Lecture 1: Introduction to Management Science Introduction to Optimization and Linear Programming

1. Solve the following LP problem graphically by enumerating the corner points.

MAX: $2 X_1 + 7 X_2$ Subject to: $5 X_1 + 9 X_2 \le 90$ $9 X_1 + 8 X_2 \le 144$ $X_2 \le 8$

 $X_1, X_2 \ge 0$

2. Solve the following LP problem graphically using level curves.

Solve the following LF problem MAX: $7 X_1 + 4 X_2$ Subject to: $2 X_1 + X_2 \le 16$ $X_1 + X_2 \le 10$ $2 X_1 + 5 X_2 \le 40$ $X_1, X_2 \ge 0$

3. Solve the following LP problem graphically by enumerating the corner points.

MIN: $8 X_1 + 3 X_2$ Subject to: $X_2 \ge 8$ $8 X_1 + 5 X_2 \ge 80$ $3 X_1 + 5 X_2 \ge 60$ $X_1, X_2 \ge 0$

4. Solve the following LP problem graphically using level curves.

Solve the following Li proof

MAX: $5 X_1 + 3 X_2$ Subject to: $2 X_1 - 1 X_2 \le 2$ $6 X_1 + 6 X_2 \ge 12$ $1 X_1 + 3 X_2 \le 5$ $X_1, X_2 \ge 0$

5. Solve the following LP problem graphically using level curves.

MIN: $5 X_1 + 7 X_2$ Subject to: $4 X_1 + 1 X_2 \ge 16$ $6 X_1 + 5 X_2 \ge 60$ $5 X_1 + 8 X_2 \ge 80$ $X_1, X_2 \ge 0$

Lecture 1: Question Bank

6. Jones Furniture Company produces beds and desks for college students. The production process requires carpentry and varnishing. Each bed requires 6 hours of carpentry and 4 hour of varnishing. Each desk requires 4 hours of carpentry and 8 hours of varnishing. There are 36 hours of carpentry time and 40 hours of varnishing time available. Beds generate \$30 of profit and desks generate \$40 of profit. Demand for desks is limited so at most 8 will be produced.

x1 = num of bed, x2 = num of deskFormulate the LP model for this problem.

MAX: 30*x2+40*x1 RE: x2<=8

6x1+4x2<=36 Solve the problem using the graphical method. 4x1+8x2<=40

7. The Big Bang explosives company produces customized blasting compounds for use in the mining industry. The two ingredients for these explosives are agent A and agent B. Big Bang just received an order for 1400 pounds of explosive. Agent A costs \$5 per pound and agent B costs \$6 per pound. The customer's mixture must contain at least 20% agent A and at least 50% agent B. The company wants to provide the least expensive mixture which will satisfy the customers requirements.

x1 = num of AA, x2 = num of ABFormulate the LP model for this problem.

MIN: 5*x1+6*x2 RF: x1+x2=1400

Solve the problem using the graphical method.

x1>=20%*1400 x2>=50%*1400

8. Bob and Dora Sweet wish to start investing \$1,000 each month. The Sweets are looking at five investment plans and wish to maximize their expected return each month. Assume interest rates remain fixed and once their investment plan is selected they do not change their mind. The investment plans offered are:

> Fidelity 9.1% return per year x1 = num of fi, x2 = num of op, x3 = num of ca, x4 = num of sa, x5 = num of na, Optima 16.1% return per year MAX: 9.1%x1+16.1%x2+7.3%x3+5.6%x4+12.3%x5 RE: 0<x1+x2+x3+x4+x5<=1000 CaseWay 7.3% return per year x2+x5<=30%*1000 Safeway 5.6% return per year x4+x1>=40%*1000

National 12.3% return per year

Since Optima and National are riskier, the Sweets want a limit of 30% per month of their total investments placed in these two investments. Since Safeway and Fidelity are low risk, they want at least 40% of their investment total placed in these investments.

Formulate the LP model for this problem.

Reference:

Ragsdale, C. T., Spreadsheet Modelling and Decision Analysis 5th Ed, Thomson, 2008: Chapter 1 & 2