

# CPSC-354 Report

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## The MU Puzzle

The MU Puzzle, introduced in Chapter 1, starts with a very simple setup the axiom string **MI** and four rules that let us change or extend the string using the letters M, I, and U. The puzzle asks whether it's possible to reach the string **MU** by applying these rules.

At first glance it seems like it might work if you just keep trying different combinations, but after some trial and error this problem will not have a solution. The key observation is that no matter what rule you apply, the number of I's never becomes a multiple of three. It always stays in a certain pattern.

- The starting axiom  $MI$  has one I.
- Rule 1 ( $xI \rightarrow xIU$ ) adds a U at the end, but doesn't change the number of I's.
- Rule 2 ( $Mx \rightarrow Mxx$ ) doubles the part after the M, which changes the number of I's but never makes it a multiple of three.
- Rule 3 ( $III \rightarrow U$ ) removes three I's, so the overall pattern stays the same.
- Rule 4 ( $UU \rightarrow \text{delete}$ ) only affects U's, not I's.

So the system never produces a string where the number of I's is a multiple of three. Since  $MU$  has zero I's, it doesn't fit the pattern, which means there's no way to reach it from  $MI$ .

For example, starting with  $MI$  (which has 1 I), Rule 1 gives  $MIU$ . This still has 1 I. If we keep going,  $MIU \rightarrow MIUIU$  using Rule 2, the number of I's doubles to 2. At no point does the number of I's ever become a multiple of three, which is why  $MU$  can't be reached.

## Conclusion

In the end, the MU puzzle has no solution. The rules simply don't allow us to create  $MU$  starting from  $MI$ . By spotting the pattern with the I's, we can prove once and for all that  $MU$  is unreachable.