

Programmering

Exercises

- (1) Write down a proof that the following recursive factorial function is correct using *proof by induction*. Put your inductive proof into a pdf file (`text_answers.pdf`).
Hint: review the lecture slides for the two components of a proof by induction, i.e. (a) the base case and (b) the inductive step.

```
/* Factorial function definition */
int fact(int n)
{
    /* pre-condition */
    assert (n >= 1);

    /* post-condition */
    if(n > 1)
        return n * fact(n - 1);
    else
        return 1;
}
```

Proof by induction is we need to prove that the claim is true from $1 \rightarrow n$.

First, we test for 1 (base case)

We insert 1

It can go through the assert because $1 = 1 = \text{true}$

Does not do the if statement because 1 aren't over 1=false

So we go to the else statement where it returns $1 \rightarrow \text{true}$

Then we prove that the claim is true for the inductive step.

We insert 2

Assert is tried because $2 \geq 1 = \text{true}$

Does do the statement $2 > 1 = \text{true}$

Returns= $2 \cdot \text{fact}(2 - 1) = 2 = \text{true}$