



# Normalization of Relations

- **Normalization:**

- The process of decomposing unsatisfactory "bad" relations by breaking up their attributes into smaller relations

- **Normal form:**

- Condition using keys and FDs of a relation to certify whether a relation schema is in a particular normal form

- 2NF, 3NF, BCNF □based on keys and FDs of a relation schema
- Practical Use of Normal Forms: Normalization is carried out in practice so that the resulting designs are of high quality and meet the desirable properties

- A **superkey** of a relation schema  $R = \{A_1, A_2, \dots, A_n\}$  is a set of attributes  $S$  *subset-of*  $R$  with the property that no two tuples  $t_1$  and  $t_2$  in any legal relation state  $r$  of  $R$  will have  $t_1[S] = t_2[S]$

**Candidate Keys:**

## Example: Super key

| Emp_SSN   | Emp_Number | Emp_Name  |
|-----------|------------|-----------|
| -----     | -----      | -----     |
| 123456789 | 226        | Steve     |
| 999999321 | 227        | Ajeet     |
| 888997212 | 228        | Chaitanya |
| 777778888 | 229        | Robert    |

- {Emp\_SSN}
- {Emp\_Number}
- {Emp\_SSN, Emp\_Number}
- {Emp\_SSN, Emp\_Name}
- {Emp\_SSN, Emp\_Number, Emp\_Name}
- {Emp\_Number, Emp\_Name}

## Example: candidate key

a candidate key is a minimal super key with no redundant attributes

- {Emp\_SSN}
- {Emp\_Number}

A **Primary key** is selected from a set of candidate keys. This is done by database admin or database designer.

We can say that either {Emp\_SSN} **or** {Emp\_Number} can be chosen as a primary key

<Student>

| Student_ID | Student_Enroll | Student_Name | Student_Email |
|------------|----------------|--------------|---------------|
| S02        | 4545           | Dave         | ddd@gmail.com |
| S34        | 4541           | Jack         | jjj@gmail.com |
| S22        | 4555           | Mark         | mmm@gmail.com |

The following are the super keys for the above table –

{Student\_ID}  
{Student\_Enroll}  
{Student\_Email}  
{Student\_ID, Student\_Enroll}  
{Student\_ID, Student\_Name}  
{Student\_ID, Student\_Email}  
{Student\_Name, Student\_Enroll}  
{Student\_ID, Student\_Enroll, Student\_Name}  
{Student\_ID, Student\_Enroll, Student\_Email}  
{Student\_ID, Student\_Enroll, Student\_Name, Student\_Email}

The following would be the candidate key from the above –

{Student\_ID}  
{Student\_Enroll}  
{Student\_Email}


## 3.2 First Normal Form 1NF

- A relation scheme  $R$  is in first normal form (1NF) if the values in  $dom(A)$  are atomic for every attribute  $A$  in  $R$ .
- **Disallows**
  - composite attributes
  - Set-valued attributes
  - **nested relations**; a cell of an *individual tuple* is a complex relation

(a)


**DEPARTMENT**

| Dname | <u>Dnumber</u> | Dmgr_ssn | Dlocations |
|-------|----------------|----------|------------|
|       |                |          |            |



(b)


**DEPARTMENT**



| Dname          | <u>Dnumber</u> | Dmgr_ssn  | Dlocations                     |
|----------------|----------------|-----------|--------------------------------|
| Research       | 5              | 333445555 | {Bellaire, Sugarland, Houston} |
| Administration | 4              | 987654321 | {Stafford}                     |
| Headquarters   | 1              | 888665555 | {Houston}                      |

(c)

**DEPARTMENT**



| Dname          | <u>Dnumber</u> | Dmgr_ssn  | <u>Dlocation</u> |
|----------------|----------------|-----------|------------------|
| Research       | 5              | 333445555 | Bellaire         |
| Research       | 5              | 333445555 | Sugarland        |
| Research       | 5              | 333445555 | Houston          |
| Administration | 4              | 987654321 | Stafford         |
| Headquarters   | 1              | 888665555 | Houston          |



**EMP\_PROJ**

| Ssn       | Ename                | Pnumber | Hours |
|-----------|----------------------|---------|-------|
| 123456789 | Smith, John B.       | 1       | 32.5  |
|           |                      | 2       | 7.5   |
| 666884444 | Narayan, Ramesh K.   | 3       | 40.0  |
| 453453453 | English, Joyce A.    | 1       | 20.0  |
|           |                      | 2       | 20.0  |
| 333445555 | Wong, Franklin T.    | 2       | 10.0  |
|           |                      | 3       | 10.0  |
|           |                      | 10      | 10.0  |
|           |                      | 20      | 10.0  |
| 999887777 | Zelaya, AliciaJ.     | 30      | 30.0  |
|           |                      | 10      | 10.0  |
| 987987987 | Jabbar, Ahmad V.     | 10      | 35.0  |
|           |                      | 30      | 5.0   |
| 987654321 | Wallace, Jennifer S. | 30      | 20.0  |
|           |                      | 20      | 15.0  |
| 888665555 | Borg, James E.       | 20      | NULL  |

← Composite attributes

(c)

**EMP\_PROJ1**

| Ssn | Ename |
|-----|-------|
|-----|-------|

**EMP\_PROJ2**

| Ssn | Pnumber | Hours |
|-----|---------|-------|
|-----|---------|-------|

**Figure 10.9**

Normalizing nested relations into 1NF. (a) Schema of the EMP\_PROJ relation with a *nested relation* attribute PROJ.S. (b) Example extension of the EMP\_PROJ relation showing nested relations within each tuple. (c) Decomposition of EMP\_PROJ into relations EMP\_PROJ1 and EMP\_PROJ2 by propagating the primary key.

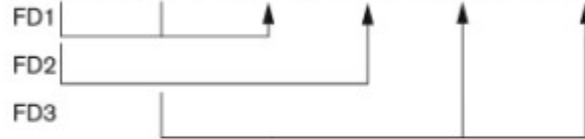
## Second Normal Form

- A relation scheme **R** is in second normal form (**2NF**) with respect to a set of FDs **F** if it is in 1NF and every nonprime attribute is fully dependent on every key of **R**.

(a)

EMP\_PROJ

| Ssn | Pnumber | Hours | Ename | Pname | Plocation |
|-----|---------|-------|-------|-------|-----------|
|-----|---------|-------|-------|-------|-----------|



2NF Normalization

EP1

| Ssn | Pnumber | Hours |
|-----|---------|-------|
|-----|---------|-------|



EP2

| Ssn | Ename |
|-----|-------|
|-----|-------|



EP3

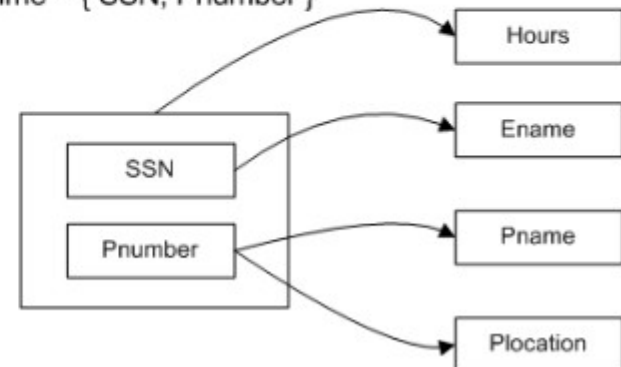
| Pnumber | Pname | Plocation |
|---------|-------|-----------|
|---------|-------|-----------|

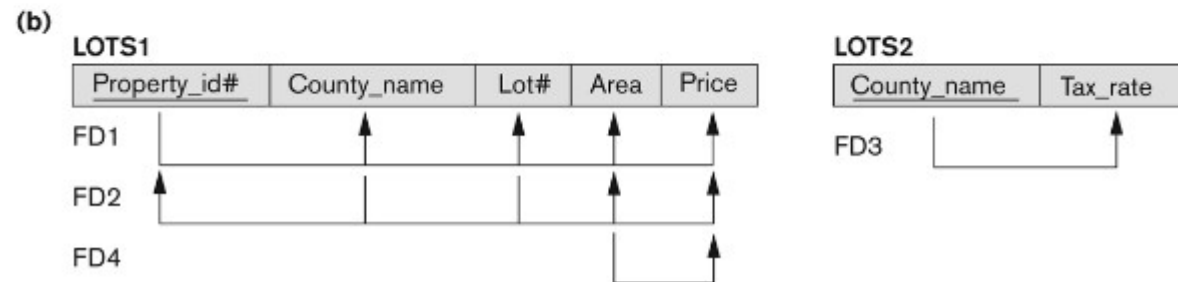
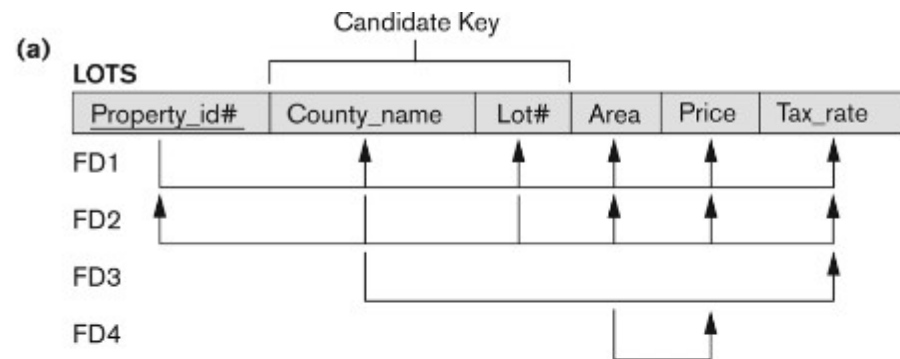


Figure 10.10

Normalizing into 2NF and 3NF.  
(a) Normalizing EMP\_PROJ into 2NF relations.  
(b) Normalizing EMP\_DEPT into 3NF relations.

Prime = { SSN, Pnumber }





Student(IDSt, StudentName, IDProf, ProfessorName, Grade)

1. The attribute ProfessorName is functionally dependent on attribute IDProf (IDProf  $\rightarrow$  ProfessorName)
2. The attribute StudentName is functionally dependent on IDSt (IDSt  $\rightarrow$  StudentName)
3. The attribute Grade is fully functional dependent on IDSt and IDProf (IDSt, IDProf  $\rightarrow$  Grade)

Students

| IDSt | LastName | IDProf | Prof       | Grade |
|------|----------|--------|------------|-------|
| 1    | Mueller  | 3      | Schmid     | 5     |
| 2    | Meier    | 2      | Borner     | 4     |
| 3    | Tobler   | 1      | Bernasconi | 6     |

Startsituation



Students

| ID | LastName |
|----|----------|
| 1  | Mueller  |
| 2  | Meier    |
| 3  | Tobler   |

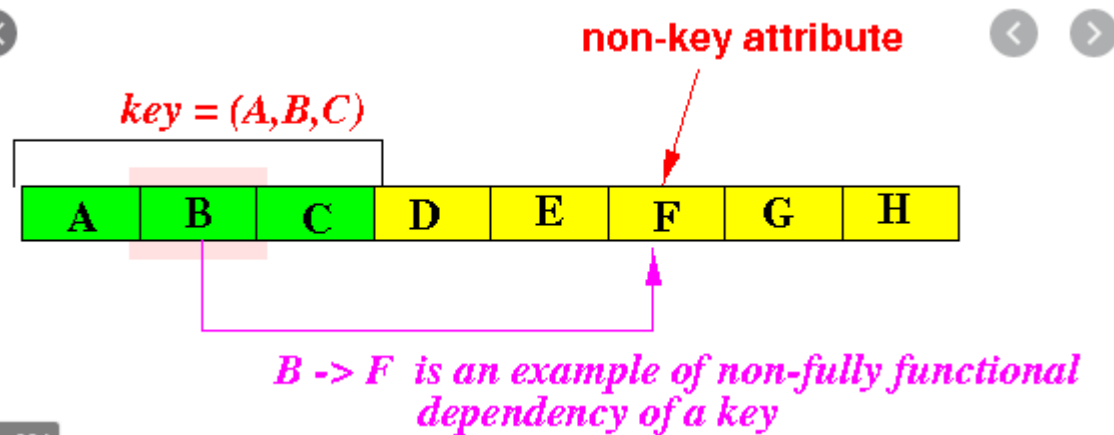
Result after normalisation

Professors

| IDProf | Professor  |
|--------|------------|
| 1      | Bernasconi |
| 2      | Borner     |
| 3      | Schmid     |

Grades

| IDStIDProf | Grade |   |
|------------|-------|---|
| 1          | 3     | 5 |
| 2          | 2     | 4 |
| 3          | 1     | 6 |



- A relation schema  $R$  is in **third normal form (3NF)** if whenever a FD  $X \rightarrow A$  holds in  $R$ , then either:
  - (a)  $X$  is a superkey of  $R$ , or
  - (b)  $A$  is a prime attribute of  $R$

SO no non-prime attribute  $A$  in  $R$  is transitively dependent on the primary key

## Example

Key: { SID }

SID  $\rightarrow$  Building

Building  $\rightarrow$  Fee

Building  $\rightarrow$  Mgr

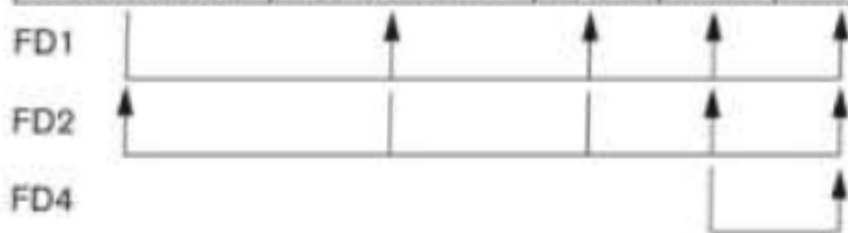
| SID | Building    | Fee | Manager |
|-----|-------------|-----|---------|
| 100 | Fenn        | 300 | Mr. T   |
| 300 | $\Delta\Pi$ | 400 | Ali     |
| 200 | Holiday Inn | 400 | Tyson   |



(b)

LOTS1

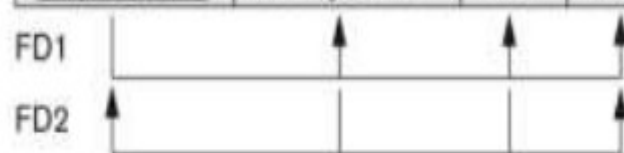
| <u>Property_id#</u> | County_name | Lot# | Area | Price |
|---------------------|-------------|------|------|-------|
|---------------------|-------------|------|------|-------|



(c)

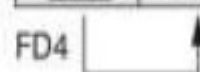
LOTS1A

| <u>Property_id#</u> | County_name | Lot# | Area |
|---------------------|-------------|------|------|
|---------------------|-------------|------|------|



LOTS1B

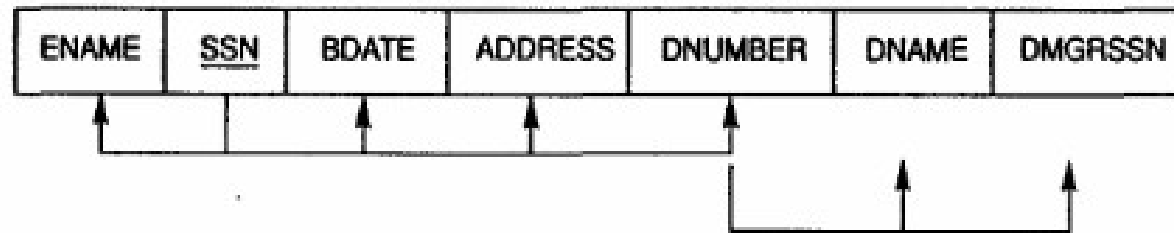
| <u>Area</u> | Price |
|-------------|-------|
|-------------|-------|





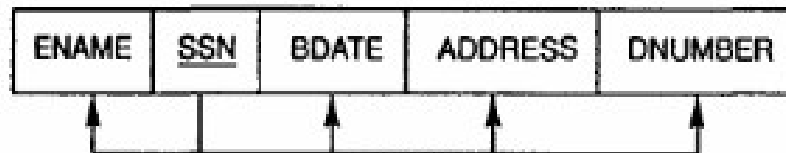
(b)

EMP\_DEPT

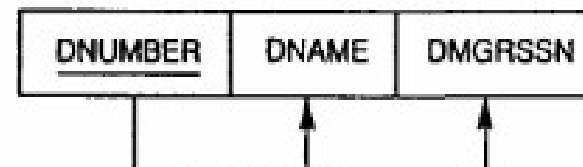


3NF NORMALIZATION

ED1



ED2



## BCNF (Boyce-Codd Normal Form)

- A relation schema R is in Boyce-Codd Normal Form (BCNF) if whenever an **FD  $X \rightarrow A$**  holds in R, then **X is a superkey** of R
- Each normal form is strictly stronger than the previous one
  - Every 2NF relation is in 1NF
  - Every 3NF relation is in 2NF
  - Every BCNF relation is in 3NF
- There exist relations that are in 3NF but not in BCNF
- The goal is to have each relation in BCNF (or 3NF)

(a)

**LOTS1A**

| <u>Property_id#</u> | County_name | Lot# | Area |
|---------------------|-------------|------|------|
|---------------------|-------------|------|------|



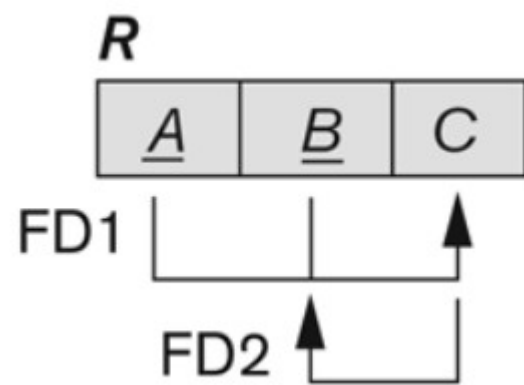
BCNF Normalization

**LOTS1AX**

| <u>Property_id#</u> | Area | Lot# |
|---------------------|------|------|
|---------------------|------|------|

**LOTS1AY**

| <u>Area</u> | County_name |
|-------------|-------------|
|-------------|-------------|



Consider the following relationship : **R (A,B,C,D)**

and following dependencies :

**A -> BCD**

**BC -> AD**

**D -> B**

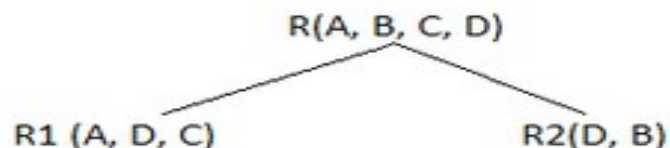
Above relationship is already in 3rd NF. Keys are **A** and **BC**.

Hence, in the functional dependency, **A -> BCD**, A is the super key.

in second relation, **BC -> AD**, BC is also a key.

but in, **D -> B**, D is not a key.

Hence we can break our relationship R into two relationships **R1** and **R2**.



Breaking, table into two tables, one with A, D and C while the other with D and B.