

4th symbol Grammer we have given input n & KGrammer desired

Kth Symbol Grammer

→ Problem statement → IP. of

→ (IBH) Induction → Base condition → Hypothesis

→ Code

Problem statement :- We have given input $n \& k$ →

$$n=1, k=1$$

return 0

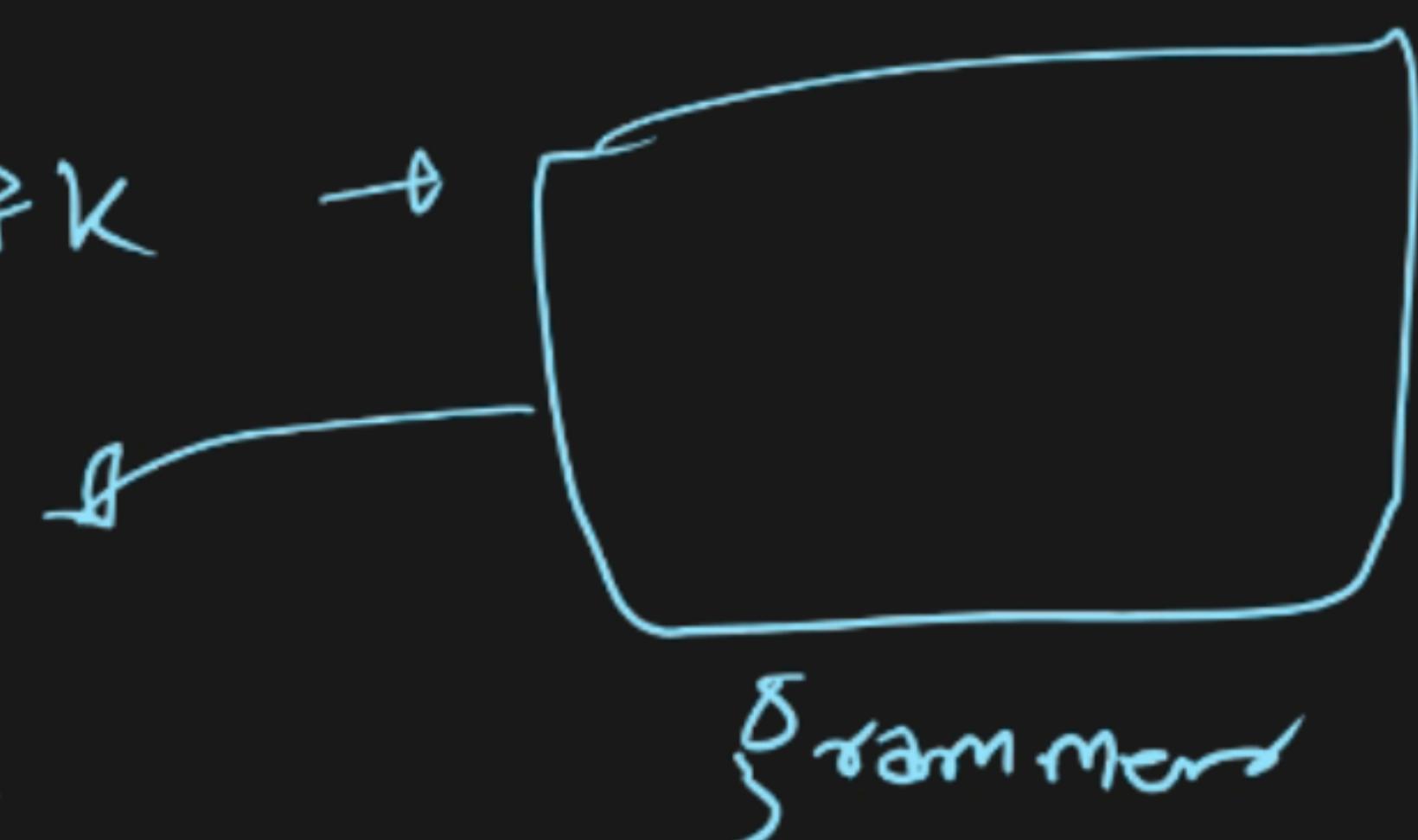
defined

$$n \rightarrow \text{row}$$

$$k \rightarrow \text{col}$$

$$0^{\text{th}} \rightarrow 0$$

$$1^{\text{th}} \rightarrow 1$$



$$\text{Ex:- } n=1, k=1$$

Output = 0

$$\text{Ex:- } n=2, k=1$$

$$n=2 \xrightarrow{k=1} 0$$

$$n=2 \quad ① \mid 1$$

Output = 0

$$\text{Ex:- } n=2, k=2$$

$$n=1$$

0

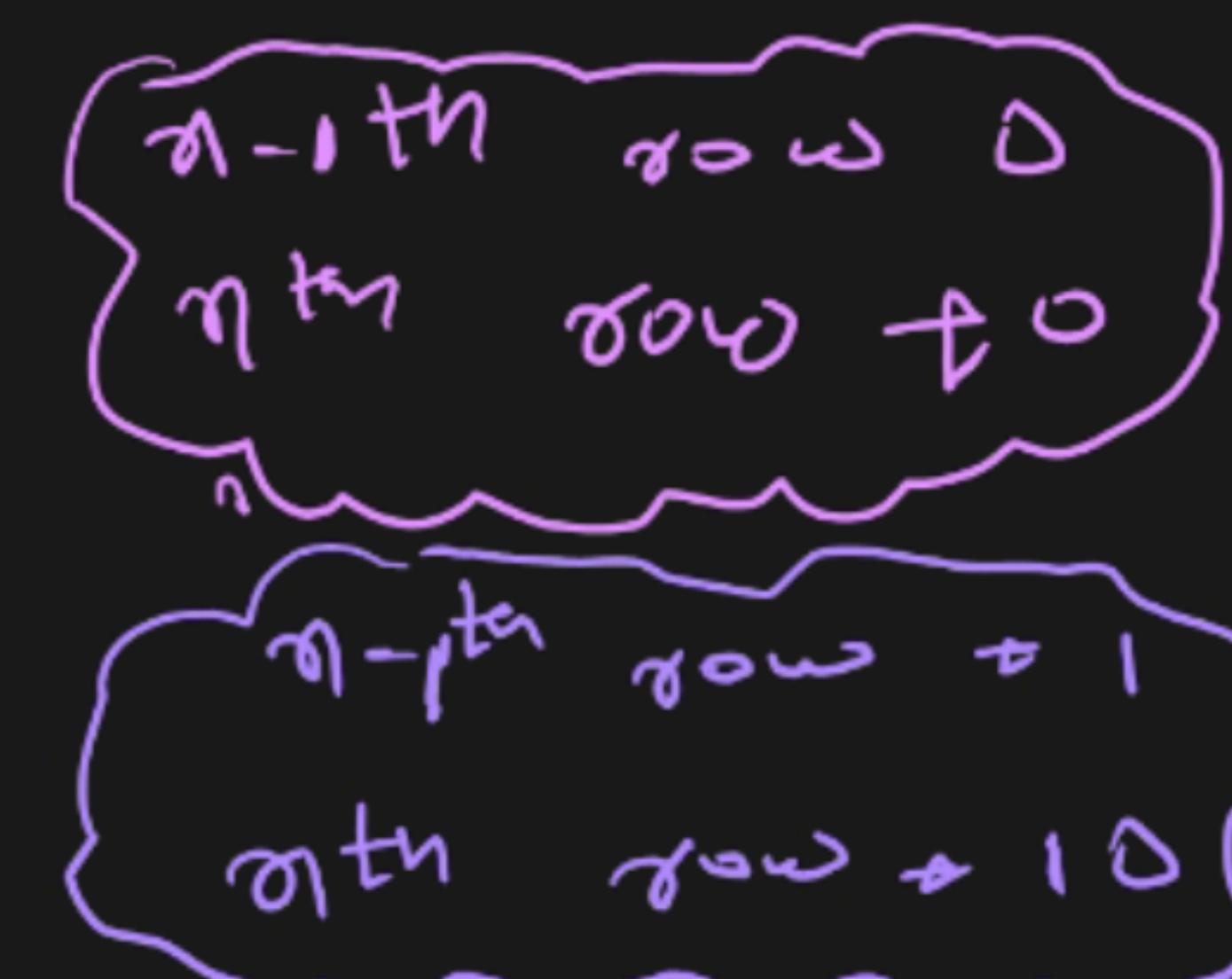
$$n=2$$

$$0 \quad 1$$

$$n=3$$

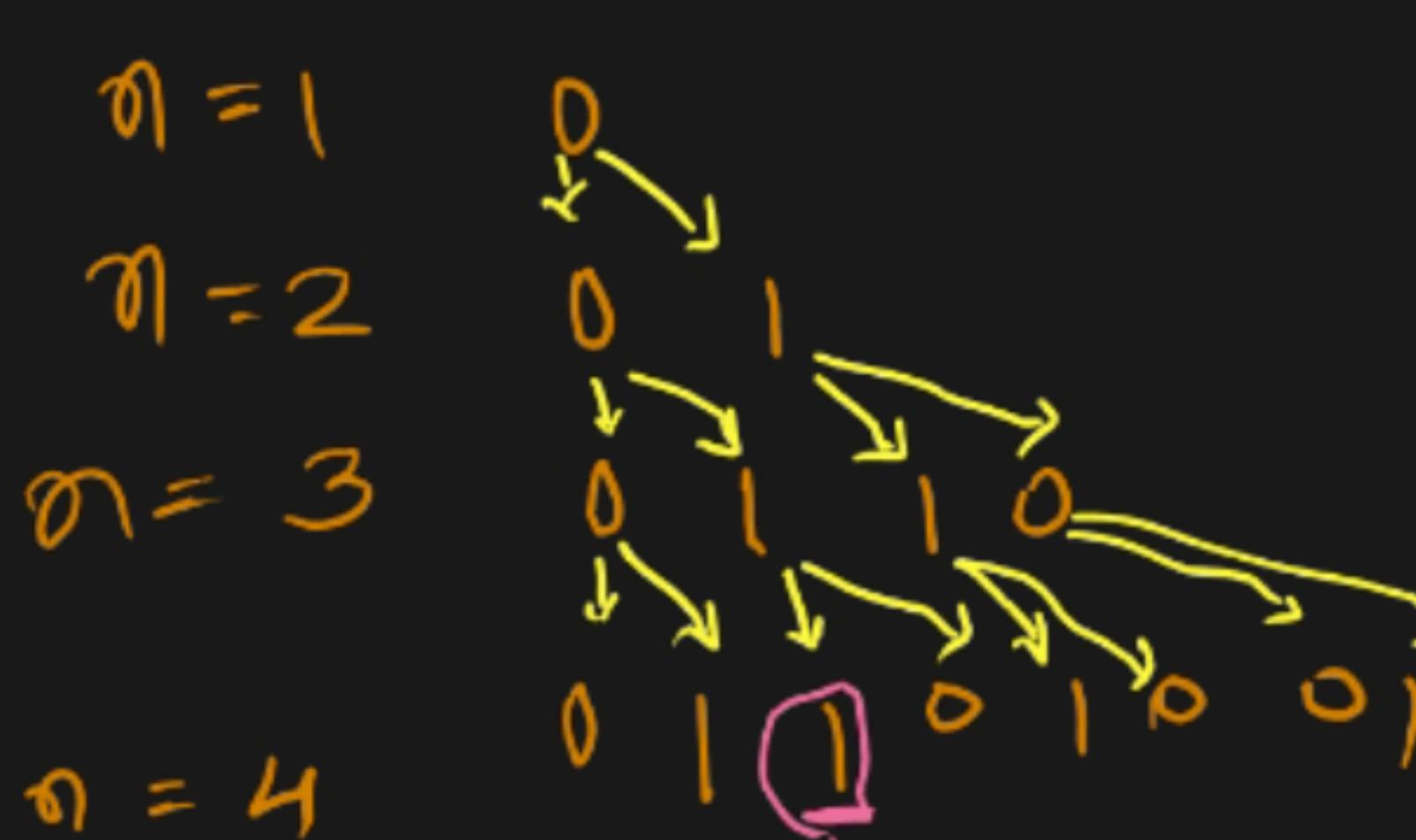
$$0 \quad 1 \quad 1 \quad 0$$

Output = 1



we have to return
kth symbol in nth row
(1-index)

$$\text{Ex:- } n=4, k=3$$



IP-OP.Qs : n,k



IBH Method :-

Hypothesis n, k

Solve(n,k) → 0 or 1 Gramm

Small IP

↪ Solve(n-1, ?)

$$n=1 \quad 0 \rightarrow 1$$

$$n=2 \quad 0 \quad 1 \rightarrow 2$$

$$n=3 \quad \begin{matrix} 0 & | & 1 & 0 \end{matrix} \rightarrow 4$$

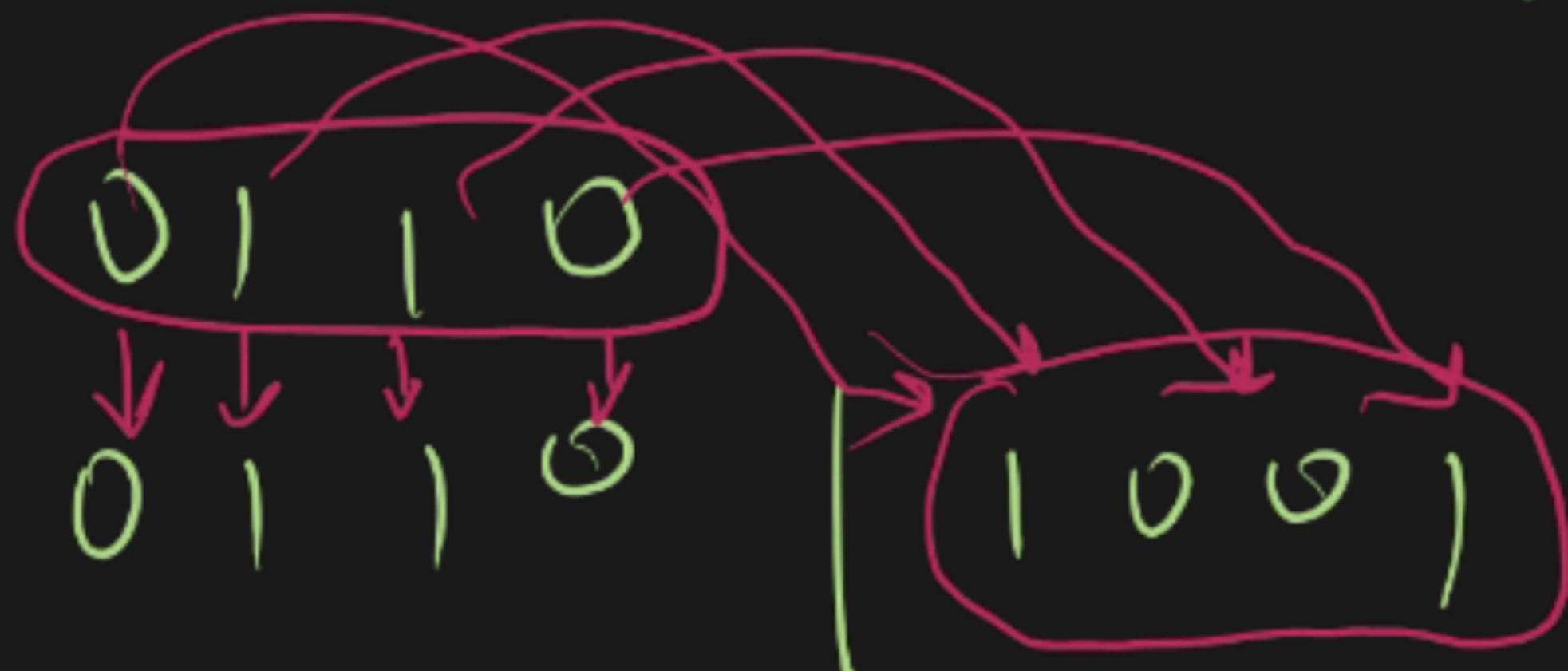
complement → 4

Observation

- (a) length $\geq 2 \times \text{time}$
- (b) n^{th} row \rightarrow 1st half $k = n-1$ row k
- (c) n^{th} row \rightarrow 2nd half $k = \text{complement of } n-1 \text{ row } k$

$$N = 3$$

$$n = 4$$



$$\leftarrow^{\text{mid}} \frac{\text{length}}{2} \Rightarrow$$

\rightarrow Hypothesis

if ($k \leq \text{mid}$)

solve(n, k) \rightarrow solve($n-1, k$)

if ($k > \text{mid}$)

solve(n, k) \rightarrow solve($n-1, k - \text{mid}$)

Base Condition:- $n=1, k=1$

return 0;

Induction Step:

int mid = $\lceil \log(2, N-1) \rceil$ $\text{mid} = \frac{\text{length}}{2}$

```

if ( $k \leq \text{mid}$ ) return solve( $n-1, k$ );
else
    return !solve( $n-1, k - \text{mid}$ );
}

```

$$\begin{aligned}
 N=1 \quad 0 &\rightarrow 1 = 2^0 \\
 N=2 \quad 0 &\rightarrow 2 = 2^1 \\
 N=3 \quad 0 &\rightarrow 4 = 2^2 \\
 N=4 \quad 0 &\rightarrow 8 = 2^3
 \end{aligned}$$

if $N=1$, length = 2^{N-1}