## cs 107e

- §1 Baremetal systems programming
- §2 Building a personal computer
  - **■** Graphics
  - Keyboard
- §3 Topics in systems programming

## Systems Programming

Computer arithmetic (today)

Caches; debugging discussion

New systems prog lang: Rust and Go

Veronica, Quinn Dunki

To Linux and beyond

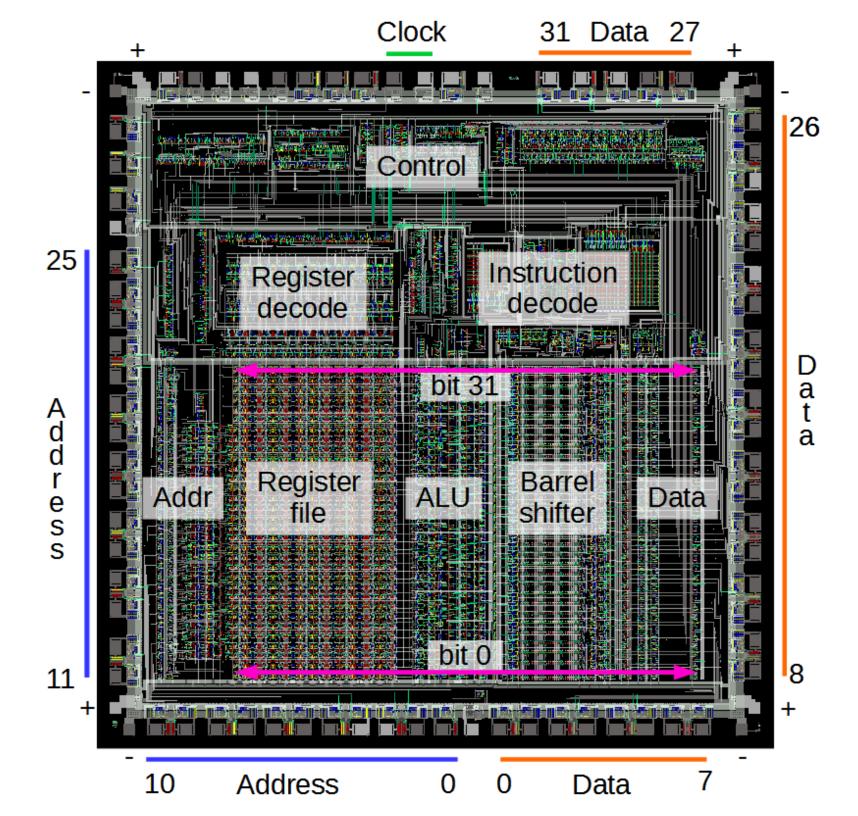
Final project demonstrations

Debugging discussion (due Mon)

Send me email with the answers to the following questions.

- 1. What was the most interesting bug in your cs107e code?
- 2. What symptoms let you to the bug?
- 3. How did you figure out what the problem was?
- 4. How did you fix it?

Due by 12 noon on Mon.



## Learning Goals

Processor flags: Z, N, C, V

Addition and carry, subtraction and borrow

2's complement representation of negative numbers

Signed and unsigned conversions (C craziness)

**Arithmetic-logic units (ALUs)** 

## Addition

247

9

\_ \_ \_

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\_ \_ \_

### High School Addition (Hexadecimal)

**F7** 

**09** 

\_ \_ \_

```
High School Addition (Hexadecimal)
```

F7 09

\_ \_ \_

```
High School Addition (Hexadecimal)
```

11

**F7** 

**09** 

\_ \_ \_

```
High School Addition (Hexadecimal)
```

11

**F7** 

**09** 

\_ \_ \_

```
11110111
00001001
```

```
High School Addition (Binary)
```

```
1
11110111
00001001
----
```

```
High School Addition (Binary)
```

```
11
11110111
00001001
----
```

```
111
11110111
00001001
-----
```

```
1111
11110111
00001001
```

```
11111
11110111
00001001
```

```
111111
11110111
00001001
```

```
1111111
11110111
00001001
```

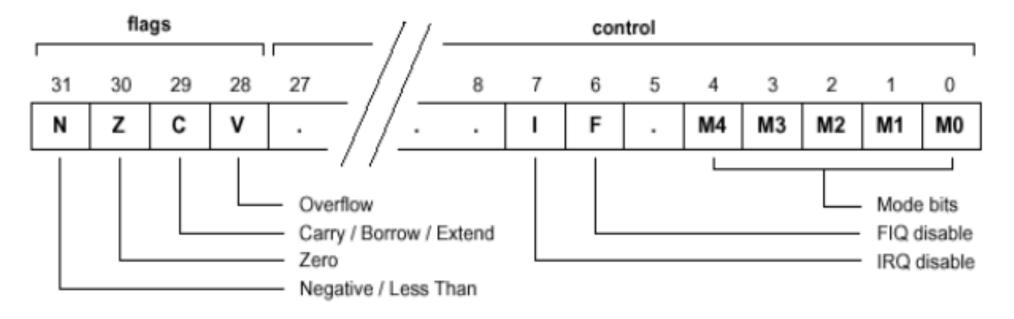
```
11111111
11110111
00001001
```

```
1111111
11110111
00001001
-----
```

Result: 00000000 (only room for 8-bits) Carry (C): 1 (extra bit)

To hold the result of adding two n-bit numbers requires n+1 bits

#### **CPSR**



Arithmetic instructions set Z, N, C, V Logic instructions set Z, N

We will cover V soon

# cpsr.c: uadd32

```
// Multiple precision addition
// https://gcc.godbolt.org/
int64_t add64(int64_t a, int64_t b)
  return a + b;
add64(int64_t, int64_t):
       adds
               r2, r2, r0 // adds, not add
               r3, r3, r1 // add w/ carry
       adc
               r0, r2
       mov
              r1, r3
       mov
              lr
       bx
```

## **Negative Numbers**

Up to now, all binary numbers have been positive (unsigned)

How would you define negative numbers?

A clever way of defining -1 is to say that it is the number that when added to 1, results in 0 mod 256

0xFF + 0x01 = 0x100 = 0x00

0xFF can be interpreted as -1

In this system, adding unsigned numbers is exactly the same as adding signed numbers. Cool!

How do we negate a number?

Subtract the number from 0!

1111111 0000000

0000001

\_\_\_\_\_

11111111

1111111 (0xFF) is -1

Note the borrows.

```
0x00 = 0
0xFF = -1
0xFE = -2
...
0x80 = -128 (could interpret as 128)
0x7F = 127
...
0x01 = 1
```

if we choose to *interpret* 0x80=-128, then the most-significant bit of the number indicates that it is negative (N) - sign bit

8-bit signed number range from -128 to 127 32-bit numbers from -2147483648 to 2147483647

```
But, 100000000 is more than 8-bits!
Rewrite as 100000000 = 11111111 + 1
-x = (11111111-x)+1
  11111111
 -00000001
  11111110 = ~00000001
  11111110
 +00000001
  11111111
```

### Negating

$$-x = \sim x + 1$$

Some nomenclature:

 $\sim x$ : One's complement ( $\sim 0-x$ )

 $\sim x + 1$ : Two's complement  $(2^{32}-x)$ 

#### Subtraction is negation and addition

$$a - b = a + (-b) = a + \sim b + 1$$

$$0x01 - 0x00 = 0x01+0xFF+0x01 = 0x01 + C$$

$$0x01 - 0x01 = 0x01+0xFE+0x01 = 0x00 + C$$

$$0x01 - 0x02 = 0x01+0xFD+0x01 = 0xFF$$

Note that carry is set if a >= b

borrow = !carry

# cpsr.c: usub32

```
// Multiple precision subtraction
// https://gcc.godbolt.org/
int64_t sub64(int64_t a, int64_t b)
  return a - b;
sub64(int64_t, int64_t):
       subs
               r2, r2, r0 // subs, not sub
               r3, r3, r1 // sub w/ carry
       sbc
               r0, r2
       mov
              r1, r3
       mov
              lr
       bx
```

# Signed subtraction - overflow (sub32)

```
8000000+0000001=80000001 : z=0,=1,c=0,uge=0
8000000-00000001=7fffffff : z=0,=0,c=1,uge=1
7fffffff+00000001=80000000 : z=0,=1,c=0,uge=0
7fffffff-00000001=7fffffe : z=0,=0,c=1,uge=1
-2147483648+1=-2147483647 : z=0,=1,c=0,v=0,ge=0
-2147483647+1=-2147483648 : z=0,=0,c=1,v=1,ge=0
2147483647-1= 2147483646 : z=0,=0,c=1,v=0,ge=1
```

"Overflow" happens when adding two numbers of the same sign, and getting a result with a different sign.

$$V = (n1 == n2) & (n != n1)$$

# Comparison

# unsigned comparison (usub32)

bcs: branch carry set (greater than or equal)

bcc: branch carry clear (less than)

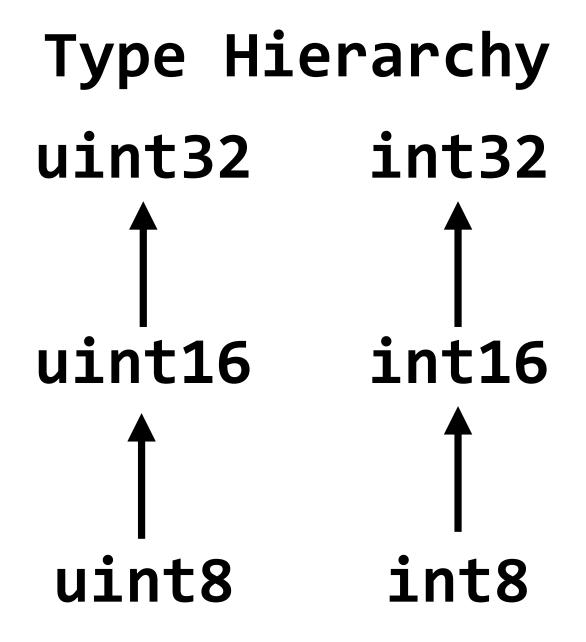
# Signed comparison (sub32)

```
8000000+0000001=80000001 : z=0,=1,c=0,uge=0
80000000-00000001=7fffffff : z=0,=0,c=1,uge=1
7ffffff+0000001=80000000 :
                            z=0,=1,c=0,uge=0
7fffffff-00000001=7ffffffe : z=0,=0,c=1,uge=1
-2147483648+1=-2147483647 :
                            z=0,=1,c=0,v=0,ge=0
-2147483648-1=2147483647:z=0,=0,c=1,v=1,ge=0
2147483647+1=-2147483648 : z=0,=1,c=0,v=1,ge=1
2147483647-1= 2147483646 :
                            z=0,=0,c=1,v=0,ge=1
bge: signed greater than or equal (n == v)
blt: signed less than (n != v)
int ge() { return !v ? n : !n }
```

Code	Suffix	Flags	Meaning
0000	EQ	Z set	equal
0001	NE	Z clear	not equal
0010	CS	C set	unsigned higher or same
0011	CC	C clear	unsigned lower
0100	МІ	N set	negative
0101	PL	N clear	positive or zero
0110	VS	V set	overflow
0111	VC	V clear	no overflow
1000	НІ	C set and Z clear	unsigned higher
1001	LS	C clear or Z set	unsigned lower or same
1010	GE	N equals V	greater or equal
1011	LT	N not equal to V	less than
1100	GT	Z clear AND (N equals V)	greater than
1101	LE	Z set OR (N not equal to V)	less than or equal
1110	AL	(ignored)	always

# Converting Signed and Unsigned Types in C

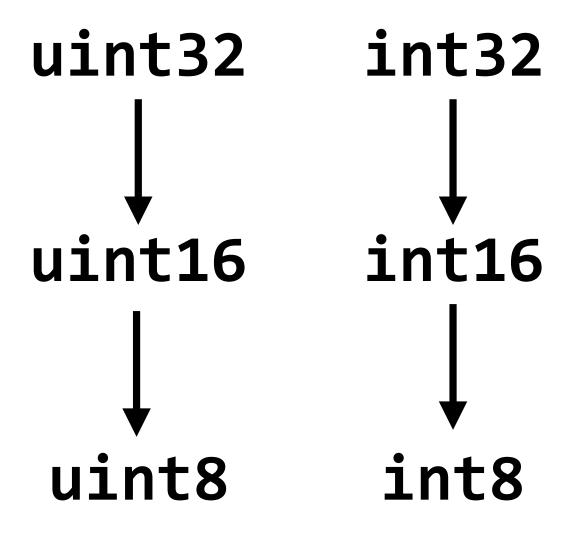
Ninja Job Interview Questions



Types are sets of allowed values
Arrow indicate subsets: uint8 ⊂ uint16

```
// Sign extension:extend signrightwards
// code/sign.c
int8 0xFE -> int32 0xFFFFFFE
int8 0x7E -> int32 0x0000007E
```

```
// Assembly language
LSL r0,r0,#24
ASR r0,r0,#24
```



**Truncate!** 

uint32

←int32

uint16 ← int16

uint8 ← int8

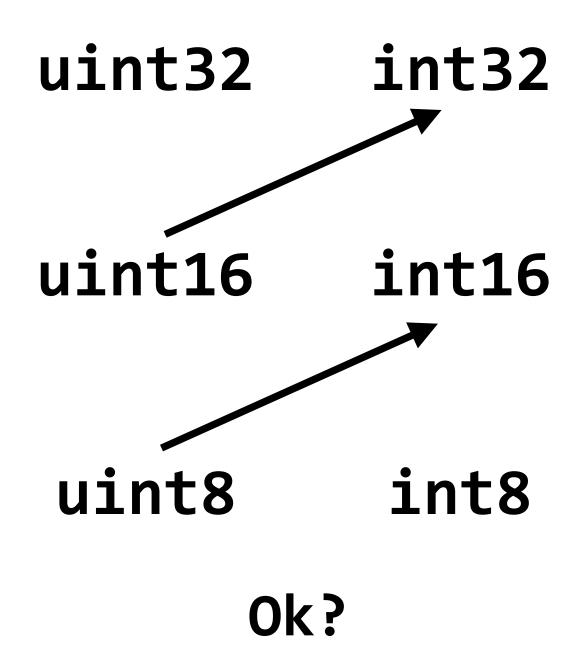
Ok?

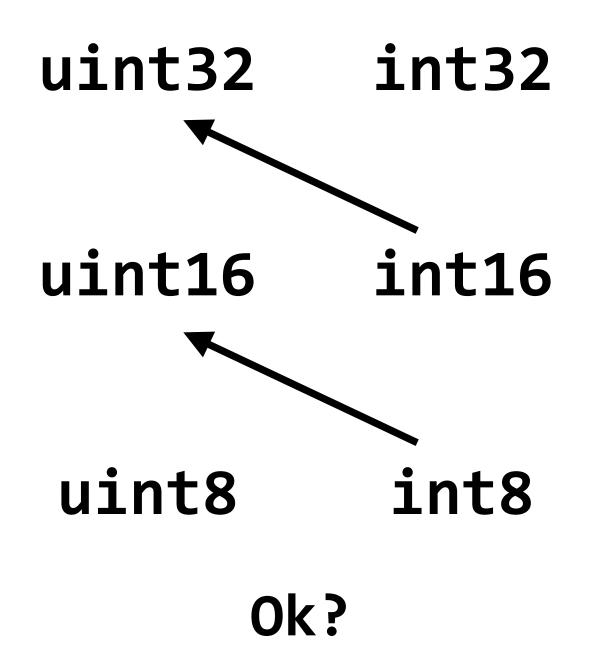
uint32—→int32

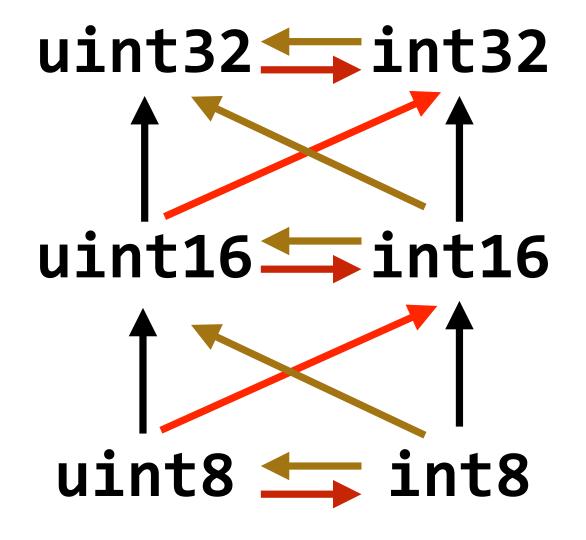
uint16 → int16

uint8 → int8

Ok?







technically, not defined
defined

# 6.3.1.3 Signed and unsigned integers

- 1 When a value with integer type is converted to another integer type other than \_Bool, if the value can be represented by the new type, it is unchanged.
- 2 Otherwise, if the new type is unsigned, the value is converted by repeatedly adding or subtracting one more than the maximum value that can be represented in the new type until the value is in the range of the new type.
- 3 Otherwise, the new type is signed and the value cannot be represented in it; either the result is implementation-defined or an implementation-defined signal is raised.

Operations involving signed and unsigned

int32 + uint32?

What is the type of the result?

Why is this the right thing to do?

Operations involving signed and unsigned

int32 + uint32?

What is the type of the result? Signed integers are changed to unsigned!

Why is this the right thing to do?
Unsigned conversion is well-defined

This leads to unexpected behavior!

```
#include <stdio.h>
int main(void)
    unsigned int a = 6;
    int b = -20;
    (b>a) ?
       puts("-20 > 6"):
       puts("-20 <= 6");</pre>
```

### 6.3.1.8 Usual arithmetic conversions

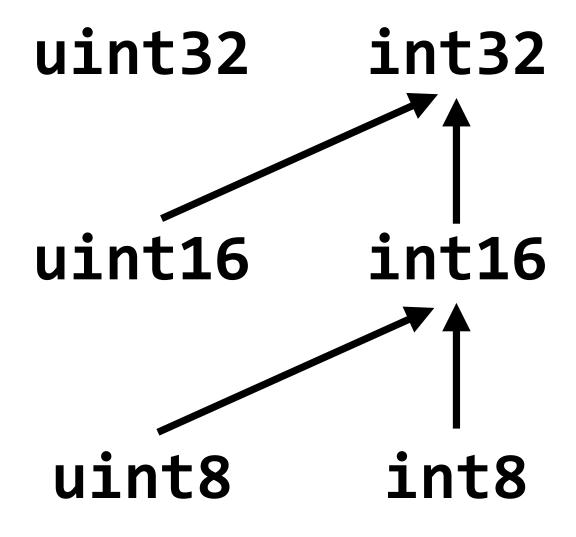
1 If both operands have the same type, then no further conversion is needed.

2 Otherwise, if both operands have signed integer types or both have unsigned integer types, the operand with the type of lesser integer conversion rank is converted to the type of the operand with greater rank.

3 Otherwise, if the operand that has unsigned integer type has rank greater or equal to the rank of the type of the other operand, then the operand with signed integer type is converted to the type of the operand with unsigned integer type.

4 Otherwise, if the type of the operand with signed integer type can represent all of the values of the type of the operand with unsigned integer type, then the operand with unsigned integer type is converted to the type of the operand with signed integer type.

5 Otherwise, both operands are converted to the unsigned integer type corresponding to the type of the operand with signed integer type.



Alternative: Promote to greatest common type

"Whenever you mix signed and unsigned numbers you get in trouble"

**Bjarne Stroustrup** 

# 1-Bit Adder

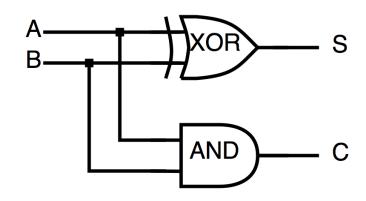
# Add 2 1-bit numbers

- a b sum
- 0 0 00
- 0 1 01
- 1 0 01
- 1 1 10

# Add 2 1-bit numbers (Half Adder)

```
a b sum0 0 000 1 011 0 011 1 10
```

bit 0 of sum: S = a^b
bit 1 of sum: C = a&b



Have reduced addition to bitwise, logical operations!

# Add 3 1-bit numbers

```
abc=sc
00000
0 1 0 0 1
100
       0 1
1 1 0
     1 0
0 0 1
       0 1
0 1 1
       1 0
1 0 1
       1 0
1 1 1
       1 1
```

# Add 3 1-bit numbers

a b	ci	=	S	CO	
0 0	0		0	0	
0 1	0		0	1	Full Adder
1 0	0		0	1	×
1 1	0		1	0	A S
0 0	1		0	1	
0 1	1		1	0	
1 0	1		1	0	
1 1	1		1	1	

# 8-bit adder

