

μ prob
measure

$$\mu\left(\bigcup A_i\right) = \sum \mu(A_i)$$

$$\mu(A) \uparrow$$

Borel

① $\{x: \mu(\{x\}) > 0\}$ obtained from open Borel sets
by taking unions and complements.

$$B = [0, 1)$$

$$\underline{B} = \bigcup_n [0, 1 - \frac{1}{n}]$$

Picard / Quiz set of atoms is countable

countable set is always Borel

$$= \bigcup_{\text{countable}} \{x\}$$



no dots : all mass will eventually disappear
when zooming in.

$$A_c = \{x : \mu(\{x\}) \geq \underline{c}\}$$

$$A = \bigcup_{c \in \mathbb{Q}^+} A_c$$

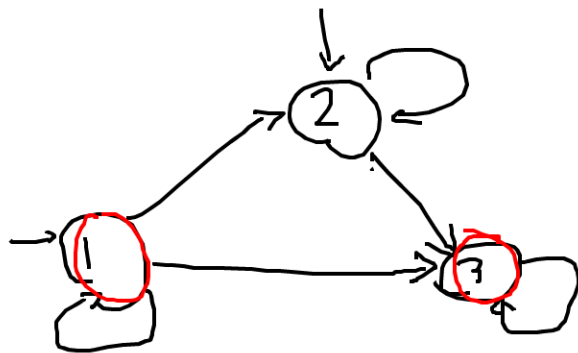
countable union

$$c = \frac{1}{2}$$



T

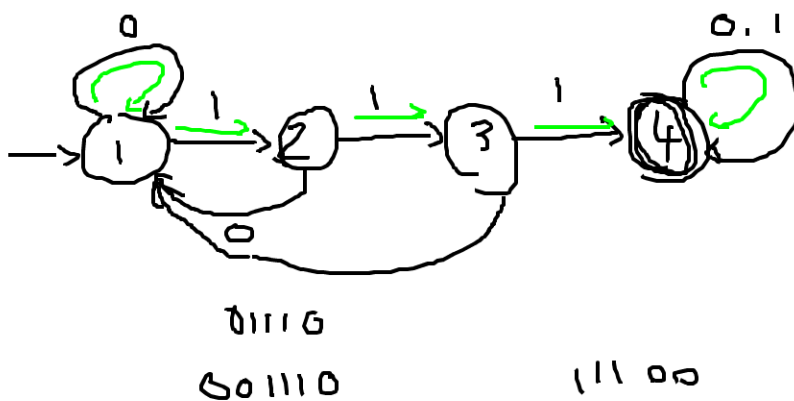
$$T^{\infty} = A_c$$



$\{w : w = 01101 \vee \}$

01101*

$\{w : w \text{ contains } \underline{11}\} = \underline{*11*}$ 666



*
ls * .txt
but all files
that end with .txt

wild card
↙

Lemma:

$\{v_1, \dots, v_n\}$

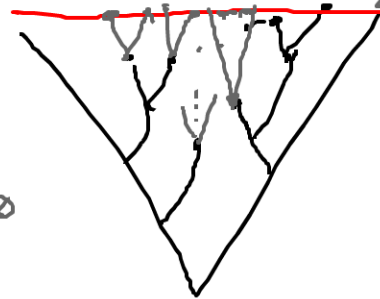
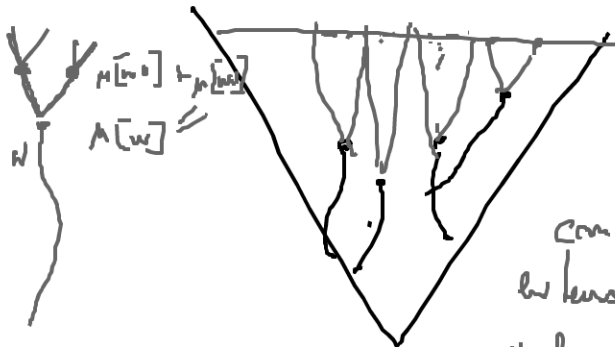
$\{w_1, \dots, w_m\}$

prefix-free

$$\bigcup [v_i] = \bigcup [w_j]$$

$$\Rightarrow \sum \mu[v_i] = \sum \mu[w_j]$$

show: two prefix-free
set of strings
of same length
generating same
open set
must be
identical



can do this
extension
while: (1) preserve open set
generated
(2) preserve measure