

Week 11: Verifying Correctness of Recursive Programs

Exercise 1

Base case:

Since n must be greater than or equal to one, the base case will be:

$\text{fact}(1)$ returns 1, which is correct.

Inductive step:

The function is correct if $\text{fact}(n) = n * \text{fact}(n - 1)$ is correct when $\text{fact}(n - 1)$ is correct.

$\text{fact}(2)$ returns $2 * \text{fact}(1) = 2 * 1 = 2$, which is correct.

Since $\text{fact}(2)$ is correct, then $\text{fact}(n)$ is correct for all $n \geq 1$.