gmp

Ruby bindings to the GMP library Edition 0.4.3 8 March 2010

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This manual describes how to use the gmp Ruby gem, which provides bindings to the GNU multiple precision arithmetic library, version 4.3.x or 5.0.x.

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1 Introduction to GNU MP

This entire page is copied verbatim from the GMP Manual.

GNU MP is a portable library written in C for arbitrary precision arithmetic on integers, rational numbers, and floating-point numbers. It aims to provide the fastest possible arithmetic for all applications that need higher precision than is directly supported by the basic C types.

Many applications use just a few hundred bits of precision; but some applications may need thousands or even millions of bits. GMP is designed to give good performance for both, by choosing algorithms based on the sizes of the operands, and by carefully keeping the overhead at a minimum.

The speed of GMP is achieved by using fullwords as the basic arithmetic type, by using sophisticated algorithms, by including carefully optimized assembly code for the most common inner loops for many different CPUs, and by a general emphasis on speed (as opposed to simplicity or elegance).

There is assembly code for these CPUs: ARM, DEC Alpha 21064, 21164, and 21264, AMD 29000, AMD K6, K6-2, Athlon, and Athlon64, Hitachi SuperH and SH-2, HPPA 1.0, 1.1, and 2.0, Intel Pentium, Pentium Pro/II/III, Pentium 4, generic x86, Intel IA-64, i960, Motorola MC68000, MC68020, MC88100, and MC88110, Motorola/IBM PowerPC 32 and 64, National NS32000, IBM POWER, MIPS R3000, R4000, SPARCv7, SuperSPARC, generic SPARCv8, UltraSPARC, DEC VAX, and Zilog Z8000. Some optimizations also for Cray vector systems, Clipper, IBM ROMP (RT), and Pyramid AP/XP.

For up-to-date information on GMP, please see the GMP web pages at http://gmplib.org/

The latest version of the library is available at ftp://ftp.gnu.org/gnu/gmp/

Many sites around the world mirror 'ftp.gnu.org', please use a mirror near you, see http://www.gnu.org/orc for a full list.

There are three public mailing lists of interest. One for release announcements, one for general questions and discussions about usage of the GMP library, and one for bug reports. For more information, see

http://gmplib.org/mailman/listinfo/.

The proper place for bug reports is gmp-bugs@gmplib.org. See Chapter 4 [Reporting Bugs], page 28 for information about reporting bugs.

2 Introduction to the gmp gem

The gmp Ruby gem is a Ruby library that provides bindings to GMP. The gem is incomplete, and will likely only include a subset of the GMP functions. It is built as a C extension for ruby, interacting with gmp.h. The gmp gem is not endorsed or supported by GNU or the GMP team. The gmp gem also does not ship with GMP, so GMP must be compiled separately.

3 Installing the gmp gem

3.1 Prerequisites

OK. First, we've got a few requirements. To install the gmp gem, you need one of the following versions of Ruby:

- (MRI) Ruby 1.8.6 tested lightly.
- (MRI) Ruby 1.8.7 tested seriously.
- (MRI) Ruby 1.9.1 tested seriously.

As you can see only Matz's Ruby Interpreter (MRI) is supported. I haven't even put a thought into trying other interpreters/VMs. I intend to look into FFI, which supposedly will allow me to load this extension into JRuby and Rubinius, not sure about others...

Next is the platform, the combination of the architecture (processor) and OS. As far as I can tell, if you can compile GMP and Ruby on a given platform, you can use the gmp gem there too. Please report problems with that hypothesis.

Lastly, GMP. GMP must be compiled and working. "and working" means you ran "make check" while installing GMP. The following versions of GMP have been tested:

- GMP 4.3.1
- GMP 4.3.2
- GMP 5.0.0
- GMP 5.0.1

That's all. I don't intend to test any older versions, maybe 4.3.0 for completeness.

Here is a table of the exact environments on which I have tested the gmp gem:

Platform	Ruby	GMP
Cygwin on x86	(MRI) Ruby 1.8.7	
Linux (LinuxMint 7) on x86	(MRI) Ruby 1.8.7	GMP 4.3.1
Mac OS X 10.5.7 on x86 (32-bit)	(MRI) Ruby 1.8.6	GMP 4.3.1
Mac OS X 10.5.7 on x86 (32-bit)	(MRI) Ruby 1.9.1	GMP 4.3.1
Windows XP on x86 (32-bit)	(MRI) Ruby 1.9.1	GMP 5.0.1

3.2 Installing

You may clone the gmp gem's git repository with:

```
git clone git://github.com/srawlins/gmp.git
```

Or you may install the gem from gemcutter:

```
gem install gmp
```

Or you may install the gem from github (old):

```
gem install srawlins-gmp
```

At this time, the gem does not self-compile (how does that work?). To compile the C extensions, do the following:

```
cd <gmp gem directory>/ext
ruby extconf.rb
make
```

There shouldn't be any errors, or warnings.

4 Testing the gmp gem

Testing the gmp gem is quite simple. The test/unit_tests.rb suite uses Unit::Test. You can run this test suite with:

```
cd <gmp gem directory>/test
ruby unit_tests.rb
```

All tests should pass. If you don't have the test-unit gem installed, then you may run into one error. I'm not sure why this is... I suspect a bug in Ruby's Test::Unit that the test-unit gem monkey patches.

5 GMP and gmp gem basics

5.1 Classes

The gmp gem includes the namespace GMP and four classes within GMP:

- GMP::Z Methods for signed integer arithmetic. There are at least 45 methods here (still accounting).
- GMP::Q Methods for rational number arithmetic. There are at least 11 methods here (still accounting).
- GMP::F Methods for floating-point arithmetic. There are at least 6 methods here (still accounting).

• GMP::RandState - Methods for random number generation. There are 3 methods here.

In addition to the above four classes, there is also one constant within GMP:

- GMP::GMP_VERSION The version of GMP linked into the gmp gem
- GMP::GMP_CC The compiler that compiled GMP linked into the gmp gem
- GMP::GMP_CFLAGS The compiler flags used to compile GMP linked into the gmp gem
- GMP::GMP_BITS_PER_LIMB The number of bits per limb

6 MPFR basics

The gmp gem can optionally link to MPFR, the Multiple Precision Floating-Point Reliable Library. The x86-mswin32 version of the gmp gem comes with MPFR. This library uses the floating-point type from GMP, and thus the MPFR functions mapped in the gmp gem become methods in GMP::F.

There are additional constants within GMP when MPFR is linked:

- GMP::MPFR_VERSION The version of MPFR linked into the gmp gem.
- GMP::GMP_RNDN Rounding mode representing "round to nearest."
- GMP::GMP_RNDZ Rounding mode representing "round toward zero."
- GMP::GMP_RNDU Rounding mode representing "round toward positive infinity."
- GMP::GMP_RNDD Rounding mode representing "round toward negative infinity."

Integer Functions

Initializing, Assigning Integers 7.1

GMP::Z.new $\rightarrow integer$ new GMP::Z.new(numeric = 0) $\rightarrow integer$ $GMP::Z.new(str) \rightarrow integer$

> This method creates a new GMP::Z integer. It takes one optional argument for the value of the integer. This argument can be one of several classes. Here are some examples:

GMP::Z.new #=> 0 (default) GMP::Z.new(1)#=> 1 (Ruby Fixnum) GMP::Z.new("127") #=> 127 (Ruby String) GMP::Z.new(4294967296)

#=> 4294967296 (Ruby Bignum)

GMP::Z.new(GMP::Z.new(31)) #=> 31 (GMP Integer)

There is also a convenience method available, GMP::Z().

Converting Integers 7.2

 $to_{-}d$ $integer.to_d \rightarrow float$

Returns integer as an Float if integer fits in a Float.

Otherwise returns the least significant part of integer, with the same sign as

If integer is too big to fit in a Float, the returned result is probably not very useful. To find out if the value will fit, use the function mpz_fits_slong_p (Unimplemented).

to_i $integer.to_i \rightarrow fixnum$

Returns integer as a Fixnum if integer fits in a Fixnum.

Otherwise returns the least significant part of *integer*, with the same sign as integer.

If integer is too big to fit in a Fixnum, the returned result is probably not very useful. To find out if the value will fit, use the function mpz_fits_slong_p (Unimplemented).

to_s

 $integer.to_s(base = 10) \rightarrow str$

Converts *integer* to a string of digits in base *base*. The *base* argument may vary from 2 to 62 or from -2 to -36, or be a symbol, one of *:bin*, *:oct*, *:dec*, or *:hex*.

For base in the range 2..36, digits and lower-case letters are used; for -2..-36 (and :bin, :oct, :dec, and :hex), digits and upper-case letters are used; for 37..62, digits, upper-case letters, and lower-case letters (in that significance order) are used. Here are some examples:

```
GMP::Z(1).to_s #=> "1"

GMP::Z(32).to_s(2) #=> "100000"

GMP::Z(32).to_s(4) #=> "200"

GMP::Z(10).to_s(16) #=> "a"

GMP::Z(10).to_s(-16) #=> "A"

GMP::Z(255).to_s(:bin) #=> "11111111"

GMP::Z(255).to_s(:oct) #=> "377"

GMP::Z(255).to_s(:dec) #=> "255"

GMP::Z(255).to_s(:hex) #=> "ff"
```

7.3 Integer Arithmetic

+

 $integer + numeric \rightarrow numeric$

Returns the sum of *integer* and *numeric*. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *GMP::Q*, *GMP::F*, or *Bignum*.

add!

 $integer.add!(numeric) \rightarrow numeric$

Sums integer and numeric, in place. numeric can be an instance of GMP::Z, Fixnum, GMP::Q, GMP::F, or Bignum.

 $integer - numeric \rightarrow numeric$ $integer.sub!(numeric) \rightarrow numeric$

Returns the difference of *integer* and *numeric*. The destructive method calculates the difference in place. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *GMP::Q*, *GMP::F*, or *Bignum*. Here are some examples:

```
seven = GMP::Z(7)
nine
     = GMP::Z(9)
half
     = GMP::Q(1,2)
      = GMP::F("3.14")
рi
nine - 5
               #=> 4 (GMP Integer)
nine - seven
               #=> 2 (GMP Integer)
nine - (2**32) #=> -4294967287 (GMP Integer)
nine - nine
               #=> 0 (GMP Integer)
nine - half
               #=> 8.5 (GMP Rational)
nine - pi
               #=> 5.86 (GMP Float)
```

*

 $integer*numeric \rightarrow numeric$ $integer.mul(numeric) \rightarrow numeric$ $integer.mul!(numeric) \rightarrow numeric$

Returns the product of *integer* and *numeric*. The destructive method calculates the product in place. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *GMP::Q*, *GMP::F*, or *Bignum*.

<< $integer << numeric \rightarrow integer$

Returns *integer* times 2 to the *numeric* power. This can also be defined as a left shift by *numeric* bits.

 $\begin{array}{ccc} \textbf{-} @ & & & \\ & & integer. \mathrm{neg} \\ & & integer. \mathrm{neg}! \end{array}$

Returns the negation, the additive inverse, of *integer*. The destructive method negates in place.

 $\begin{array}{c} \textbf{abs} \\ \textbf{integer.abs} \\ \textbf{integer.abs!} \end{array}$

Returns the absolute value of *integer*. The destructive method calculates the absolute value in place.

7.4 Integer Division

tdiv

 $integer.tdiv(numeric) \rightarrow integer$

Returns the division of *integer* by *numeric*, truncated. *numeric* can be an instance of GMP :: Z, Fixnum, Bignum. The return object's class is always GMP :: Z.

fdiv

 $integer.fdiv(numeric) \rightarrow integer$

Returns the division of *integer* by *numeric*, floored. *numeric* can be an instance of GMP :: Z, Fixnum, Bignum. The return object's class is always GMP :: Z.

cdiv

 $integer.cdiv(numeric) \rightarrow integer$

Returns the ceiling division of *integer* by *numeric*. *numeric* can be an instance of GMP :: Z, Fixnum, Bignum. The return object's class is always GMP :: Z.

tmod

 $integer.tmod(numeric) \rightarrow integer$

Returns the remainder after truncated division of *integer* by *numeric*. *numeric* can be an instance of GMP :: Z, Fixnum, or Bignum. The return object's class is always GMP :: Z.

fmod

 $integer. \texttt{fmod}(numeric) \rightarrow integer$

Returns the remainder after floored division of integer by numeric. numeric can be an instance of GMP :: Z, Fixnum, or Bignum. The return object's class is always GMP :: Z.

cmod

 $integer.cmod(numeric) \rightarrow integer$

Returns the remainder after ceilinged division of integer by numeric. numeric can be an instance of GMP :: Z, Fixnum, or Bignum. The return object's class is always GMP :: Z.

%

 $integer \% numeric \rightarrow integer$

Returns integer modulo numeric. numeric can be an instance of GMP::Z, Fixnum, or Bignum. The return object's class is always GMP::Z.

7.5 Integer Roots

root

 $integer.root(numeric) \rightarrow numeric$

Returns the integer part of the numeric'th root of integer.

sqrt

 $integer.sqrt \rightarrow numeric$ $integer.sqrt!(numeric) \rightarrow numeric$

Returns the truncated integer part of the square root of *integer*.

sqrtrem

 $integer.sqrtrem \rightarrow sqrt, rem$

Returns the truncated integer part of the square root of integer as sqrt and the remainder, integer - sqrt * sqrt, as rem, which will be zero if integer is a perfect square.

power?

 $integer.power? \rightarrow true \mid false$

Returns true if integer is a perfect power, i.e., if there exist integers a and b, with b > 1, such that integer equals a raised to the power b.

Under this definition both 0 and 1 are considered to be perfect powers. Negative values of integers are accepted, but of course can only be odd perfect powers.

square?

 $integer.square? \rightarrow true \mid false$

Returns true if integer is a perfect square, i.e., if the square root of integer is an integer. Under this definition both 0 and 1 are considered to be perfect squares.

7.6 Integer Exponentiation

**

 $integer ** numeric \rightarrow numeric$ $integer.pow(numeric) \rightarrow numeric$

Returns integer raised to the numeric power.

powmod

 $integer.powmod(exp, mod) \rightarrow integer$

Returns integer raised to the exp power, modulo mod. Negative exp is supported if an inverse, $integer^{-1}$ modulo mod, exists. If an inverse doesn't exist then a divide by zero exception is raised.

7.7 Number Theoretic Functions

is_probab_prime?

 $integer.is_probab_prime?(reps = 5) \rightarrow 0, 1, or 2$

Determine whether *integer* is prime. Returns 2 if *integer* is definitely prime, returns 1 if *integer* is probably prime (without being certain), or returns 0 if *integer* is definitely composite.

This function does some trial divisions, then some Miller-Rabin probabilistic primality tests. *reps* controls how many such tests are done, 5 to 10 is a reasonable number, more will reduce the chances of a composite being returned as probably prime.

Miller-Rabin and similar tests can be more properly called compositeness tests. Numbers which fail are known to be composite but those which pass might be prime or might be composite. Only a few composites pass, hence those which pass are considered probably prime.

$next_prime$

```
integer.next\_prime \rightarrow prime integer.next\_prime! \rightarrow prime integer.next\_prime! \rightarrow prime integer.nextprime! \rightarrow prime
```

Returns the next prime greater than *integer*. The destructive method sets *integer* to the next prime greater than *integer*.

This function uses a probabilistic algorithm to identify primes. For practical purposes it's adequate, the chance of a composite passing will be extremely small.

gcd

```
a.\gcd(b) \to g
```

Computes the greatest common divisor of a and b. g will always be positive, even if a or b is negative. b can be an instance of GMP::Z, Fixnum, or Biqnum.

```
GMP::Z(24).gcd(GMP::Z(8)) #=> GMP::Z(8)

GMP::Z(24).gcd(8) #=> GMP::Z(8)

GMP::Z(24).gcd(2**32) #=> GMP::Z(8)
```

invert

```
a.invert(m) \rightarrow integer
```

Computes the inverse of $a \mod m$. m can be an instance of GMP::Z, Fixnum, or Bignum.

```
GMP::Z(2).invert(GMP::Z(11)) #=> GMP::Z(6)
GMP::Z(3).invert(11) #=> GMP::Z(4)
GMP::Z(5).invert(11) #=> GMP::Z(9)
```

jacobi $a.\mathrm{jacobi}(b) \rightarrow integer$ GMP::Z.jacobi $(a, b) \rightarrow integer$ Returns the Jacobi symbol (a/b). This is defined only for b odd. If b is even, a range exception will be raised. GMP::Z.jacobi (the instance method) requires b to be an instance of GMP::Z. GMP::Z#jacobi (the class method) requires a and b each to be an instance of GMP::Z, Fixnum, or Bignum. legendre $a.\operatorname{legendre}(b) \to integer$ Returns the Legendre symbol (a/b). This is defined only for p an odd positive prime. If p is even, negative, or composite, a range exception will be raised. $n.remove(factor) \rightarrow (integer, times)$ remove Remove all occurrences of the factor factor from n. factor can be an instance of GMP::Z, Fixnum, or Bignum. integer is the resulting integer, an instance of GMP::Z. times is how many times factor was removed, a Fixnum. fac $GMP::Z.fac(n) \rightarrow integer$ Returns n!, or, n factorial. fib $GMP::Z.fib(n) \rightarrow integer$ Returns F[n], or, the *n*th Fibonacci number. Integer Logic and Bit Fiddling 7.8and $a \& b \rightarrow integer$ Returns integer, the bitwise and of a and b. ior $a \mid b \rightarrow integer$ Returns integer, the bitwise inclusive or of a and b.

Returns integer, the bitwise exclusive or of a and b.

xor

 $a \hat{b} \rightarrow integer$

scan0 $n.scan0(i) \rightarrow integer$

Scans n, starting from bit i, towards more significant bits, until the first 0 bit is found. Return the index of the found bit.

If the bit at i is already what's sought, then i is returned.

If there's no bit found, then $INT2FIX(ULONG_MAX)$ is returned. This will happen in scan0 past the end of a negative number.

8 Rational Functions

8.1 Initializing, Assigning Rationals

```
 \begin{aligned} \text{GMP::Q.new} & \text{GMP::Q.new} \rightarrow \textit{rational} \\ \text{GMP::Q.new}(\textit{numerator} = 0, \textit{denominator} = 1) \rightarrow \textit{rational} \\ \text{GMP::Q.new}(\textit{str}) \rightarrow \textit{rational} \end{aligned}
```

This method creates a new GMP::Q rational number. It takes two optional arguments for the value of the numerator and denominator. These arguments can each be an instance of several classes. Here are some examples:

```
GMP::Q.new #=> 0 (default)
GMP::Q.new(1) #=> 1 (Ruby Fixnum)
GMP::Q.new(1,3) #=> 1/3 (Ruby Fixnums)
GMP::Q.new("127") #=> 127 (Ruby String)
GMP::Q.new(4294967296) #=> 4294967296 (Ruby Bignum)
GMP::Q.new(GMP::Z.new(31)) #=> 31 (GMP Integer)
```

There is also a convenience method available, GMP::Q().

9 Random Number Functions

9.1 Random State Initialization

new

GMP::RandState.new \rightarrow mersenne twister state GMP::RandState.new(:default) \rightarrow mersenne twister state GMP::RandState(:mt) \rightarrow mersenne twister random state GMP::RandState.new(:lc_2exp, a, c, m2exp) \rightarrow linear congruential state GMP::RandState.new(:lc_2exp_size, size) \rightarrow linear congruential state

This method creates a new GMP::RandState instance. The first argument defaults to :default (also :mt), which initializes the GMP::RandState for a Mersenne Twister algorithm. No other arguments should be given if :default or :mt is specified.

If the first argument given is $:lc_2exp$, then the GMP::RandState is initialized for a linear congruential algorithm. $:lc_2exp$ must be followed with a, c, and m2exp. The algorithm can then proceed as $(X = (a * X + c) \mod 2^{m2exp})$.

GMP::RandState can also be initialized for a linear congruential algorithm with $:lc_2exp_size$. This initializer instead takes just one argument, size. a, c, and m2exp are then chosen from a table, with m2exp/2 > size. The maximum size currently supported is 128.

GMP::RandState.new

GMP::RandState.new(:mt)

GMP::RandState.new(:lc_2exp, 1103515245, 12345, 15) #=> Perl's

old rand()

GMP::RandState.new(:lc_2exp, 25_214_903_917, 11, 48) #=> drand48

9.2 Random State Seeding

seed

 $state.seed(integer) \rightarrow integer$

Set an initial seed value into *state*. *integer* can be an instance of *GMP::Z*, *Fixnum*, or *Bignum*.

9.3 Integer Random Numbers

urandomb

 $state.urandomb(n) \rightarrow integer$

Generates a uniformly distributed random integer in the range 0 to $2^n - 1$, inclusive.

urandomm

 $state.urandomm(n) \rightarrow integer$

Generates a uniformly distributed random integer in the range 0 to n-1, inclusive. n can be an instance of GMP::Z, Fixnum, or Bignum.