

The following table gives Euclidean algorithm working showing that $\gcd(327,75)=3$.

$$327 = 4 \times 75 + 27$$

$$75 \quad = \quad 2 \quad \times \quad 27 \quad + \quad 21$$

$$27 \quad = \quad 1 \quad \times \quad 21 \quad + \quad 6$$

$$21 = 3 \times 6 + 3$$

$$6 = 2 \times 3 + 0$$

Use the extended Euclidean algorithm to complete the following table. Remember to enter negative numbers where appropriate.

$$3 = \begin{vmatrix} 1 & \times 21 & + \end{vmatrix} -3 \times 6$$

$$3 = \begin{vmatrix} -3 & \times & 27 & + & -4 & \times & 21 \end{vmatrix}$$

$$3 = \begin{vmatrix} 4 & \times 75 + \end{vmatrix} -11 \times 27$$

Enter an integer z such that $75z\equiv 12\pmod{327}$ and $0\leq z\leq 326$:

Let x and y be integers such that $x \equiv 4 \pmod 9$ and $y \equiv 7 \pmod 9$. Find the integer z such that $93x + 4y^2 \equiv z \pmod 9$ and $0 \le z \le 8$.

Answer: 10