

## Exercise 1)

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- (1) Write down a proof that the following recursive factorial function is correct using *proof by induction*. Put your inductive proof into a pdf file (`text_answers.pdf`).  
*Hint:* review the lecture slides for the two components of a proof by induction, i.e. (a) the base case and (b) the inductive step.

```
/* Factorial function definition */
int fact(int n)
{
    /* pre-condition */
    assert (n >= 1);

    /* post-condition */
    if(n > 1)
        return n * fact(n - 1);
    else
        return 1;
}
```

First we prove that the function is correct for a given base case. The integer range in the factorial function is  $n \geq 1$ . Let's use `fact(1)` which equals 1 and is what the function will return when  $n=1$ .

Next is the inductive step. We consider the recursive case with the integer input  $k > 1$ .

$\text{Fact}(k) = k * \text{fact}(k-1)$ . We assume this is correct (inductive hypothesis). The  $k$ 'th factorial is then  $\text{fact}(k) = k * \text{fact}(k-1)$ .

Let's say  $k=3$ . The function computes  $3 * 2 * 1 = 6$  which correlates to the above function. Since `fact(3)` is proved to be correct then `fact(2)` and `fact(1)` are proven as well. So is `fact(4)`, `fact(5)` and so on.