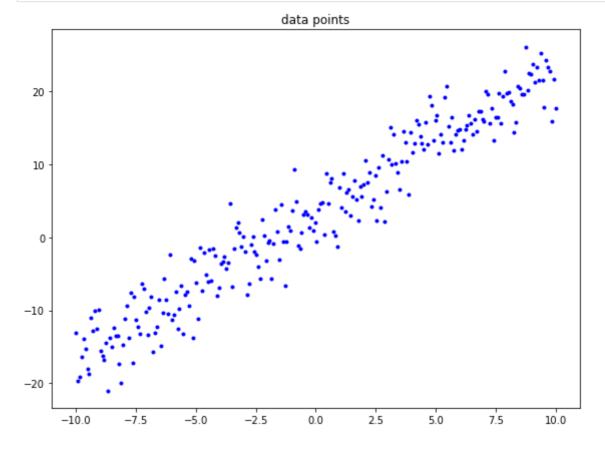
Linear regression

import library

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
import matplotlib.colors as colors
from mpl_toolkits.mplot3d import Axes3D
```

load data points

• $\{(x_i, y_i)\}_{i=1}^n$



compute the residual

compute the loss

• useful functions: np.inner

compute the gradient with respect to θ_0

• useful functions: np.inner

```
# ++++++++
return derivative
```

compute the gradient with respect to $heta_1$

• useful functions: np.inner

gradient descent for the optimization

```
In [ ]:
       number_iteration = 500
       learning_rate = 0.01
                      = ()
       theta0
                       = 0
       theta1
       list_theta0 = np.zeros(number_iteration)
       list_theta1
                      = np.zeros(number_iteration)
       list_loss
                     = np.zeros(number_iteration)
       for i in range(number_iteration):
          # complete the blanks
          theta0 = theta0 - learning_rate*compute_gradient_theta0(x, y, theta0, theta1)
          theta1 = theta1 - learning_rate*compute_gradient_theta1(x, y, theta0, theta1)
          loss = compute_loss(x, y, theta0, theta1)
          list_theta0[i] = theta0
          list\_theta1[i] = theta1
          list_loss[i] = loss
```

functions for presenting the results

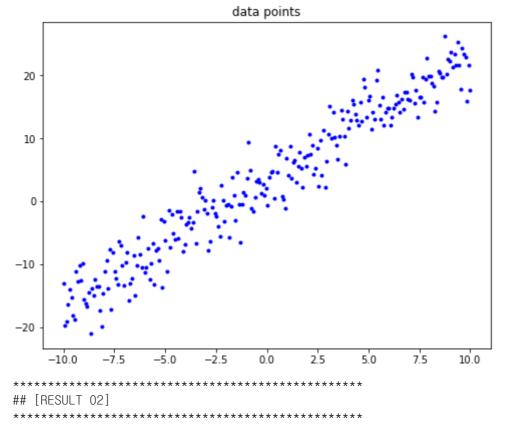
```
In [ ]:
         def function_result_01():
             plt.figure(figsize=(8,6))
             plt.plot(x, y, '.', color='blue')
              plt.title('data points')
              plt.show()
In [ ]:
         def function result 02():
             plt.figure(figsize=(8,6))
             ax = plt.gca()
             plt.plot(list_theta0, '-', color='blue', label=r'$\text{\text{wtheta_0$'}}
              plt.plot(list_theta1, '-', color='red', label=r'$\text{\text{W}theta_1$}')
             plt.title('model parameters')
              ax.legend()
             plt.show()
In [ ]:
         def function_result_03():
             plt.figure(figsize=(8,6))
             plt.plot(list_loss, '-', color='blue')
             plt.title('loss curve')
              plt.show()
In [ ]:
         def function_result_04():
              f = theta0 + theta1 * x
             plt.figure(figsize=(8,6))
              ax = plt.gca()
             plt.plot(x, y, '.', color='blue', label='data point')
             plt.plot(x, f, '-', color='red', label='regression')
             plt.title('regression')
              ax.legend()
              plt.show()
In [ ]:
         def function_result_05():
             X0 = np.arange(-10, 10, 0.1)
             X1 = np.arange(-10, 10, 0.1)
             grid_theta0, grid_theta1 = np.meshgrid(X0, X1)
             grid_loss = np.zeros(grid_theta0.shape)
              for i, t0 in enumerate(X0):
                  for j, t1 in enumerate(X1):
                      grid_loss[j, i] = compute_loss(x, y, t0, t1)
              fig = plt.figure(figsize=(8,6))
              ax = fig.add_subplot(111, projection='3d')
              plt.title('loss surface')
             ax = plt.axes(projection='3d')
```

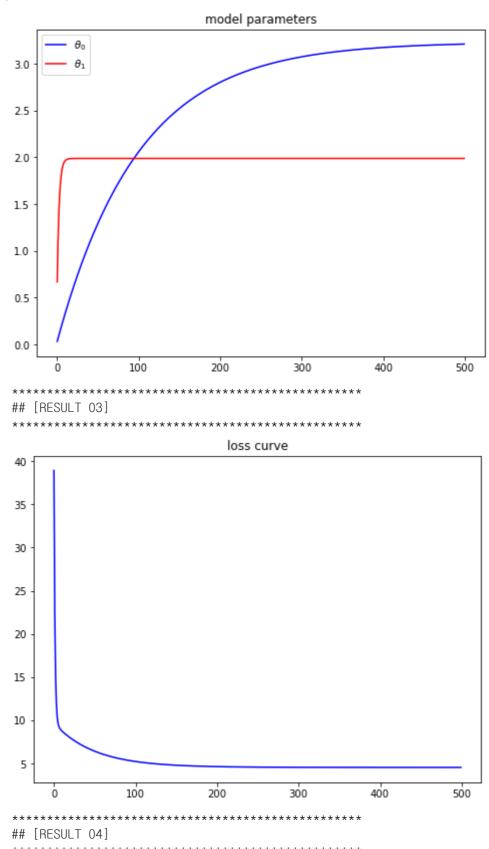
```
ax.set_xlabel(r'$\text{wtheta_0$'})
ax.set_ylabel(r'$\text{wtheta_1$'})
ax.set_zlabel('loss')

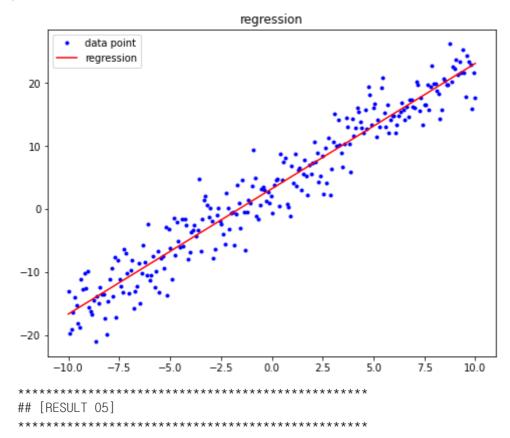
ax.plot_surface(grid_theta0, grid_theta1, grid_loss, rstride=1, cstride=1, cmap='
plt.tight_layout()
plt.show()
```

results

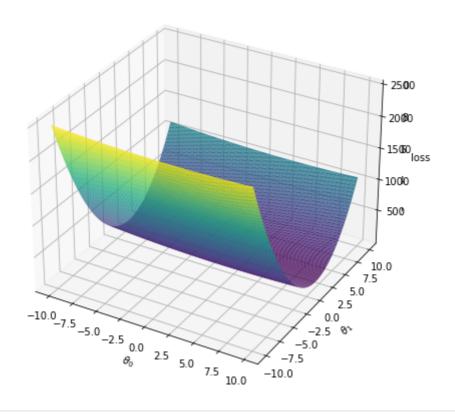
[RESULT 01]











In []: