#### Week 9

#### Progress during 24-30th Aug

Hao SUN

August 30, 2017



#### Contents

- Unsupervised star-galaxy segmentation
  - A paper: Learning Hierarchical Features from Generative Models
  - A hierarchical structure
  - Some mathematical intuitons and interpretations



### Progress in this week

- Classification task
  - A paper: Learning Hierarchical Features from Generative Models
  - Some mathematical intuitons and interpretations
  - 3 Use a hierarchical structure that can deal with larger dataset



#### Generation vs. classification

Knowing more about the high-level features can not help to generate consistent images. Knowing more about the low-level features can not help to perform classification tasks.

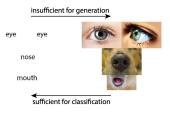


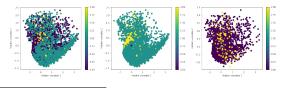
Figure: Fig1. of the paper<sup>1</sup>

If a hierarchical generative model attempts to reconstruct an image based on these high-level features, it could generate inconsistent images, even when each part can be perfectly generated.

## Can VAE learn high-level features?

The most successful generative models often use only a single layer of latent variables <sup>2</sup>, and those that use multiple layers only show modest performance increases in quantitative metrics such as log-likelihood <sup>3</sup>.

- when using more hidden variables (30), the representation ability would be more sufficient to generate consistant images. But the features are more likely to be in lower-level. So that unsupervised clustering methods can not work here.
- when using less hidden variables (2), the representation ability would be less sufficient to generate consistant images, although the features are more likely to be in higher-level. So that accuracy of unsupervised learning is limited.



<sup>&</sup>lt;sup>2</sup>Radford et al., 2015; van den Oord et al., 2016 <sup>3</sup>Sønderby et al., 2016; Bachman, 2016



5 / 10

4 D > 4 A > 4 B > 4

## A hierarchical design

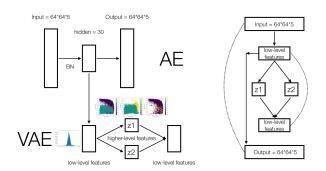
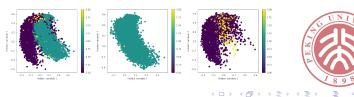


Figure: Left:AE + VAE; Right: VAE with the loss defined by AE

## A hierarchical design

- AE for low-level feature representation
  - Reproduce the original images with 30 hidden variables is easy
  - It's more robust to normalization methods.
  - Few hyperparameters to tune.
  - Can get 93% supervised accuracy
- 2 Then a VAE for classification
  - Use VAE instead of AE to use the double peak Gaussian prior
  - Lots of hyperparameters to tune (m, s, KL-term...); faster and easier
  - Was sensitive to initialization; use batchnormalization in AE
  - The optimization goal is more accessible: reproduce the 30 hidden variables in AE using 2 hidden units.



# Math part<sup>4</sup>

- "Generative modeling" is a broad area of machine learning which deals with models of distributions  $P_{gt}(X)$ , defined over datapoints X in some potentially high-dimensional space  $\mathcal{X}$ .
- Our goal is to learn a P(X) that is as similar as possible to  $P_{qt}(X)$
- Our SDSS images are  $64 \times 64 \times 5$ -dimensional images. Sample from such high-dimensional space is computationally expensive.
- An idea is that, if we can use some latent variable z that we can easily sample according to some probability density function (PDF) P(z) and then use a family of deterministic functions  $f(z;\theta)$ , parameterized by a vector  $\theta$  in some space  $\Theta$ . s.t.

$$P(X) = \int P_{\theta}(X|z)P(z)dz$$



<sup>4</sup>Tutorial on Variational Autoencoders, CARL DOERSCH, Carnegie Mellon / UC Berkeley

### Math part cont.

We are aiming at maximize the probability of each X in the training set under the entire generative process, according to:

$$P(X) = \int P_{\theta}(X|z)P(z)dz \tag{1}$$

The intuition here is maximum likelihood

In order to implement gradient descent (or any other optimization technique) to increase P(X) by making  $f(z;\theta)$  approach X for some z, the choice of this output distribution is often Gaussian, i.e.  $P(X|z;\theta) = N(X|f(z;\theta),\sigma^2*I)$  Now the problems in optimizing (1) are:

- how to define the latent variables z
- Thow to define the latent variables a
- 2 how to deal with the integral over z



### Math part cont.

- 1 how to define the latent variables z
  - Any distribution in d dimensions can be generated by taking a set of d variables that are normally distributed and mapping them through a sufficiently complicated function
  - Provided powerful function approximators, we can simply learn a function which maps our independent, normally-distributed z values to whatever latent variables might be needed for the model
  - $P(z) = \mathcal{N}(0, I)$
- 2 how to deal with the integral over z
  - $P(X) \approx \frac{1}{n} \sum_{i} P(X|z_i)$
  - Since P(X|z) is an isotropic Gaussian, the negative log probability of X proportional squared Euclidean distance between f(z) and X