

# **Lesson 2**

## **Computability**

Math 574 - Topics in Logic  
Penn State, Spring 2014

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2-3

Turing machines - an example

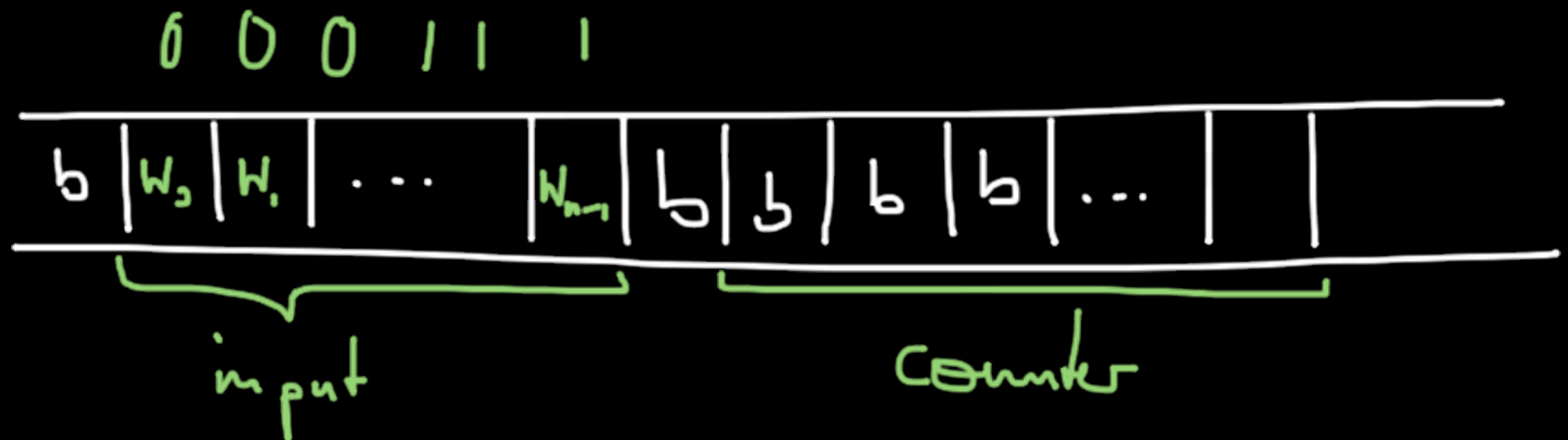
Goal: Find a TM  $M$  s.t.

$M$  outputs  $\begin{cases} 1 & \text{if input is} \\ & \text{of form } 0^n 1^n \\ 0 & \text{for all other} \\ & \text{inputs} \end{cases}$

$M$  "accepts" the language

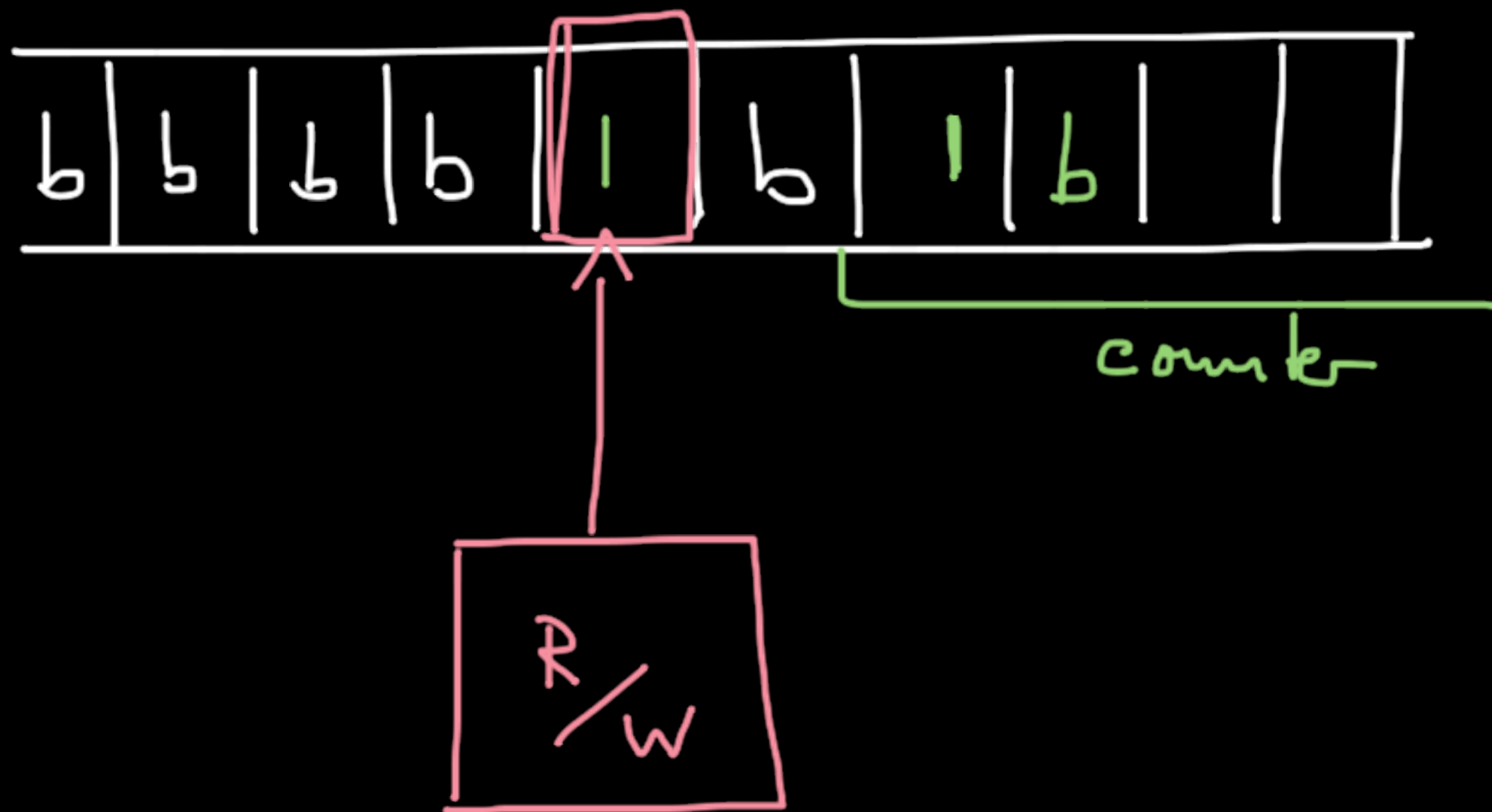
$$L = \{0^n 1^n : n \geq 0\}$$

Input:  $w = w_0 w_1 \dots w_{n-1} \in \{0,1\}^{<IN}$



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$0^n 1^n$



- Subroutines
- loops
- while
- if .. then ...