

Assume a point mass m at radius r from a pivot point attached by a massless arm with length r. The angle of the arm is  $\theta$ , a function of time. The torque applied to the arm is T, positive in the counterclockwise direction. The moment of inertia is given by

$$I = mr^2$$
.

The angular version of Newton's second law is

$$T = I\ddot{\theta}$$
.

The torque due to gravity is given by

$$T_g = -mrg\cos(\theta),$$

where  $g=9.81~{\rm m/s^2}$  is the acceleration of gravity at sea level. The net torque is  $T-T_q$ . Hence,

$$\ddot{\theta} = \frac{T}{mr^2} - \frac{g\cos(\theta)}{r}.$$