gmp

Ruby bindings to the GMP library Edition 0.6.7 9 December 2012

written by Sam Rawlins with extensive quoting from the GMP Manual

This manual describes how to use the gmp Ruby gem, which provides bindings to the GNU multiple precision arithmetic library, version 4.3.x or 5.0.x.

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1 Introduction to GNU MP

This entire page is copied verbatim from the GMP Manual.

GNU MP is a portable library written in C for arbitrary precision arithmetic on integers, rational numbers, and floating-point numbers. It aims to provide the fastest possible arithmetic for all applications that need higher precision than is directly supported by the basic C types.

Many applications use just a few hundred bits of precision; but some applications may need thousands or even millions of bits. GMP is designed to give good performance for both, by choosing algorithms based on the sizes of the operands, and by carefully keeping the overhead at a minimum.

The speed of GMP is achieved by using fullwords as the basic arithmetic type, by using sophisticated algorithms, by including carefully optimized assembly code for the most common inner loops for many different CPUs, and by a general emphasis on speed (as opposed to simplicity or elegance).

There is assembly code for these CPUs: ARM, DEC Alpha 21064, 21164, and 21264, AMD 29000, AMD K6, K6-2, Athlon, and Athlon64, Hitachi SuperH and SH-2, HPPA 1.0, 1.1, and 2.0, Intel Pentium, Pentium Pro/II/III, Pentium 4, generic x86, Intel IA-64, i960, Motorola MC68000, MC68020, MC88100, and MC88110, Motorola/IBM PowerPC 32 and 64, National NS32000, IBM POWER, MIPS R3000, R4000, SPARCv7, SuperSPARC, generic SPARCv8, UltraSPARC, DEC VAX, and Zilog Z8000. Some optimizations also for Cray vector systems, Clipper, IBM ROMP (RT), and Pyramid AP/XP.

For up-to-date information on GMP, please see the GMP web pages at http://gmplib.org/

The latest version of the library is available at ftp://ftp.gnu.org/gnu/gmp/

Many sites around the world mirror 'ftp.gnu.org', please use a mirror near you, see http://www.gnu.org/order/ftp.html for a full list.

There are three public mailing lists of interest. One for release announcements, one for general questions and discussions about usage of the GMP library, and one for bug reports. For more information, see http://gmplib.org/mailman/listinfo/.

The proper place for bug reports is gmp-bugs@gmplib.org. See Chapter 4 [Reporting Bugs], page 28 for information about reporting bugs.

2 Introduction to MPFR

The gmp gem optionally interacts with the MPFR library as well. This entire page is copied verbatim from the MPFR manual.

The MPFR library is a C library for multiple-precision floating-point computations with correct rounding. MPFR has continuously been supported by the INRIA and the current main authors come from the Caramel and Arnaire project-teams at Loria (Nancy, France) and LIP (Lyon, France) respectively; see more on the credit page. MPFR is based on the GMP multiple-precision library.

The main goal of MPFR is to provide a library for multiple-precision floating-point computation which is both efficient and has a well-defined semantics. It copies the good ideas from the ANSI/IEEE-754 standard for double-precision floating-point arithmetic (53-bit mantissa).

MPFR is free. It is distributed under the GNU Lesser General Public License (GNU Lesser GPL), version 3 or later (2.1 or later for MPFR versions until 2.4.x). The library has been registered in France by the Agence de Protection des Programmes under the number IDDN FR 001 120020 00 R P 2000 000 10800, on 15 March 2000. This license guarantees your freedom to share and change MPFR, to make sure MPFR is free for all its users. Unlike the ordinary General Public License, the Lesser GPL enables developers of non-free programs to use MPFR in their programs. If you have written a new function for MPFR or improved an existing one, please share your work!

3 Introduction to the gmp gem

The gmp Ruby gem is a Ruby library that provides bindings to GMP. The gem is incomplete, and will likely only include a subset of the GMP functions. It is built as a C extension for Ruby, interacting with gmp.h. The gmp gem is not endorsed or supported by GNU or the GMP team (or MPFR team). The gmp gem also does not ship with GMP (or MPFR), so GMP (and MPFR) must be compiled separately.

4 Installing the gmp gem

4.1 Prerequisites

OK. First, we've got a few requirements. To install the gmp gem, you need one of the following versions of Ruby:

- (MRI) Ruby 1.8.6 tested lightly.
- (MRI) Ruby 1.8.7 tested seriously.
- (MRI) Ruby 1.9.1 tested seriously.
- (MRI) Ruby 1.9.2 tested seriously.
- (REE) Ruby 1.8.7 tested lightly.
- (RBX) Rubinius 1.1 tested lightly.

As you can see only Matz's Ruby Interpreter (MRI) is seriously supported. I've just started to poke around with REE. Everything seems to work on REE 1.8.7 on Linux, x86 and x86_64. Also, Rubinius 1.1 seems to work great on Linux, but support won't be official until Rubinius 1.1.1.

Next is the platform, the combination of the architecture (processor) and OS. As far as I can tell, if you can compile GMP and Ruby (and optionally MPFR) on a given platform, you can use the gmp gem there too. Please report problems with that hypothesis.

Lastly, GMP (and MPFR). GMP (and MPFR) must be compiled and working. "And working" means you ran "make check" after compiling GMP (and MPFR), and it 'check's out. The following versions of GMP (and MPFR) have been tested:

- GMP 4.3.1 (with MPFR 2.4.2)
- GMP 4.3.2 (with MPFR 2.4.2 and 3.0.0)
- GMP 5.0.0 (with MPFR 3.0.0)
- GMP 5.0.1 (with MPFR 3.0.0)

That's all. I don't intend to test any older versions.

Here is a table of the exact environments on which I have tested the gmp gem. The (MPFR) version denotes that the gmp gem was tested both with and without the given version of MPFR:

Platform	Ruby	GMP	(MPFR)
Linux (Ubuntu NR 10.04) on x86 (32-bit)	(MRI) Ruby 1.8.7	GMP 4.3.2	(2.4.2)
	(MRI) Ruby 1.8.7	GMP 5.0.1	(3.0.0)
	(MRI) Ruby 1.9.1	GMP 4.3.2	(2.4.2)
	(MRI) Ruby 1.9.1	GMP 5.0.1	(3.0.0)
	(MRI) Ruby 1.9.2	GMP $4.3.2$	(2.4.2)
	(MRI) Ruby 1.9.2	GMP $5.0.1$	(3.0.0)
	(RBX) Rubinius 1.1	GMP $4.3.2$	(2.4.2)
	(RBX) Rubinius 1.1	GMP 5.0.1	(3.0.0)
Linux (Ubuntu 10.04) on x86_64 (64-bit)	(MRI) Ruby 1.8.7	GMP $4.3.2$	(2.4.2)
	(MRI) Ruby 1.8.7	GMP $5.0.1$	(3.0.0)
	(MRI) Ruby 1.9.1	GMP $4.3.2$	(2.4.2)
	(MRI) Ruby 1.9.1	GMP $5.0.1$	(3.0.0)
	(MRI) Ruby 1.9.2	GMP 4.3.2	(2.4.2)
	(MRI) Ruby 1.9.2	GMP $5.0.1$	(3.0.0)
	(RBX) Rubinius 1.1	GMP $4.3.2$	(2.4.2)
	(RBX) Rubinius 1.1	GMP 5.0.1	(3.0.0)
Mac OS X 10.6.4 on x86_64 (64-bit)	(MRI) Ruby 1.8.7	GMP $4.3.2$	(2.4.2)
	(MRI) Ruby 1.8.7	GMP 5.0.1	(3.0.0)
	(MRI) Ruby 1.9.1	GMP $4.3.2$	(2.4.2)
	(MRI) Ruby 1.9.1	GMP $5.0.1$	(3.0.0)
	(MRI) Ruby 1.9.2	GMP $4.3.2$	(2.4.2)
	(MRI) Ruby 1.9.2	GMP 5.0.1	(3.0.0)
	(RBX) Rubinius 1.1	GMP 4.3.2	(2.4.2)
	(RBX) Rubinius 1.1	GMP 5.0.1	(3.0.0)
Windows 7 on x86_64 (64-bit)	(MRI) Ruby 1.8.7	GMP $4.3.2$	(2.4.2)
	(MRI) Ruby 1.8.7	GMP 5.0.1	(3.0.0)
	(MRI) Ruby 1.9.1	GMP 4.3.2	(2.4.2)
	(MRI) Ruby 1.9.1	GMP 5.0.1	(3.0.0)
	(MRI) Ruby 1.9.2	GMP 4.3.2	(2.4.2)
	(MRI) Ruby 1.9.2	GMP 5.0.1	(3.0.0)
Windows XP on x86 (32-bit)	(MRI) Ruby 1.9.1	GMP 4.3.2	(2.4.2)
	(MRI) Ruby 1.9.1	GMP 5.0.1	(3.0.0)

In addition, I $used\ to\ test$ on the following environments, in versions 0.4.7 and earlier of the gmp gem:

Platform	Ruby	GMP
Cygwin on x86	(MRI) Ruby 1.8.7	GMP 4.3.1
Linux (LinuxMint 7) on x86	(MRI) Ruby 1.8.7	GMP 4.3.1
Mac OS X 10.5.7 on x86 (32-bit)	(MRI) Ruby 1.8.6	GMP 4.3.1
Mac OS X 10.5.7 on x86 (32-bit)	(MRI) Ruby 1.9.1	GMP 4.3.1

4.2 Installing

You may clone the gmp gem's git repository with:

git clone git://github.com/srawlins/gmp.git

Or you may install the gem from gemcutter (rubygems.org):

gem install gmp

At this time, the gem self-compiles. If required libraries cannot be found, you may compile the C extensions manually with:

```
cd <gmp gem directory>/ext
ruby extconf.rb
make
```

There shouldn't be any errors, or warnings.

5 Testing the gmp gem

Testing the gmp gem is quite simple. The test/unit_tests.rb suite uses Unit::Test. You can run this test suite with:

```
cd <gmp gem directory>/test
ruby unit_tests.rb
```

All tests should pass. If you don't have the test-unit gem installed, then you may run into one error. It would look like:

1) Error:

```
test_z_div(TC_division):
TypeError: GMP::Q can't be coerced into Float
C:/Ruby191/devkit/msys/1.0.11/projects/gmp_gem/test/tc_division.rb:18:in 'test_z_div'
```

6 GMP and gmp gem basics

6.1 Classes

The gmp gem includes the namespace GMP and four classes within GMP:

- GMP::Z Methods for signed integer arithmetic. There are about 64 methods here.
- GMP::Q Methods for rational number arithmetic. There are at least 11 methods here (still accounting).
- GMP::F Methods for floating-point arithmetic. There are at least 6 methods here (still accounting).
- GMP::RandState Methods for random number generation. There are 3 methods here.

In addition to the above four classes, there are also four constants within GMP:

- GMP::GMP_VERSION The version of GMP linked into the gmp gem
- GMP::GMP_CC The compiler that compiled GMP linked into the gmp gem
- GMP::GMP_CFLAGS The compiler flags used to compile GMP linked into the gmp gem
- GMP::GMP_BITS_PER_LIMB The number of bits per limb
- GMP::GMP_NUMB_MAX The maximum value that can be stored in the number part of a limb.

7 MPFR basics

The gmp gem can optionally link to MPFR, the Multiple Precision Floating-Point Reliable Library. The x86-mswin32 version of the gmp gem comes with MPFR. This library uses the floating-point type from GMP, and thus the MPFR functions mapped in the gmp gem become methods in GMP::F.

There are additional constants within GMP when MPFR is linked:

- GMP::MPFR_VERSION The version of MPFR linked into the gmp gem.
- GMP::MPFR_PREC_MIN The minimum precision available.
- GMP::MPFR_PREC_MAX The maximum precision available
- GMP::GMP_RNDN Rounding mode representing "round to nearest."
- GMP::GMP_RNDZ Rounding mode representing "round toward zero."
- GMP::GMP_RNDU Rounding mode representing "round toward positive infinity."
- GMP::GMP_RNDD Rounding mode representing "round toward negative infinity."
- GMP::MPFR_RNDN Rounding mode representing "round to nearest." (MPFR version 3.0.0 or higher only)
- GMP::MPFR_RNDZ Rounding mode representing "round toward zero." (MPFR version 3.0.0 or higher only)
- GMP::MPFR_RNDU Rounding mode representing "round toward positive infinity." (MPFR version 3.0.0 or higher only)
- GMP::MPFR_RNDD Rounding mode representing "round toward negative infinity." (MPFR version 3.0.0 or higher only)
- GMP::MPFR_RNDZ Rounding mode representing "round away from zero." (MPFR version 3.0.0 or higher only)

8 Integer Functions

8.1 Initializing, Assigning Integers

This method creates a new *GMP::Z* integer. It typically takes one optional argument for the value of the integer. This argument can be one of several classes. If the first argument is a String, then a second argument, the base, may be optionally supplied. Here are some examples:

```
GMP::Z.new #=> 0 (default)
GMP::Z.new(1) #=> 1 (Ruby Fixnum)
GMP::Z.new("127") #=> 127 (Ruby String)
GMP::Z.new("FF", 16) #=> 255 (Ruby String with base)
GMP::Z.new("1Z", 36) #=> 71 (Ruby String with base)
GMP::Z.new(4294967296) #=> 4294967296 (Ruby Bignum)
GMP::Z.new(GMP::Z.new(31)) #=> 31 (GMP Integer)
```

There is also a convenience method available, GMP::Z().

8.2 Converting Integers

 to_d $integer.to_d \rightarrow float$

Returns integer as an Float if integer fits in a Float.

Otherwise returns the least significant part of integer, with the same sign as integer.

If *integer* is too big to fit in a Float, the returned result is probably not very useful. To find out if the value will fit, use the function $mpz_fits_slong_p$ (**Unimplemented**).

 to_{-i} $integer.to_{-i} \rightarrow fixnum$

Returns integer as a Fixnum if integer fits in a Fixnum.

Otherwise returns the least significant part of *integer*, with the same sign as *integer*.

If *integer* is too big to fit in a *Fixnum*, the returned result is probably not very useful. To find out if the value will fit, use the function *mpz_fits_slong_p* (**Unimplemented**).

to_s

 $integer.to_s(base = 10) \rightarrow str$

Converts *integer* to a string of digits in base *base*. The *base* argument may vary from 2 to 62 or from -2 to -36, or be a symbol, one of *:bin*, *:oct*, *:dec*, or *:hex*.

For base in the range 2..36, digits and lower-case letters are used; for -2..-36 (and :bin, :oct, :dec, and :hex), digits and upper-case letters are used; for 37..62, digits, upper-case letters, and lower-case letters (in that significance order) are used. Here are some examples:

```
GMP::Z(1).to_s #=> "1"

GMP::Z(32).to_s(2) #=> "100000"

GMP::Z(32).to_s(4) #=> "200"

GMP::Z(10).to_s(16) #=> "a"

GMP::Z(10).to_s(-16) #=> "A"

GMP::Z(255).to_s(:bin) #=> "11111111"

GMP::Z(255).to_s(:oct) #=> "377"

GMP::Z(255).to_s(:dec) #=> "255"

GMP::Z(255).to_s(:hex) #=> "ff"
```

8.3 Integer Arithmetic

+

 $integer + numeric \rightarrow numeric$

Returns the sum of *integer* and *numeric*. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *GMP::Q*, *GMP::F*, or *Bignum*.

add!

 $integer.add!(numeric) \rightarrow numeric$

Sums integer and numeric, in place. numeric can be an instance of GMP::Z, Fixnum, GMP::Q, GMP::F, or Bignum.

integer - $numeric \rightarrow numeric$ $integer.sub!(numeric) \rightarrow numeric$

Returns the difference of *integer* and *numeric*. The destructive method calculates the difference in place. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *GMP::Q*, *GMP::F*, or *Bignum*. Here are some examples:

```
seven = GMP::Z(7)
nine
     = GMP::Z(9)
half
     = GMP::Q(1,2)
      = GMP::F("3.14")
рi
nine - 5
               #=> 4 (GMP Integer)
nine - seven
               #=> 2 (GMP Integer)
nine - (2**32) #=> -4294967287 (GMP Integer)
nine - nine
               #=> 0 (GMP Integer)
nine - half
               #=> 8.5 (GMP Rational)
nine - pi
               #=> 5.86 (GMP Float)
```

* $integer * numeric \rightarrow numeric \\ integer.mul(numeric) \rightarrow numeric \\ integer.mul!(numeric) \rightarrow numeric \\$

Returns the product of *integer* and *numeric*. The destructive method calculates the product in place. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *GMP::Q*, *GMP::F*, or *Bignum*.

addmul! $integer.addmul!(b, c) \rightarrow numeric$

Sets integer to the sum of integer and the product of b and c. This destructive method calculates the result in place. Both b and c can be an instance of GMP::Z, Fixnum, or Bignum.

submul! $integer.submul!(b, c) \rightarrow numeric$

Sets integer to the difference of integer and the product of b and c. This destructive method calculates the result in place. Both b and c can be an instance of GMP::Z, Fixnum, or Bignum.

<< integer <<numeric \rightarrow integer

Returns *integer* times 2 to the *numeric* power. This can also be defined as a left shift by *numeric* bits.

 $\begin{array}{ccc} \textbf{-}@ & & -integer \\ & integer. \mathrm{neg} \\ & integer. \mathrm{neg}! \end{array}$

Returns the negation, the additive inverse, of *integer*. The destructive method negates in place.

 $\begin{array}{c} \text{abs} \\ \text{integer.abs} \\ \text{integer.abs}. \end{array}$

Returns the absolute value of *integer*. The destructive method calculates the absolute value in place.

8.4 Integer Division

tdiv $integer.tdiv(numeric) \rightarrow integer$

Returns the division of *integer* by *numeric*, truncated. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *Bignum*. The return object's class is always *GMP::Z*.

fdiv $integer.fdiv(numeric) \rightarrow integer$

Returns the division of *integer* by *numeric*, floored. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *Bignum*. The return object's class is always *GMP::Z*.

 $cdiv \qquad \qquad integer.cdiv(numeric) \rightarrow integer$

Returns the ceiling division of *integer* by *numeric*. *numeric* can be an instance of *GMP::Z*, *Fixnum*, *Bignum*. The return object's class is always *GMP::Z*.

tmod $integer.tmod(numeric) \rightarrow integer$

Returns the remainder after truncated division of *integer* by *numeric*. *numeric* can be an instance of GMP::Z, Fixnum, or Bignum. The return object's class is always GMP::Z.

fmod $integer.fmod(numeric) \rightarrow integer$

Returns the remainder after floored division of *integer* by *numeric*. numeric can be an instance of GMP::Z, Fixnum, or Bignum. The return object's class is always GMP::Z.

 \mathbf{cmod} $integer.\mathbf{cmod}(numeric) \rightarrow integer$

Returns the remainder after ceilinged division of *integer* by *numeric*. *numeric* can be an instance of GMP::Z, Fixnum, or Bignum. The return object's class is always GMP::Z.

% integer % numeric \rightarrow integer

Returns integer modulo numeric. numeric can be an instance of GMP::Z, Fixnum, or Bignum. The return object's class is always GMP::Z.

divisible?

integer.divisible? $numeric \rightarrow boolean$

Returns whether integer is divisible by $numeric.\ numeric$ can be an instance of $GMP::Z,\ Fixnum,$ or Bignum.

8.5 Integer Exponentiation

**

 $integer ** numeric \rightarrow numeric$

 $integer.pow(numeric) \rightarrow numeric$

GMP::Z.pow(integer, numeric) \rightarrow numeric

Returns integer raised to the numeric power. In the singleton method (GMP::Z.pow()), integer can be either a GMP::Z, Fixnum, Bignum, or String.

powmod

 $integer.powmod(exp, mod) \rightarrow integer$

Returns integer raised to the exp power, modulo mod. Negative exp is supported if an inverse, $integer^{-1}$ modulo mod, exists. If an inverse doesn't exist then a divide by zero exception is raised.

8.6 Integer Roots

root

 $integer.root(numeric) \rightarrow numeric$

Returns the integer part of the numeric'th root of integer.

sqrt

 $integer.sqrt \rightarrow numeric$ $integer.sqrt! \rightarrow numeric$

Returns the truncated integer part of the square root of *integer*.

sqrtrem

 $integer.sqrtrem \rightarrow sqrt, rem$

Returns the truncated integer part of the square root of integer as sqrt and the remainder, integer - sqrt * sqrt, as rem, which will be zero if integer is a perfect square.

power?

 $integer.power? \rightarrow true \mid false$

Returns true if *integer* is a perfect power, i.e., if there exist integers a and b, with b > 1, such that *integer* equals a raised to the power b.

Under this definition both 0 and 1 are considered to be perfect powers. Negative values of integers are accepted, but of course can only be odd perfect powers.

square?

 $integer.square? \rightarrow true \mid false$

Returns true if *integer* is a perfect square, i.e., if the square root of *integer* is an integer. Under this definition both 0 and 1 are considered to be perfect squares.

8.7 Number Theoretic Functions

probab_prime?

 $integer.probab_prime?(reps = 5) \rightarrow 0, 1, or 2$

Determine whether *integer* is prime. Returns 2 if *integer* is definitely prime, returns 1 if *integer* is probably prime (without being certain), or returns 0 if *integer* is definitely composite.

This function does some trial divisions, then some Miller-Rabin probabilistic primality tests. *reps* controls how many such tests are done, 5 to 10 is a reasonable number, more will reduce the chances of a composite being returned as probably prime.

Miller-Rabin and similar tests can be more properly called compositeness tests. Numbers which fail are known to be composite but those which pass might be prime or might be composite. Only a few composites pass, hence those which pass are considered probably prime.

next_prime

 $\begin{array}{c} integer. {\tt next_prime} \to prime \\ integer. {\tt next_prime!} \to prime \\ integer. {\tt next_prime!} \to prime \\ integer. {\tt next_prime!} \to prime \end{array}$

Returns the next prime greater than *integer*. The destructive method sets *integer* to the next prime greater than *integer*.

This function uses a probabilistic algorithm to identify primes. For practical purposes it's adequate, the chance of a composite passing will be extremely small.

gcd

 $a.\gcd(b) \to g$

Computes the greatest common divisor of a and b. g will always be positive, even if a or b is negative. b can be an instance of GMP::Z, Fixnum, or Biqnum.

GMP::Z(24).gcd(GMP::Z(8)) #=> GMP::Z(8)

GMP::Z(24).gcd(8) #=> GMP::Z(8) GMP::Z(24).gcd(2**32) #=> GMP::Z(8)

gcdext

 $a.\gcd(b) \to g, s, t$

Computes the greatest common divisor of a and b, in addition to s and t, the coefficients satisfying a*s+b*t=g. g will always be positive, even if a or b is negative. s and t are chosen such that |s| <= |b| and |t| <= |a|. b can be an instance of GMP::Z, Fixnum, or Bignum.

invert

 $a.invert(m) \rightarrow integer$

Computes the inverse of $a \mod m$. m can be an instance of GMP::Z, Fixnum, or Bignum.

GMP::Z(2).invert(GMP::Z(11)) #=> GMP::Z(6)

GMP::Z(3).invert(11) #=> GMP::Z(4)GMP::Z(5).invert(11) #=> GMP::Z(9)

jacobi GMP::Z.jacobi $(a, b) \rightarrow integer$

 $a.\mathrm{jacobi}(b) \rightarrow integer$

Returns the Jacobi symbol (a/b). This is defined only for b odd. If b is even, a range exception will be raised.

GMP::Z.jacobi (the instance method) requires b to be an instance of GMP::Z. GMP::Z#jacobi (the class method) requires a and b each to be an instance of GMP::Z, Fixnum, or Bignum.

legendre

 $a.\operatorname{legendre}(b) \to integer$

Returns the Legendre symbol (a/b). This is defined only for p an odd positive prime. If p is even, negative, or composite, a range exception will be raised.

remove

 $n.\text{remove}(factor) \rightarrow (integer, times)$

Remove all occurrences of the factor factor from n. factor can be an instance of GMP::Z, Fixnum, or Bignum. integer is the resulting integer, an instance of GMP::Z. times is how many times factor was removed, a Fixnum.

fac

 $GMP::Z.fac(n) \rightarrow integer$

Returns n!, or, n factorial.

fib

 $GMP::Z.fib(n) \rightarrow integer$

Returns F[n], or, the *n*th Fibonacci number.

8.8 **Integer Comparisons**

<=>

 $a \iff b \implies fixnum$

Returns a negative Fixnum if a is less than b.

Returns 0 if a is equal to b.

Returns a positive Fixnum if a is greater than b.

<

 $a < b \rightarrow boolean$

Returns true if a is less than b.

<=		$a <= b \rightarrow boolean$
	Returns true if a is less than or equal to b .	
==	·	$a == b \to boolean$
	Returns true if a is equal to b .	
		. 1 . 1 1
>=	Determine the state of the stat	$a >= b \rightarrow boolean$
	Returns true if a is greater than or equal to b .	
>		$a > b \rightarrow boolean$
	Returns true if a is greater than b .	
cmpabs		$mpabs(b) \to fixnum$
	Returns a negative Fixnum if $abs(a)$ is less than $abs(b)$.	
	Returns 0 if $abs(a)$ is equal to $abs(b)$. Returns a positive Fixnum if $abs(a)$ is greater than $abs(b)$.	
	1000ating a positive i initial if abs(a) is greater than abs(b).	
sgn		$a.\mathrm{sgn} \to -1, 0, \text{ or } 1$
	Returns -1 if a is less than b .	
	Returns 0 if a is equal to b .	
	Returns 1 if a is greater than b .	
eql?		$a.eql?(b) \rightarrow boolean$
	Used when comparing objects as Hash keys.	
hash		$a.\text{hash} \rightarrow string$
	Used when comparing objects as Hash keys.	
8.9 Integer	er Logic and Bit Fiddling	
and		$a \& b \rightarrow integer$
	Returns $integer$, the bitwise and of a and b .	
ion		~ L
ior	Detumps interes the literal literal Control	$a \mid b \rightarrow integer$
	Returns $integer$, the bitwise inclusive or of a and b .	
xor		$a \hat{} b \rightarrow integer$
	Returns $integer$, the bitwise exclusive or of a and b .	

com

 $integer.com \rightarrow complement$ $integer.com! \rightarrow complement$

Returns the one's complement of *integer*. The destructive method sets *integer* to the one's complement of *integer*.

popcount

 $n.popcount \rightarrow fixnum$

If n >= 0, return the population count of n, which is the number of 1 bits in the binary representation. If n < 0, the number of 1s is infinite, and the return value is the largest possible mp_bitcnt_t .

scan0

 $n.scan0(i) \rightarrow integer$

Scans n, starting from bit i, towards more significant bits, until the first 0 bit is found. Return the index of the found bit.

If the bit at i is already what's sought, then i is returned.

If there's no bit found, then $INT2FIX(ULONG_MAX)$ is returned. This will happen in scan0 past the end of a negative number.

scan1

 $n.\text{scan1}(i) \rightarrow integer$

Scans n, starting from bit i, towards more significant bits, until the first 1 bit is found. Return the index of the found bit.

If the bit at i is already what's sought, then i is returned.

If there's no bit found, then $INT2FIX(ULONG_MAX)$ is returned. This will happen in scan1 past the end of a negative number.

П

 $n[bit_index] \rightarrow 0 \text{ or } 1$

Tests bit bit_index in n and return 0 or 1 accordingly.

=

 $n[bit_index] = i \rightarrow nil$

Sets bit bit_index in n to i.

8.10 Miscellaneous Integer Functions

odd? $n.odd? \rightarrow boolean$ Returns whether n is odd.even? $n.even? \rightarrow boolean$ Returns whether n is even.sizeinbase $n.sizeinbase(b) \rightarrow digits$ Returns the number of digits in base b. b can vary between 2 and 62.

Returns the number of digits in n's binary representation.

8.11 Integer Special Functions

size $integer.size \rightarrow fixnum$

Returns the size of *integer* measured in number of limbs. If *integer* is zero, then the returned value will be zero.

9 Rational Functions

9.1 Initializing, Assigning Rationals

new $GMP::Q.new \rightarrow rational$

GMP::Q.new(numerator = 0, denominator = 1) \rightarrow rational GMP::Q.new(str) \rightarrow rational

This method creates a new *GMP*:: Qrational number. It takes two optional arguments for the value of the numerator and denominator. These arguments can each be an instance of several classes. Here are some examples:

GMP::Q.new #=> 0 (default)
GMP::Q.new(1) #=> 1 (Ruby Fixnum)
GMP::Q.new(1,3) #=> 1/3 (Ruby Fixnums)
GMP::Q.new("127") #=> 127 (Ruby String)
GMP::Q.new(4294967296) #=> 4294967296 (Ruby Bignum)

GMP::Q.new(GMP::Z.new(31)) #=> 31 (GMP Integer)

There is also a convenience method available, GMP::Q().

9.2 Converting Rationals

 to_d rational.to_d \rightarrow float

Returns rational as an Float if rational fits in a Float.

Otherwise returns the least significant part of rational, with the same sign as rational.

If *rational* is too big to fit in a Float, the returned result is probably not very useful.

 to_s $rational.to_s \rightarrow str$

Converts rational to a string.

9.3 Rational Arithmetic

+ $rational + numeric \rightarrow numeric$

10 Floating-point Functions

10.1 Initializing, Assigning Floats

10.2 Floating-point Special Functions (MPFR Only)

Every method below accepts two additional parameters in addition to any required parameters. These are rnd_mode , the rounding mode to use in calculation, which defaults to $GMP::GMP_RNDN$, and res_prec , the precision of the result, which defaults to the f.prec, the precision of f.

$\log \log 2 \log 10$	$f.\log(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$ $f.\log2(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$ $f.\log10(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$ $\operatorname{Returns} \text{ the natural log, log_2, and log_1 0 of } f, \operatorname{respectively. Returns} -Inf \text{ if } f \text{ is}$
	-0.
exp exp2 exp10	$f.\exp(\text{rnd_mode} = \text{GMP_RNDN, res_prec} = f.\text{prec}) \rightarrow g$ $f.\exp(\text{rnd_mode} = \text{GMP_RNDN, res_prec} = f.\text{prec}) \rightarrow g$ $f.\exp(\text{lnd_mode} = \text{GMP_RNDN, res_prec} = f.\text{prec}) \rightarrow g$
	Returns the exponential of f , 2 to the power of f , and 10 to the power of f , respectively.
cos	$f.\cos(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
sin	$f.\sin(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
tan	$f.\tan(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$ Returns the cosine, sine, and tangent of f , respectively.
	returns the cosme, sine, and tangent of j, respectively.
sec	$f.\operatorname{sec}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
csc	$f.\operatorname{csc}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
\cot	$f.\cot(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
	Returns the secant, cosecant, and cotangent of f , respectively.
acos	$f.acos(rnd_mode = GMP_RNDN, res_prec=f.prec) \rightarrow g$
asin	$f.\operatorname{asin}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
atan	$f.atan(rnd_mode = GMP_RNDN, res_prec=f.prec) \rightarrow g$
	Returns the arc-cosine, arc-sine, and arc-tangent of f , respectively.
\cosh	$f.\operatorname{cosh}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
\sinh	$f.\sinh(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
tanh	$f.tanh(rnd_mode = GMP_RNDN, res_prec = f.prec) \rightarrow g$
	Returns the hyperbolic cosine, sine, and tangent of f , respectively.

sech csch coth	$f.\operatorname{sech}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$ $f.\operatorname{csch}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$ $f.\operatorname{coth}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
	Returns the hyperbolic secant, cosecant, and cotangent of f , respectively.
acosh asinh atanh	$f.\operatorname{acosh}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$ $f.\operatorname{asinh}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$ $f.\operatorname{atanh}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
	Returns the hyperbolic arc-cosine, arc-sine, and arc-tangent of f , respectively.
log1p	$f.\log 1p(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
	Returns the logarithm of 1 plus f .
expm1	$f.\text{expm1}(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
	Returns the exponential of f minus 1.
eint	$f.\mathrm{eint}(\mathrm{rnd_mode} = \mathrm{GMP_RNDN}, \mathrm{res_prec} = f.\mathrm{prec}) \to g$
	Returns the exponential integral of f . For positive f , the exponential integral is the sum of Euler's constant, of the logarithm of f , and of the sum for k from 1 to infinity of f to the power k , divided by k and factorial(k). For negative f , this method returns NaN.
li2	$f.\mathrm{li2}(\mathrm{rnd_mode} = \mathrm{GMP_RNDN}, \mathrm{res_prec} = f.\mathrm{prec}) \rightarrow g$
	Returns the real part of the dilogarithm of f . MPFR defines the dilogarithm as the integral of $-\log(1-t)/t$ from 0 to f .
gamma	$f. \operatorname{gamma}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
	Returns the value of the Gamma function on f . When f is a negative integer, this method returns NaN.
lngamma	$f.\operatorname{lngamma}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
	Returns the value of the logarithm of the Gamma function on f . When $-2k-1 \le f \le -2k$, k being a non-negative integer, this method returns NaN.
digamma	$f. ext{digamma}(ext{rnd_mode} = ext{GMP_RNDN}, ext{res_prec} = f. ext{prec}) o g$
	Returns the value of the Digamma (sometimes called Psi) function on f . When f is negative, this method returns NaN.
	Only available in MPFR version 3.0.0 or later.

zeta	$f.\mathrm{zeta}(\mathrm{rnd_mode} = \mathrm{GMP_RNDN}, \mathrm{res_prec} = f.\mathrm{prec}) \rightarrow g$
	Returns the value of the Riemann Zeta function on f .
erf	$f.\operatorname{erf}(\operatorname{rnd_mode} = \operatorname{GMP_RNDN}, \operatorname{res_prec} = f.\operatorname{prec}) \to g$
erfc	$f.{ m erfc}({ m rnd_mode} = { m GMP_RNDN}, { m res_prec} = f.{ m prec}) ightarrow g$
	Returns the value of the error function on f (respectively the complementary error function on f).
j0 j1 jn	$f.j0(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$ $f.j1(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$ $f.jn(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
	Returns the value of the first kind Bessel function of order 0 (respectively 1 and n) on f . When f is NaN, this method returns NaN. When f is +Inf or -Inf, this method returns +0. When f is zero, this method returns +Inf or -Inf, depending on the parity and sign of n , and the sign of f .
y 0	$f.y0(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$
y1	$f.y1(\text{rnd_mode} = \text{GMP_RNDN}, \text{res_prec} = f.\text{prec}) \rightarrow g$

 $\mathbf{y}\mathbf{n}$

Returns the value of the second kind Bessel function of order 0 (respectively 1 and n) on f. When f is NaN or negative, this method returns NaN. When f is +Inf, this method returns +0. When f is zero, this method returns +Inf or -Inf, depending on the parity and sign of n.

 $f.yn(rnd_mode = GMP_RNDN, res_prec=f.prec) \rightarrow g$

11 Random Number Functions

11.1 Random State Initialization

new

GMP::RandState.new \rightarrow mersenne twister state GMP::RandState.new(:default) \rightarrow mersenne twister state GMP::RandState(:mt) \rightarrow mersenne twister random state GMP::RandState.new(:lc_2exp, a, c, m2exp) \rightarrow linear congruential state GMP::RandState.new(:lc_2exp_size, size) \rightarrow linear congruential state

This method creates a new GMP::RandState instance. The first argument defaults to :default (also :mt), which initializes the GMP::RandState for a Mersenne Twister algorithm. No other arguments should be given if :default or :mt is specified.

If the first argument given is $:lc_2exp$, then the GMP::RandState is initialized for a linear congruential algorithm. $:lc_2exp$ must be followed with a, c, and m2exp. The algorithm can then proceed as $(X = (a * X + c) \mod 2^{m2exp})$.

GMP::RandStatecan also be initialized for a linear congruential algorithm with $:lc_2exp_size$. This initializer instead takes just one argument, size. a, c, and m2exp are then chosen from a table, with m2exp/2 > size. The maximum size currently supported is 128.

GMP::RandState.new

GMP::RandState.new(:mt)

GMP::RandState.new(:lc_2exp, 1103515245, 12345, 15) #=> Perl's

old rand()

GMP::RandState.new(:lc_2exp, 25_214_903_917, 11, 48) #=> drand48

11.2 Random State Seeding

seed

 $state.seed(integer) \rightarrow integer$

Set an initial seed value into state. integer can be an instance of GMP::Z, Fixnum, or Bignum.

11.3 Integer Random Numbers

urandomb

 $state.urandomb(n) \rightarrow integer$

Generates a uniformly distributed random integer in the range 0 to $2^n - 1$, inclusive.

urandomm

 $state.urandomm(n) \rightarrow integer$

Generates a uniformly distributed random integer in the range 0 to n-1, inclusive. n can be an instance of GMP::Z, Fixnum, or Bignum.

11.4 Floating-point Miscellaneous Functions (MPFR Only)

$mpfr_buildopt_tls_p$

GMP::F.mpfr_buildopt_tls_p() $\rightarrow integer$

Available only in MPFR 3.0.0 and greater.

From the MPFR Manual: Return a non-zero value if MPFR was compiled as thread safe using compiler-level Thread Local Storage (that is, MPFR was built with the --enable-thread-safe configure option, see INSTALL file), return zero otherwise.

$mpfr_buildopt_decimal_p$

 $GMP::F.mpfr_buildopt_decimal_p() \rightarrow integer$

Available only in MPFR 3.0.0 and greater.

From the MPFR Manual: Return a non-zero value if MPFR was compiled with decimal float support (that is, MPFR was built with the --enable-decimal-float configure option), return zero otherwise.

12 Benchmarking

Benchmark results can be found in performance.pdf.