

Assignment 11

(1)

We have been asked to write the proof for a recursive factorial function using proof by induction.

```
/* Factorial function definition */
int fact(int n)
{
    /* pre-condition */
    assert (n >= 1);

    /* post-condition */
    if (n > 1)
        return n * fact(n - 1);
    else
        return 1;
}
```

The program computes the factorial of an integer. It consists of a base case and a following recursive step. In this function the precondition ensures that $n \geq 1$, furthermore the base case is that if $n=1$ it returns 1. That is confirmed by $1 * \text{fact}(n - 1) = 1 * 0! = 1$.

Now that the base case is confirmed by $\text{fact}(0) = 1$, we can proceed to the recursive step, that is when $n > 1$.

In layman's terms the function does as shown: $\text{fact}(k) = k * \text{fact}(k - 1)$, for any k above 1. Since we know that $\text{fact}(1)$ is correct it would also apply to $\text{fact}(2)$. Since $\text{fact}(2) = 2 * \text{fact}(1)$, and $\text{fact}(1)$ was 1, it would mean that $\text{fact}(2) = 2 * 1 = 2$.

Since $\text{fact}(1)$ was correct $\text{fact}(2)$ was also correct, the same applies to $\text{fact}(3)$ and for $\text{fact}(4)$ and so on, up until $\text{fact}(k)$.

That is true because of the recursive step of the function, it moves towards the base case of the function. This proves that the program is correct for all positive integers n .