l1, r1, l2, r2) 可视为将只考虑时间 [l1, l2], [l2, r2] 上的历史最大值
                                                                                          57
 5 // 每个询问套在线段树分治区间 [l,r], 分成 [l,mid], [mid+1,r] 两段询问
                                                                                           58
    // 总复杂度 O(nlog^2n+glogn)
                                                                                           59
    #include <bits/stdc++.h>
                                                                                           60
                                                                                                  }
    #define maxn 500050
                                                                                          61
    using namespace std;
                                                                                          62
10
    typedef long long LL;
                                                                                          63
11
                                                                                          64
12
    const LL N=65536, M=1e10, inf=1e18;
                                                                                          65
13
                                                                                           66
14
    struct node {
                                                                                          67
15
        LL mx, hmx;
                                                                                          68
16
        LL tag, htag;
                                                                                          69
17 } T[N<<1];
                                                                                           70
    #define mx(k) T[k].mx
    #define tag(k) T[k].tag
```

```
#define hmx(k) T[k].hmx
     #define htag(k) T[k].htag
     void build(int k,int l,int r) {
         mx(k)=hmx(k)=0;
         tag(k)=htag(k)=0;
         if (l==r) return ;
         int mid=(1+r)>>1;
         build(k<<1,1,mid);
         build(k<<1|1,mid+1,r);
     void renew(int k,LL h,LL d) {
         h=max(h,OLL);
         htag(k)=max(htag(k),tag(k)+h);
         tag(k)+=d;
         hmx(k)=max(hmx(k),mx(k)+h);
         mx(k)+=d;
     void godown(int k) {
         renew(k<<1,htag(k),tag(k));
         renew(k<<1|1,htag(k),tag(k));
         htag(k)=tag(k)=0;
     void update(int k) {
         mx(k)=max(mx(k<<1),mx(k<<1|1));
         hmx(k)=max(hmx(k<<1),hmx(k<<1|1));
     void change(int k,int l,int r,int a,int b,LL d) {
         if (a<=1&&r<=b)
             renew(k,d,d);
         else {
             godown(k);
             int mid=(1+r)>>1;
             if (a<=mid)
                 change(k<<1,1,mid,a,b,d);
             if (b>mid)
                 change(k<<1|1,mid+1,r,a,b,d);
             update(k);
     LL query(int k, int l, int r, int a, int b) {
         if (a>r||1>b) return -inf;
         if (a<=1&&r<=b) return hmx(k):
         godown(k);
         int mid=(1+r)>>1;
         return max(query(k<<1,1,mid,a,b),query(k<<1|1,mid+1,r,a,b));</pre>
71 struct seg {
```

23 5 OTHERS

```
72
          int l,r,x;
73
         bool operator < (const seg& s) const {</pre>
74
             return x<s.x;
 75
76
 77
     vector<seg> L[maxn],R[maxn];
78
79
     int n,m,q;
     int Log2(int x) {    return !x?-1:Log2(x>>1)+1; }
80
     LL ans[maxn];
81
     vector<pair<seg,int> > LQ[maxn], RQ[maxn];
82
83
      void Max(LL &a,LL b) {    a=max(a,b); }
84
85
      int main() {
          scanf("%d%d%d",&n,&m,&q);
86
          while (m--) {
87
 88
             int 11,12,r1,r2,x;
 89
             scanf("%d%d%d%d%d",&11,&12,&r1,&r2,&x);
90
             L[11].push_back(seg{12,r2,x});
91
             R[r1].push_back(seg{12,r2,x});
92
         }
93
         for (int i=0;i<q;++i) {</pre>
94
             int 11,12,r1,r2;
95
             scanf("%d%d%d%d",&11,&12,&r1,&r2);
             int t=max(Log2(l1^r1),0);
96
97
             LQ[t].emplace_back(seg{12,r2,r1},i);
98
             RQ[t].emplace_back(seg{12,r2,l1},i);
99
         }-
100
101
          for (int t=0;(1<<t)<=N;++t) {</pre>
102
             build(1,0,N-1);
103
             LL cnt=0, sum=0, ALL=(1<<t)-1;
```

```
104
105
                sort(LQ[t].begin(),LQ[t].end());
106
               for (int i=0,j=0;i<N;++i) {</pre>
107
                    for (seg s:L[i])
108
                         change(1,0,N-1,s.1,s.r,s.x),++cnt;
109
                    for (; j < LQ[t].size()&&LQ[t][j].first.x==i;++j)</pre>
110
                         Max(ans[LQ[t][j].second], query(1,0,N-1,LQ[t][j].first.l,LQ[t][j].first.r)-sum*M);
111
                    for (seg s:R[i])
112
                         change(1,0,N-1,s.1,s.r,-s.x),++cnt;
                    if (ALL&~i) continue;
113
114
                    change(1,0,N-1,0,N-1,cnt*M);
115
                    sum+=cnt,cnt=0;
116
               }
117
               build(1,0,N-1),sum=cnt=0;
118
               sort(RQ[t].rbegin(),RQ[t].rend());
119
120
               for (int i=N-1, j=0; i>=0; --i) {
121
                    for (seg s:R[i])
122
                         change(1,0,N-1,s.1,s.r,s.x),++cnt;
123
                    for (; j < RQ[t].size() && RQ[t][j].first.x==i;++j)</pre>
124
                          \texttt{Max}(\texttt{ans}[\texttt{RQ[t][j]}.\texttt{second}], \texttt{query}(\texttt{1,0,N-1,RQ[t][j]}.\texttt{first.l}, \texttt{RQ[t][j]}.\texttt{first.r}) - \texttt{sum*M}); 
125
                    for (seg s:L[i])
126
                         change(1,0,N-1,s.1,s.r,-s.x),++cnt;
127
                    if (ALL&i) continue:
128
                    change(1,0,N-1,0,N-1,cnt*M);
129
                    sum+=cnt,cnt=0;
130
131
132
           for (int i=0;i<q;++i) printf("%11d\n",ans[i]);</pre>
133
           return 0;
134 }
```

24 5 others