

Aufgabenblatt 14 - Daniel Norman

The notation for Aufwand is as follows:

A-OPERATION

e.g. for addition

A-+

Aufgabe 1.3

building the polynom

```
A-exp(n) = A-=, A-=, A-even + A-odd +  
           max(A-/ + A-exp(n/2) + A-*,  
              A-- + A-/ + A-exp((n-1)/2) + 2*A-*)  
A-exp(n) = 2*A-= + A-even + A-odd + A-- + A-/ + A-exp((n-1)/2) + 2*A-*=  
A-exp(n) = 2*const-equality + const-even + const-odd + const-subtraction + const-division  
           + A-exp(x, (n-1)/2) + 2 * const-multiplication  
A-exp(n) = const-all + A-exp((n-1)/2)
```

matching the variables

```
b = const  
c = 1  
k = 0
```

A-exp $\in O(\log n)$

Aufgabe 3.2

Best-case

building the polynom

```
A-qsort(n)  
= n*A-< + A-qsort(lesser) + A-+++ + A-qsort(greaterEq)  
= n*const-< + const-+++ + A-qsort(lesser) + A-qsort(greaterEq)  
= n*const-< + const-+++ + 2A-qsort((n-1)/2)  
= n + const-all + 2A-qsort((n-1)/2)
```

NOTE $A\text{-qsort(lesser)} + A\text{-qsort(greaterEq)} \sim 2A\text{-qsort}((n-1)/2)$

matching variables

```
c = 2  
b = 1  
k = 1
```

matching polynom in the complexity table

$O(n^k \cdot \log(n)) = O(n \log(n))$

Worst-case (when the list is already ordered)

building the polynom

```

A-qsrt(n) = n*A-< + A-qsrt(lesser) + A-++ + A-qsrt(greaterEq)
           = n*const-< + const-++ + A-qsrt(lesser) + A-qsrt(greaterEq)
           = n*const-< + const-++ + A-qsrt(n-1)
           = n + const-all + A-qsrt(n-1)

```

NOTE: A-qsrt(lesser) is empty and A-qsrt(greaterEq) = A-qsrt(n-1)

matching variables

```

c = 1
b = 1
k = 1

```

matching polynom in the complexity table

$O(n^{k+1}) = O(n^2)$