

Q.12) The null and alternative hypothesis are

$$H_0: p_0 = 0.05$$

$$H_a: p > 0.05$$

(b) We use the z test because we have more than 30 sample.

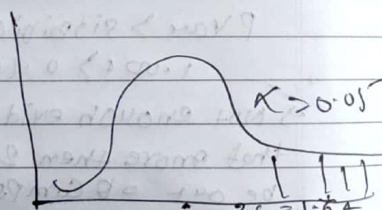
$$(c) \hat{p} = 4/38 = 0.12$$

$$q = 1 - p = 1 - 0.05 = 0.95$$

$$z_{test} = \frac{\hat{p} - p}{\sqrt{\frac{p \cdot q}{n}}} = \frac{0.12 - 0.05}{\sqrt{\frac{0.05 \times 0.95}{38}}}$$

$$= \frac{0.07}{0.011} = 6.36$$

$$\boxed{Z \text{ Score} = 6.36}$$



Here z score is greater than  $z_c$  so we reject the null hypothesis and this test claim that the increase of certain chemicals in the environment has lead to an increase in asthma.

Q(2) New hypothesis: 20% of the cars failed to meet population guidelines

$$H_0: p = 0.20$$

Alternate hypothesis: more than 20% of the failed to meet population guidelines.

$$H_a: p > 0.20$$

It is a one tailed test since we are going to check only one end of experiment and here we do 2 test.

⇒ Set the significance value = 10%  
 $\alpha = 0.10$

⇒ If  $Z_{critical} < Z\text{-score}$  we will reject null hypothesis.

For,

$P\text{-value} < \text{significance level}$ , we will reject the null hypothesis.

Z test for proportion

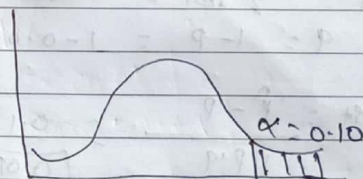
$$Z = \frac{(\hat{p} - p)}{\sqrt{p(1-p)/n}}$$

$$\hat{p} = \frac{7}{22} = 0.318$$

$$Z = \frac{0.32 - 0.20}{\sqrt{\frac{0.20(1-0.20)}{22}}} = \frac{0.12}{\sqrt{\frac{0.20 \times 0.80}{22}}}$$

$$= \frac{0.12}{\sqrt{0.00727272727}} = \frac{0.12}{0.08528028} = 1.4071$$

$$Z\text{-score} = 1.4071 \approx 1.41$$



As per Z table:  $Z_c = 1.3$

$Z_{critical} > Z\text{score}$  (we will accept null hypothesis)

$$P\text{value} = 1.004$$

$P\text{value} > \text{significance value}$

$1.004 > 0.10$  (accept the null hypothesis)

⇒ Not enough evidence to support the claim that more than 20% of the fleet might be out of compliance.

Q(2) For  $\alpha = 5\%$

$$\alpha = 0.05$$

$$Z \text{ score} = 1.41$$

$$Z \text{ critical} = 1.64 \quad - 2\text{-tailed}$$

$1.64 > 1.42$  we will accept the null hypothesis

if  $\alpha = 1\%$

$$\alpha = 0.01$$

$$Z \text{ score} = 1.41$$

$$Z \text{ critical} = 2.33$$

$Z \text{ critical} > Z \text{ score}$   
we will accept the null hypothesis



Q(3) ~~Q(2)~~ → null hypothesis: 44% of the adult population had never smoked.

$$H_0: p = 0.44$$

→ Alternative hypothesis: more than 44% of the adult population have smoked.

$$H_A: p > 0.44$$

→ one tailed test because only one end experiment.

We will do 2 test.

Confidence level = 98%

$$\alpha = 2\%$$

$$\alpha = 0.020$$

ib

2-critical < 2-test we will reject null hypothesis

for p value.

P value < significance value. We will reject the null hypothesis

P<sub>2</sub> P value,

P value & significance value

We will reject null hypothesis

$$Z_{score} = \frac{\hat{p} - p}{\sqrt{\frac{pq}{n}}}$$

$$p = 0.44, n = 891$$

$$q = 1 - p = 1 - 0.44 = 0.56$$

$$\hat{p} = \frac{463}{891} = 0.519$$

$$Z_{score} = \frac{0.519 - 0.44}{\sqrt{\frac{0.44 \times 0.56}{891}}}$$

$$Z_{score} = 4.75$$

$$Z_{critical} = 2.20$$

$$Z_{critical} < Z_{score}$$

$$2.20 < 4.75$$

We will reject the null hypothesis

Q3)

→ According to the test that they show more than 44% of the the adult population never smoked.

$$1P3 = 0.44, 1P0 = 0.56$$

$$22.0 = 44.0 - 1 = 9.1 = 1$$

$$0.22 = 0.44 - 1 = 0.22$$

$$44.0 - 1.17.0 = 32.3$$

$$\frac{22.0 \times 44.0}{100} = 9.68$$

$$2.5 = 1.12$$

$$0.22 = 0.22$$

$$2.5 < 1.12$$

$$2.5 < 1.12$$

We will reject the null hypothesis



Q. (4)

Null hypothesis  $\rightarrow$  Distance from the lens to the object and distance from the lens to real image is same.

$$H_0 : \mu_A = \mu_B$$

Alternate hypothesis  $\rightarrow$  The distance from the lens to the object and distance from the lens to real image is not same

$$\mu_A; \mu_A \neq \mu_B$$

Here we will do 2 test.

Significance value not given in the problem  
So we are going to take that

$$\alpha = 0.05$$

Since this is the two tailed test

$$\frac{\alpha}{2} = \frac{0.05}{2} = 0.025$$

Decision rule

2 - critical < 2 - Score

We will reject the null hypothesis  
for p value.

p value < significance value

We will reject the null hypothesis.



Q(4) Sample mean of the measurement ( $\bar{S}_1$ ) = 26.6 cm  
 $(\bar{S}_2) = 13.8$  cm

Standard deviation of measurement  $S_1 = 0.1$  cm  
 $S_2 = 0.5$  cm

⇒ for distance from the lens to object  $S_1$

$$\bar{S}_1 = 26.6 \text{ cm}$$

$$\sigma_1 = 0.1 \text{ cm}$$

$$n_1 = 25$$

⇒ for distance from lens to real image,  $S_2$ ,

$$\bar{S}_2 = 13.8$$

$$\sigma_2 = 0.5 \text{ cm}$$

$$n_2 = 25$$

$$Z \text{ score} = \frac{\bar{S}_1 - \bar{S}_2}{\sqrt{\frac{(\sigma_1)^2}{n_1} + \frac{(\sigma_2)^2}{n_2}}} = \frac{26.6 - 13.8}{\sqrt{\frac{(0.1)^2}{25} + \frac{(0.5)^2}{25}}}$$

$$= \frac{12.8}{0.102} = Z \text{ Score} = 125.51$$

~~for  $\alpha = 0.05$~~

$$Z_{\text{critical}} < Z \text{ score}$$

$$1.96 < 125.51$$

We will reject the null hypothesis

Q4) As per the test result we state that distance from the lens to the object and distance from the lens to the real image are not same.

i.e

$$u_A \neq u_B$$



Q(5)

Null hypothesis: Mean body temp is 98.6  
 $H_0: \mu = 98.6$

Alternate hypothesis: Mean body temp is not equal to 98.6  
 $H_a: \mu \neq 98.6$

This is two tailed test  
 $\alpha = \frac{0.02}{2} = 0.01$

Here we are going to do test.  
 Given,  $\alpha = 0.02$

Decision Rule

$t_{critical} < t_{score}$

We will reject null hypothesis

For P value,

if  $p\text{-value} < \text{Significance level}$

We will reject null hypothesis

$n = 52$ ,  $\bar{x} = 98.284$ ,  $s = 0.624$

$$t\text{-score} = \frac{\bar{x} - \mu}{s/\sqrt{n}}$$

$$= \frac{98.284 - 98.6}{\frac{0.624}{\sqrt{52}}}$$

Q(10)

$$t\text{-score} = 3.333$$

It is two tailed test

$$\alpha = \frac{0.02}{2} = 0.01$$

$$\alpha = 0.01$$

$$DF = n - 1 = 52 - 1 = 51$$

$$DF = 51$$

now using t-table

$$t_{critical} = 2.008$$

$$p\text{-value} = 0.0016$$

As per decision rule

For critical value

$$2.008 < 3.333$$

$t_{critical} < t_{score}$

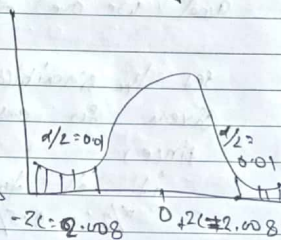
We will reject null hypothesis

$$0.0016 < 0.02$$

$p\text{-value} < \text{Significance level}$

reject the null hypothesis

So even if the body temp not equal to 98.6 °F



Q(6)

Null hypothesis  $\rightarrow$  There is no difference b/w the premium and Regular gas tanks in term of mileage.

$$H_0: \mu_A = \mu_B$$

Alternate hypothesis: There is a difference b/w the premium and Regular gas tanks in term of mileage.

$$H_1: \mu_A \neq \mu_B$$

This is two tailed test and we are going to perform T-test

set the significance var., significance var not given so assume significance  $\alpha = 0.05$

since,

it is two tailed test

$$\alpha/2 = 0.05/2 = 0.025$$

(Decision rule)

+ critical < t-test

We will reject the null hypothesis

for p-value

p value < significance value

We will reject null hypothesis

Q(7) Given data

Car	1	2	3	4	5	6	7	8	9	10
Regular	16	20	21	22	23	22	27	25	27	28
Premium	14	22	24	24	25	25	26	26	28	32

Analysis of data

sample of premium tank  
 $\bar{x} = \mu_B = 27.1$   
 $n_2 = 10, s_2 = 3.44$

t-test for two sample variable,

so we required

$$DF = \left[ \frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} \right]^2 \left[ \frac{(\frac{s_1^2}{n_1})^2}{n_1-1} + \frac{(\frac{s_2^2}{n_2})^2}{n_2-1} \right]$$

Regular tank  
 $\mu_A = \mu = 23.1$   
 $n_1 = 10$   
 $s_1 = 3.72$   
 $\bar{x}_1 = \mu_A = 23.1$

$$\frac{(1.38 + 1.18)^2}{(1.38)^2 + (1.18)^2} = \frac{6.55}{0.26} = 18$$

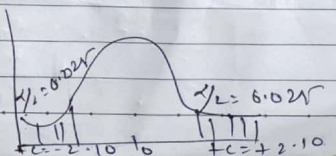
$$DF = 18$$

t-test

$$= \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$$= \frac{23.1 - 27.1}{\sqrt{\frac{(3.72)^2}{10} + \frac{(3.44)^2}{10}}} = 1.24$$

$$t_{critical} = 2.10$$





Q6)  $p = 0.22$

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youva

As per decision rule  
for  $t$ -critical,  
if

$$t_{\text{critical}} < t_{\text{score}}$$

reject the hypothesis

but here

$$t_{\text{critical}} > t_{\text{score}}$$

$$2.10 > 1.24$$

- We will accept the new hypothesis

also for the  $p$  value

$p$  value  $>$  Significance value

$$0.22 > 0.05$$

We will accept the new hypothesis

This test shows no difference in mileage  
of regular and premium tanks of  
the car.



Q(7.)

Null hypothesis  $\rightarrow$  Sugar Content of brand of cereals for children and adult are same.

$$H_0: \mu_A = \mu_B$$

Alternate hypothesis - Sugar Content of brand of cereals for children and adult are not same.

$$H_1: \mu_A \neq \mu_B$$

Here we performed two tailed test.

We are comparing the mean of two sample so, we are going to perform t-test.

Set the significance value,

Given Confidence level = 95%

Significance level is 5%

$$\alpha = 5\%$$

$$\alpha = 0.05$$

Since, it is a two tailed test.

$$\alpha/2 = 0.05/2 = 0.025$$

Decision rule,

$$t_{\text{critical}} < t_{\text{test}}$$

We will reject the null hypothesis

P-value < Significance level

We will reject the null hypothesis.



Q7)

Given,

Sugar Content of several national brand of cereals, here measured as a percentage of weight.

children	40.3	55.0	45.7	43.3	50.3	45.9	53.5	43.0	44.2
	44.0	53.6	51.1	48.6	60.4	37.8	60.3	46.6	47.4
	44.0								
Adult	20.0	30.2	2.2	7.5	4.4	22.2	16.6	12.5	21.4
	3.3	10.0	1.0	4.4	1.3	8.1	6.6	7.8	10.6
	16.2	14.5	4.1	16.8	4.1	8.4	3.5	8.5	9.7
	12.4								

⇒ For Sample of children,

$$\bar{x}_1 = \mu_A = 46.8$$

$$n_1 = 19$$

$$s_1^2 = 6.41$$

For Sample of Adult,

$$\bar{x}_2 = \mu_B = 10.16$$

$$n_2 = 29$$

$$s_2^2 = 7.47$$

$$DF = \left[ \frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} \right]^2$$

$$= \left[ \frac{(6.41)^2}{19} + \frac{(7.47)^2}{29} \right]^2$$

Q7)

$$= \frac{(2.16 + 1.92)^2}{\frac{(2.16)^2}{18} + \frac{(1.92)^2}{28}} = \frac{16.64}{0.38}$$

$$df = 43$$

Now,

$$t\text{-test} = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

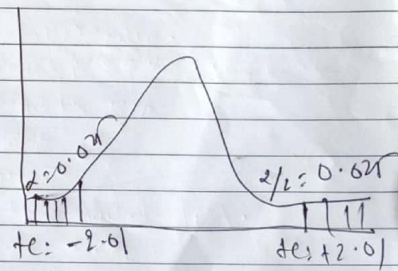
$$= \frac{6.41 - 7.47}{\sqrt{\frac{(6.41)^2}{19} + \frac{(7.47)^2}{29}}} = \frac{36.38}{1.96}$$

$$t\text{-test} = 18.10$$

as per t-table

$$t_{\alpha} = 2.01$$

$$p\text{-value} = 0.0001$$



Here,  $t_{\text{critical}} < t_{\text{test}}$   
 $2.01 < 18.10$

and,

$p\text{-value} < \text{significance value}$   
 $0.0001 < 0.05$

So, we will reject the null hypothesis

Q7)

So,

The Sugar Content in different brand of cereals for children and Adult are not same.

$$27 = 76$$

$$58 - 18 = 40$$

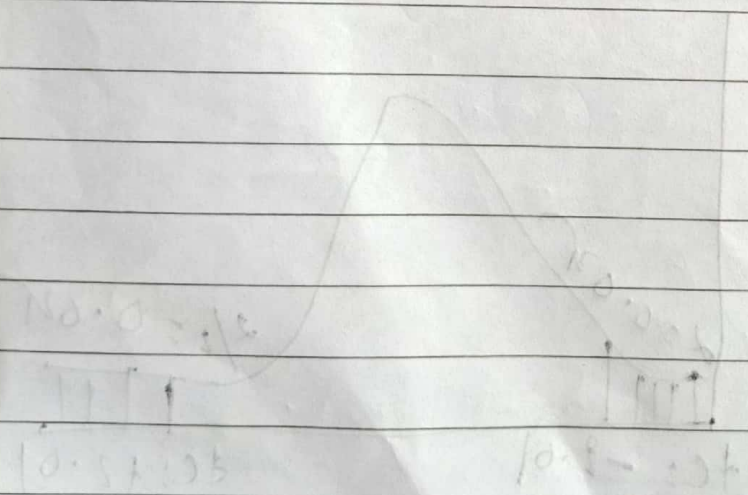
$$\frac{58}{50} = 1.16$$

$$14.5 - 14.2$$

$$(14.5) - (14.2)$$

$$0.3$$

$$101.81 = 40$$



$$10.8 \times 1000 = 10800$$

$$10.8 < 11.5$$

10.8

$$10.8 < 11.5$$

10.8 < 11.5