

4th symbol Grammer we have given input n & k Grammer desired

k^{th} Symbol Grammer

→ Problem statement → IP. OP

→ (IBH) Induction → Base condition → Hypothesis

→ Code

Problem statement :- we have given input n & k

$n=1, k=1$

return 0

defined

$n \rightarrow \text{row}$

$k \rightarrow \text{col}$

0th $\rightarrow 0$

1th $\rightarrow 10$

$n-1$ th row $\rightarrow 0$
 n th row $\rightarrow 0$

$n-1$ th row $\rightarrow 1$
 n th row $\rightarrow 10$

Ex: $n=1, k=1$

output $\rightarrow 0$

Ex: $n=2, k=1$

$n=1$ $k=1$
 0

$n=2$ 01

output $\rightarrow 0$

Ex: $n=2, k=2$

$n=1$

0

$n=2$

01

$n=3$ 0110

output $\rightarrow 1$

we have to return
 k^{th} symbol in n^{th} row
 (1-index)

Ex: $n=4, k=3$

$n=1$

0

$n=2$

01

$n=3$

0110

$n=4$

01101001

$n=4, k=3$

output $\rightarrow 1$

IP-OP. Ps : n, k



IBH Method:-

Hypothesis n, k

$\text{solve}(n, k) \rightarrow 0 \text{ or } 1$

Small IP

$\hookrightarrow \text{solve}(n-1, ?)$

Gramm

$n=1$ $0 \rightarrow 1$

$n=2$ $01 \rightarrow 2$

$n=3$

0110

complement $\rightarrow 2$

$n-1$

Observation

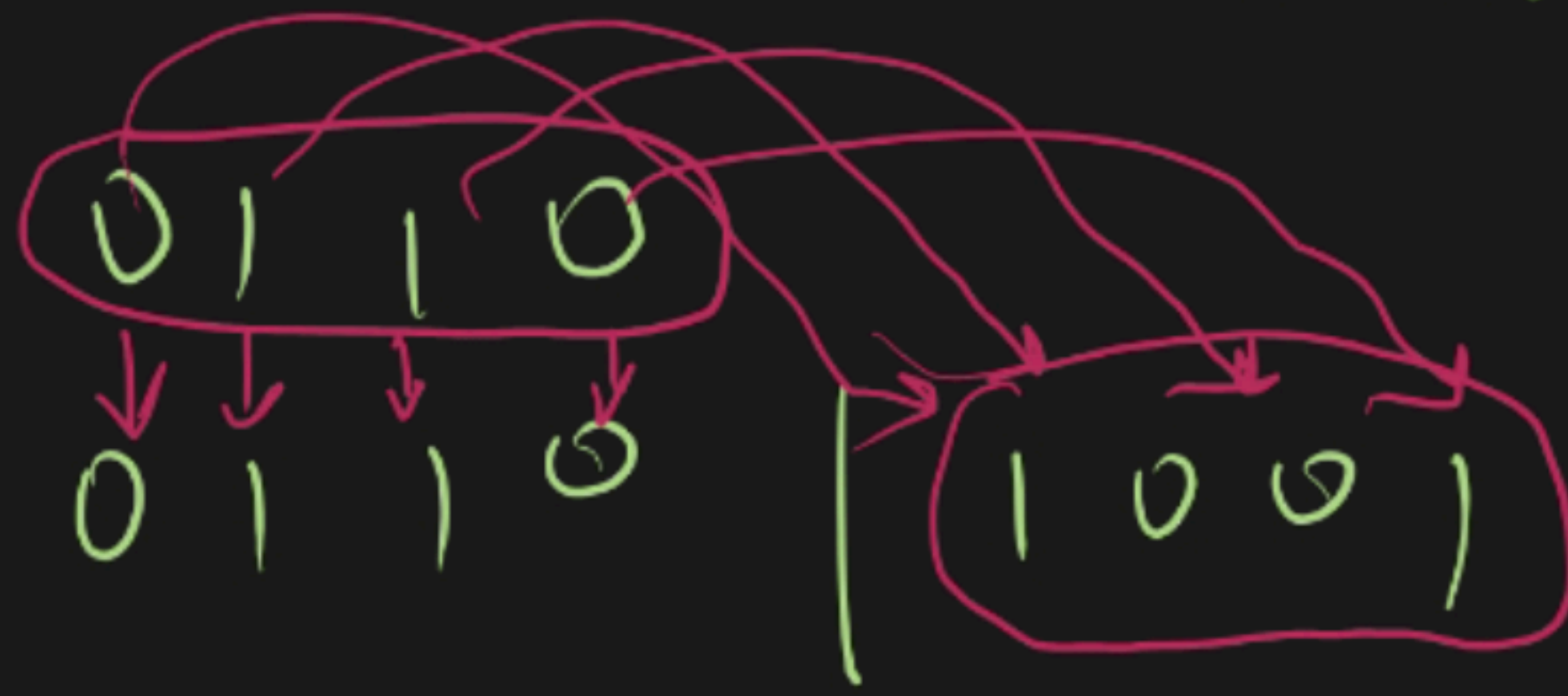
(-) length $2 \times \text{time}$

(i) n th row \rightarrow 1st half $k = n-1$ row k

(ii) n th row \rightarrow 2nd half $k = \text{complement of } n-1 \text{ row } k$
value

$n = 3$

$n = 4$



$\leftarrow \text{mid} \rightarrow$
 $= \frac{\text{len}}{2}$

\rightarrow Hypothesis

if ($k \leq \text{mid}$)

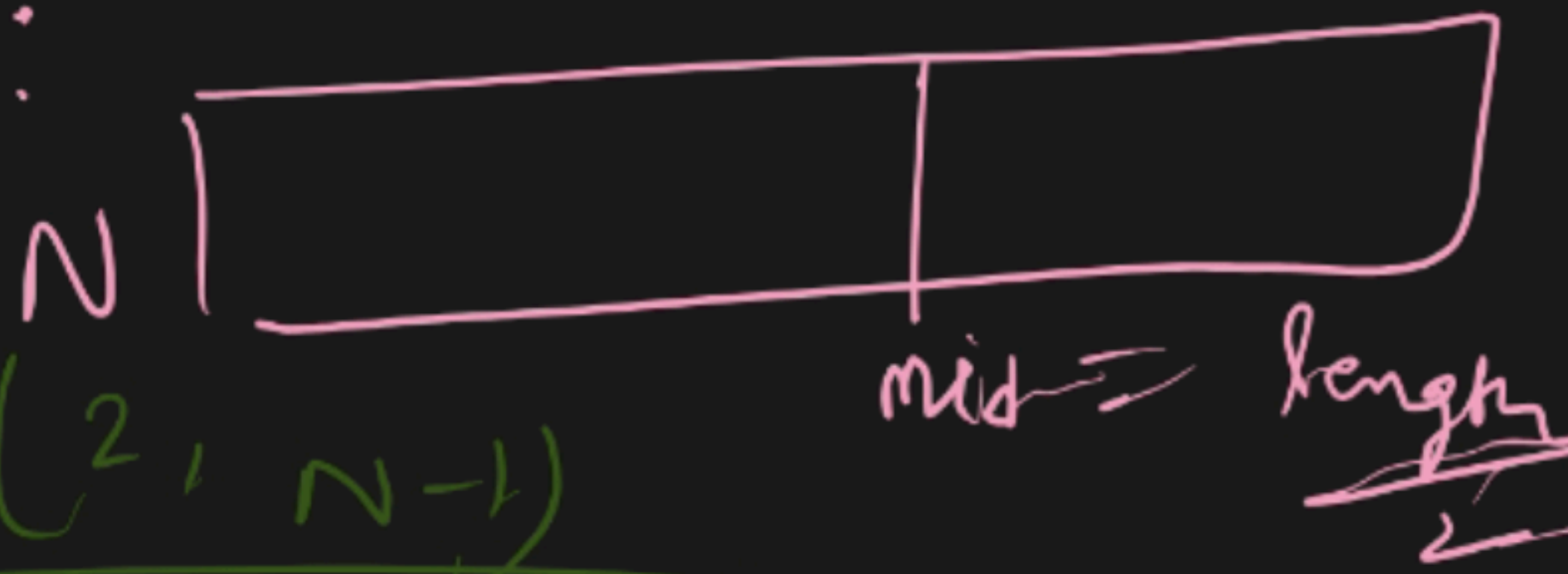
$\text{solve}(N, k) \rightarrow \text{solve}(N-1, k)$

if ($k > \text{mid}$)

$\text{solve}(N, k) \rightarrow \text{solve}(N-1, k - \text{mid})$

Base condition:- $n = 1, k = 1$
return 0;

Induction Step:



int mid = $\text{Pow}(2, N-1)$

if ($k \leq \text{mid}$) return $\text{solve}(N-1, k)$;

else return $! \text{solve}(N-1, k - \text{mid})$;

$N=1$ 0 $\rightarrow 1 = 2^0$
 $N=2$ 0 1 $\rightarrow 2 = 2^1$
 $N=3$ 0 1 1 0 $\rightarrow 4 = 2^2$
 $N=4$ 0 1 1 0 1 0 0 1 $\rightarrow 8 = 2^3$

if $N=1$, length = 2^{N-1}