

Regression Analysis: A bit of History

Predictive Modeling & Statistical Learning

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Historical Background

Introduction

In order to better understand the “modern” side of predictive models, it is worth talking about the origins of the Regression framework, and its consolidations during the first half of the 20th century.

Overview

- ▶ The method of Least Squares was discovered (or invented) in the early 1800's
- ▶ The idea of Regression appeared around 1885
- ▶ The connection between LS and Regression appeared in 1897

Least Squares

LS origins

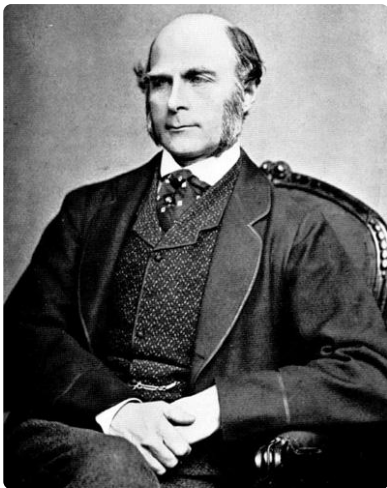
- ▶ Least Squares owes its origins to astronomy.
- ▶ Adrien-Marie Legendre's 1805 pioneering work on the determination of the orbits of planets.
- ▶ Carl Friedrich Gauss stated in 1809 that he had been using LS since 1795, but could not prove his claim with documented evidence.
- ▶ Within a few years, Gauss and Pierre Simon Laplace added a probability component (curve to describe the error distribution).
- ▶ Gauss devised an elimination algorithm to compute LS estimates.

LS origins

- ▶ Once introduced, LS caught on immediately in Astronomy and Geodetics.
- ▶ But it took 80 yers for these ideas to be applied to other disciplines.

Regression Ideas

Sir Francis Galton (1822 - 1911)



Galton's motto: "Count wherever you can"

About Galton

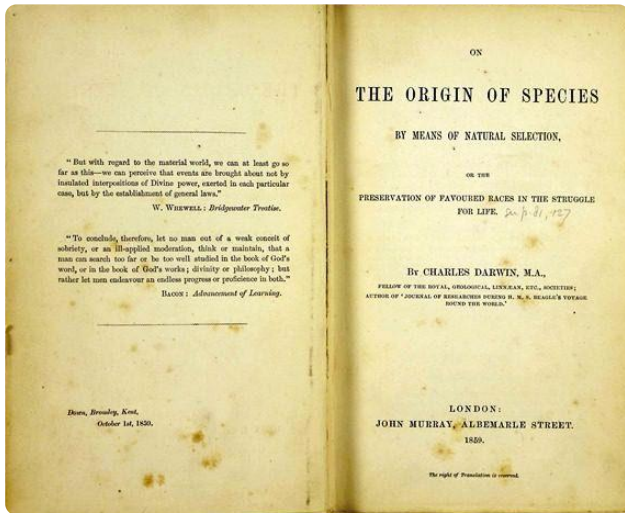
- ▶ Victorian Polymath
- ▶ 1859 - Reads *On the Origin of the Species* by Charles Darwin (Galton's half-cousin)
- ▶ 1869 - Publishes **Hereditary Genius** (book)
- ▶ 1883 - Coined the term **Eugenics**
- ▶ 1886 - **Regression towards Mediocrity in Hereditary Stature** (paper)

Galton's terminology

Some terms coined by Galton

- ▶ Percentile
- ▶ Decile
- ▶ Quartile, IQR
- ▶ Deviate (later called “deviations”)
- ▶ Normal curve
- ▶ Correlation
- ▶ Regression

1859 Darwin's "On the Origin of Species"



Thesis: Evolution by Natural Selection

Galton's research topics and ideas

- ▶ Improve humanity by carefully designed selection
- ▶ How to quantify effects of heredity?
- ▶ Inheritance of mental abilities
- ▶ Theory: intelligence, morality, civism, etc are determined by heredity

1870s Sweet pea seeds experiment



Measure weight of parents and offspring

1870s Sweet pea seeds experiment



Measure weight of parents and offspring

- ▶ Smaller parent seeds produce offspring that were larger.
- ▶ Larger parent seeds produce offspring that were smaller.

ANTHROPOMETRIC LABORATORY

For the measurement in various
ways of **Human Form and Faculty.**

Entered from the Science Collection of the S. Kensington Museum.

This laboratory is established by Mr. Francis Galton for
the following purposes:—

1. For the use of those who desire to be accurately measured in many ways, either to obtain timely warning of remediable faults in development, or to learn their powers.
2. For keeping a methodical register of the principal measurements of each person, of which he may at any future time obtain a copy under reasonable restrictions. His initials and date of birth will be entered in the register, but not his name. The names are indexed in a separate book.
3. For supplying information on the methods, practice, and uses of human measurement.
4. For anthropometric experiment and research, and for obtaining data for statistical discussion.

Charges for making the principal measurements:
THREEPENCE each, to those who are already on the Register.
FOURPENCE each, to those who are not:— one page of the Register will thenceforward be assigned to them, and a few extra measurements will be made, chiefly for future identification.

The Superintendent is charged with the control of the laboratory and with determining in each case, which, if any, of the extra measurements may be made, and under what conditions.

H. & W. Brown, Printers, 20 Pall Mall Road, B.W.

The Galton Collection at UCL

The Galton Laboratory began life as the Anthropometric Laboratory which was part of the London International Health Exhibition of 1885. Visitors to the Exhibition were tested with a battery of machines many of which Galton had devised himself and paid a fee for a copy of their measurements and other data. Over 9,000 people contributed to the exercise, and the data gathered were not properly analyzed until the 1920s/30s. Following its success at the Exhibition, Galton established a permanent home for the Anthropometric Laboratory at the South Kensington Museum (which was renamed the Victoria & Albert Museum). Again, so much data was gathered that it was not until advantages in computer technology in the 1980s that any appropriate statistical analysis was done of these.

Galton's lab, South Kensington, 1884-5



Regression Ideas

ANTHROPOLOGICAL MISCELLANEA.

1886

REGRESSION *towards* MEDIOCRITY *in* HEREDITARY STATURE.

By FRANCIS GALTON, F.R.S., &c.

[WITH PLATES IX AND X.]

THIS memoir contains the data upon which the remarks on the Law of Regression were founded, that I made in my Presidential Address to Section H, at Aberdeen. That address, which will appear in due course in the Journal of the British Association, has already been published in "Nature," September 24th. I reproduce here

Galton's reversion and regression

Reversion: reversio, -onis (go back to)

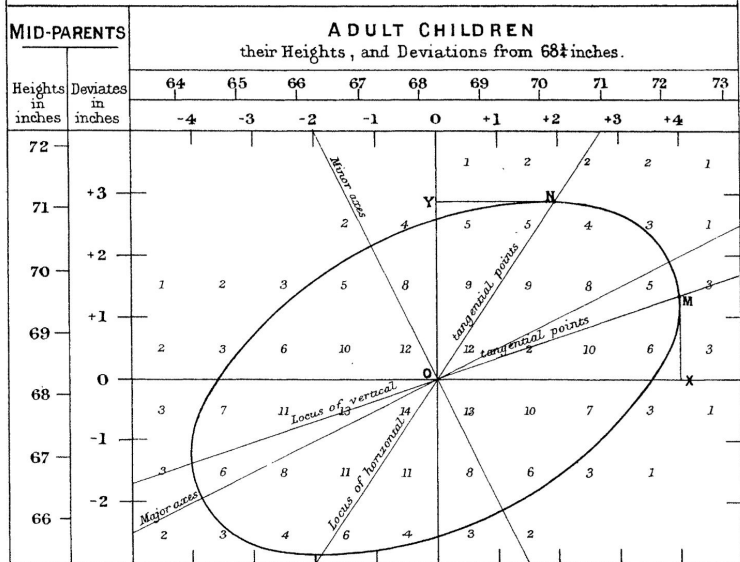
Regression: regressio, -onis (to return)

Galton's Height Data

- ▶ Height data
- ▶ 205 pairs of parents
- ▶ 928 adult children
- ▶ This was a breakthrough:
 - apples A with apples B
 - *mid-parent* idea
 - summarizing relationship with a line

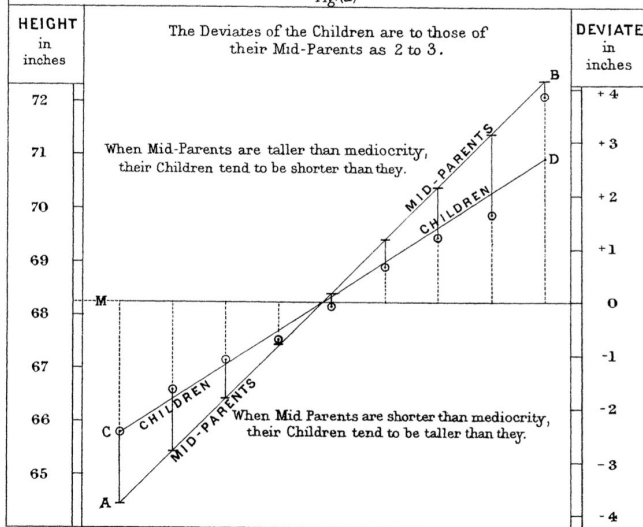
DIAGRAM BASED ON TABLE I.

(all female heights are multiplied by 1.08)



RATE OF REGRESSION IN HEREDITARY STATURE.

Fig. (a)



Galton's "Regression" Meaning

- ▶ Children's heights tend to "revert" to the average height of the population rather than diverting from it
- ▶ Future generations of offspring who are taller than average are not progressively taller than their respective parents
- ▶ and parents who are shorter than average do not beget successively smaller children

Karl Pearson and Francis Galton



Some Comments

- ▶ Galton (and Edgeworth and Pearson) failed to connect least squares to regression
- ▶ It was George Udny Yule (1897) who showed the connection of LS with regression
- ▶ Assuming errors in regression following a Normal distribution, could be replaced by an assumption that the variables were linearly related