# SES/RAS 598: Space Robotics and Al

Lecture 1: Course Introduction & State Estimation Overview

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### Lecture Outline

- Course Overview
- State Estimation Fundamentals
- 3 Linear Dynamical Systems
- 4 Next Steps

• **Meeting Times:** Tu/Th 10:30-11:45am

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  - Assignments (20%)
  - Midterm Project (20%)
  - Final Project (50%)
  - Class Participation (10%)

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- Prerequisites:
  - Linear algebra, calculus, probability theory
  - Python programming with NumPy, SciPy
  - Basic computer vision concepts
  - Linux/Unix systems experience

### Course Resources

#### Recommended Books:

- Probabilistic Robotics (Thrun, Burgard, Fox)
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- Parameter Estimation
- Gaussian Processes

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#### • Interactive Tutorials:

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#### Required Software:

- Linux OS
- ROS2
- Python with scientific computing libraries

# Why State Estimation?

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### • Impact on Space Exploration:

- Autonomous navigation
- Precision landing
- Sample collection

# Least Squares Estimation

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### • Applications:

- Sensor calibration
- Trajectory estimation
- Parameter identification

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  - More general framework
  - Handles different noise models

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- Space Applications:
  - Orbit determination
  - Attitude estimation
  - Sensor fusion

# State-Space Models

### System Dynamics:

$$x_{k+1} = Ax_k + Bu_k + w_k$$
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#### Components:

- State vector  $x_k$
- Input vector  $u_k$
- Measurement vector  $y_k$
- Process noise  $w_k$
- Measurement noise  $v_k$

# Case Study: Mars Rover Navigation

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### Challenges:

- Wheel slippage
- Varying terrain
- Limited computational resources

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#### Review:

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- Probability concepts
- Basic Python programming

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### • Reading:

- Skim Kalman filter basics
- Review assigned papers
- Explore interactive tutorials

# Questions?

# Thank you!

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