

WW3: Series & Parallel Connection

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A. Series Connection

Given:

- $V_T = 12\text{ V}$
- $R_1 = 5\ \Omega$
- $R_2 = 10\ \Omega$
- $R_3 = 4\ \Omega$
- $R_4 = 2\ \Omega$

Find:

- R_T
- I_T
- I_1, \dots, I_4
- V_1, \dots, V_4

Solution:

- $R_T = 5\ \Omega + 10\ \Omega + 4\ \Omega + 2\ \Omega$
- $R_T = 21\ \Omega$

- $I_T = \frac{12\text{ V}}{21\ \Omega}$

- $I_T = \frac{4}{7}\text{ A}$

- $I_1, \dots, I_4 = \frac{4}{7}\text{ A}$

- $V_1 = \frac{4}{7}\text{ A} \cdot 5\ \Omega = \frac{20}{7}\text{ V}$

- $V_2 = \frac{4}{7}\text{ A} \cdot 10\ \Omega = \frac{40}{7}\text{ V}$

- $V_3 = \frac{4}{7}\text{ A} \cdot 4\ \Omega = \frac{16}{7}\text{ V}$

- $V_4 = \frac{4}{7}\text{ A} \cdot 2\ \Omega = \frac{8}{7}\text{ V}$

B. Parallel Connection

Given:

- $V_T = 24\text{ V}$
- $R_1 = 3\ \Omega$
- $R_2 = 5\ \Omega$
- $R_3 = 8\ \Omega$
- $R_4 = 4\ \Omega$

Find:

- R_T
- I_T
- I_1, \dots, I_4
- V_1, \dots, V_4

Solution:

- $\frac{1}{R_T} = \frac{1}{3\ \Omega} + \frac{1}{5\ \Omega} + \frac{1}{8\ \Omega} + \frac{1}{4\ \Omega} = \frac{109}{120}\ \Omega$

- $R_T = \frac{120}{109}\ \Omega$

- $I_T = \frac{24\text{ V}}{\frac{120}{109}\ \Omega} = 24\text{ V} \cdot \frac{109}{120}\ \Omega$

- $I_T = \frac{109}{5}\text{ A}$

- $I_1 = \frac{24\text{ V}}{3\ \Omega} = 8\text{ A}$

- $I_2 = \frac{24\text{ V}}{5\ \Omega} = \frac{24}{5}\text{ A}$

- $I_3 = \frac{24\text{ V}}{8\ \Omega} = 3\text{ A}$

- $I_4 = \frac{24\text{ V}}{4\ \Omega} = 4\text{ A}$

- $V_1, \dots, V_4 = 24\text{ V}$