Lab 7: Ridge regression and lasso

Johnny Hong

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Introduction

In this lab we will use the dataset Hitters in the R packages ISLR. More specifically, you will use Salary as the response variable, and the rest of the variables in Hitters as the predictors. Our objective is to identify the model with the highest predictive power among a set of model candidates. The models in consideration are ordinary least squares (OLS), principal component regression (PCR), partial least squares regression (PLSR), ridge regression, and lasso.

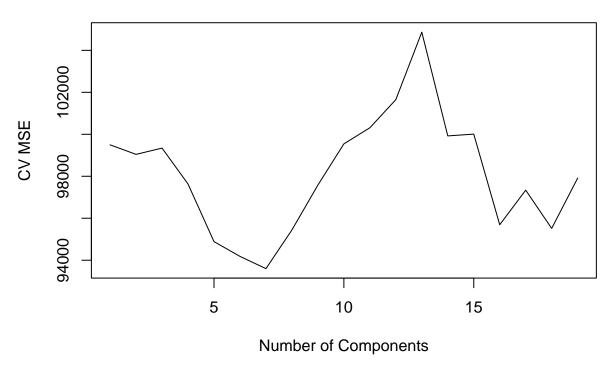
For simplicity, in this lab OLS means that we regress the response variable on all the other variables. Technically, choosing which variables to include is important, and there are many methods to do so such as forward stagewise selection and best subset selection, but we do not pursue these methods in this lab. Note that except for OLS, all the aforementioned methods require hyperparameter tuning. For PCR and PLSR, the hyperparameter is the number of components. For ridge regression and lasso, the hyperparameter is the regularization parameter. Traditionally hyperparameter tuning is performed via cross-validation with a grid search. For ridge regression and lasso, since the regularization parameter is a positive real number, grid search requires a discretization of the hyperparameter space.

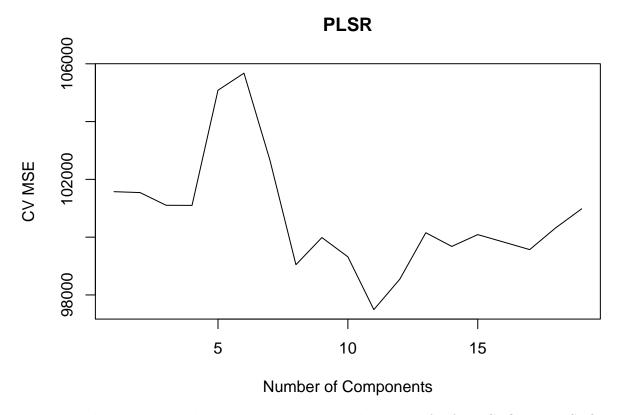
Cross-validation for pcr() and plsr()

Cross validation is built in for pcr() and plsr(). For example, to do a 5-fold CV, use the argument validation = "CV" and segments=5. Here segments refers to the number of folds.

THe following shows how to do 10-fold CV for PCR and PLSR.

PCR





• Based on the plots, how many components do you prefer for PCR? For PLSR?

Cross-validation for ridge regression and lasso

The function glmnet() in the R package glmnet is commonly used to fit ridge regression and lasso. However, glmnet() does not have an optional argument that allows us to do cross validation. We will use cv.glmnet() to perform CV for ridge regression and lasso.

glmnet() can fit a linear model with the elastic net penalty:

$$\frac{1-\alpha}{2}||\beta||_{2}^{2}+\alpha||\beta||_{1},$$

where $\alpha \in [0,1]$ is called the elastic net mixing parameter and β is the slope coefficient.

- If ridge regression is desired, what should be α ?
- If lasso is desired, what should be α ?
- Use cv.glmnet() to perform a 10-fold CV for ridge regression. Find out how to use plot.cv.glmnet() for visualization. Identify the optimal regularization parameter.
- Do the above for lasso.

```
set.seed(300)
# code for ridge regression CV
set.seed(400)
# code for lasso CV
```

Nested Cross Validation

In order to make fair comparisons among different models, we should use a nested cross validation: an inner CV for parameter tuning and an outer CV for estimating the predictive power.

- Run a nested CV to estimate the predictive power for ordinary least squares (OLS), principal component regression (PCR), partial least squares regression (PLSR), ridge regression, and lasso. For hyperparameter tuning, use a 5-fold CV; for estimating predictive power, also use a 5-fold CV. As a reminder, OLS does not have any hyperparameter(s) for tuning in this lab assignment.
- Which model is the best?