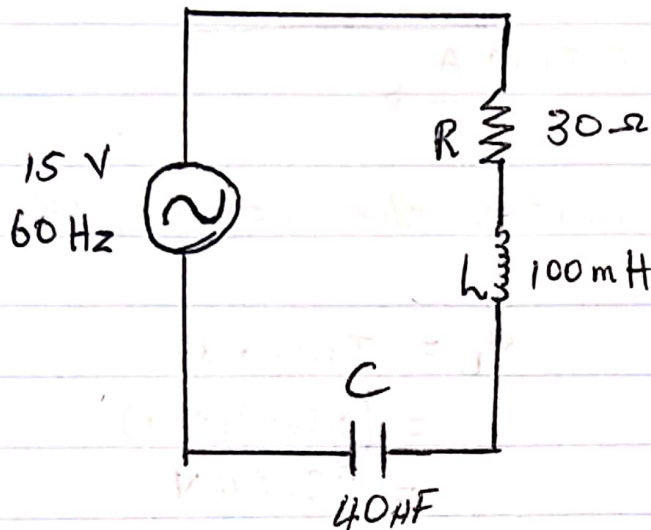


SERIES RLC CIRCUIT

* A $40\mu\text{F}$ capacitor is in series with a 100 mH inductor, a 30 ohm resistor, and a 15 V AC signal with a frequency of 60 Hz .



* Calculate the capacitive reactance and the inductive reactance in the circuit.

$$\begin{aligned} X_C &= \frac{1}{2\pi f \cdot C} \\ &= \frac{1}{2\pi \times (60) (40 \times 10^{-6})} \\ &= 66.3 \Omega \end{aligned}$$

$$\begin{aligned} X_L &= 2\pi f L \\ &= 2\pi \times (60) (100 \times 10^{-3}) \\ &= 37.7 \Omega \end{aligned}$$

* Determine the impedance of the circuit.

$$\begin{aligned} Z &= \sqrt{R^2 + (X_L - X_C)^2} \\ &= \sqrt{(30)^2 + (37.7 - 66.3)^2} \\ &= 41.45 \Omega \end{aligned}$$

* Calculate the rms current in this circuit.

$$\begin{aligned} I_{\text{rms}} &= \frac{V_s}{Z} \\ &= \frac{15}{41.45} \\ &= \underline{0.3619 \text{ A}} \end{aligned}$$

* Calculate voltage across the resistor, capacitor and inductor.

$$\begin{aligned} V_R &= I_{\text{rms}} \cdot R \\ &= (0.3619)(30) \\ &= 10.857 \text{ V} \end{aligned}$$

$$\begin{aligned} V_L &= I_{\text{rms}} \times X_L \\ &= (0.3619)(37.7) \\ &= 13.64 \text{ V} \end{aligned}$$

$$\begin{aligned} V_C &= I_{\text{rms}} \times X_C \\ &= (0.3619)(66.3) \\ &= 23.994 \text{ V} \end{aligned}$$

* How much power is consumed in the circuit?

$$\begin{aligned} P &= I^2 \cdot R \\ &= (0.3619)^2 \times (30) \\ &= 3.929 \text{ W} \end{aligned}$$

* What is the resonant frequency of this circuit?

$$\begin{aligned} f_R &= \frac{1}{2\pi\sqrt{L \times C}} \\ &= \frac{1}{2\pi\sqrt{(100 \times 10^{-3})(40 \times 10^{-6})}} \\ &= 79.57 \text{ Hz} \end{aligned}$$