Logistic Regression

import library

```
import numpy as np
import matplotlib.pyplot as plt
import matplotlib.colors as colors
from matplotlib import ticker, cm
```

load training data

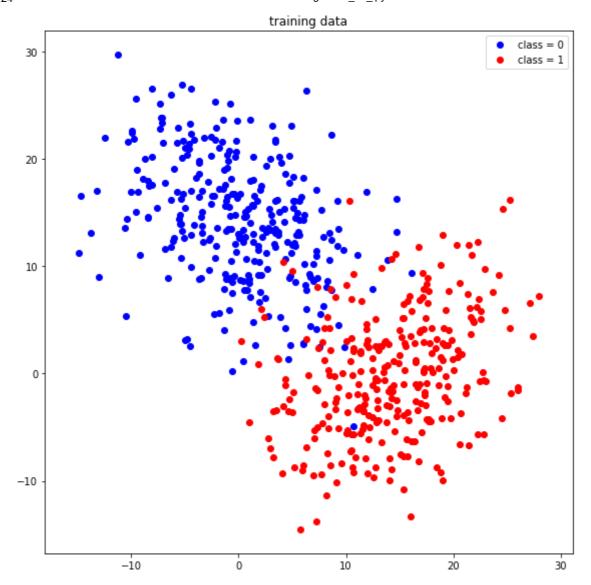
```
In [ ]:
         fname_data = 'assignment_08_data.csv'
                   = np.genfromtxt(fname_data, delimiter=',')
         number_data = data.shape[0]
         point_x = data[:, 0]
         point_y = data[:, 1]
         label = data[:, 2]
         print('number of data = ', number_data)
         print('data\ type\ of\ point\ x=',\ point\_x.dtype)
         print('data type of point y = ', point_y.dtype)
         point_x_class_0 = point_x[label == 0]
         point_y_class_0 = point_y[label == 0]
         point_x_class_1 = point_x[label == 1]
         point_y_class_1 = point_y[label == 1]
        number of data = 600
        data type of point x = float64
        data type of point y = float64
```

data type of point y - Tic

plot the data

```
In []:
    f = plt.figure(figsize=(8,8))

plt.title('training data')
    plt.plot(point_x_class_0, point_y_class_0, 'o', color='blue', label='class = 0')
    plt.plot(point_x_class_1, point_y_class_1, 'o', color='red', label='class = 1')
    plt.axis('equal')
    plt.legend()
    plt.tight_layout()
    plt.show()
```



define the linear regression function

```
• \theta = (\theta_0, \theta_1, \theta_2)
```

$$ullet$$
 point = $(1,x,y)\in\mathbb{R}^3$

define sigmoid function with input

 $ullet z \in \mathbb{R}$

```
In [ ]: def sigmoid(z):
```

define the logistic regression function

```
• \theta = (\theta_0, \theta_1, \theta_2) \in \mathbb{R}^3
```

```
• point = (1,x,y)\in\mathbb{R}^3
```

define the residual function

```
• \theta = (\theta_0, \theta_1, \theta_2) \in \mathbb{R}^3
```

• point
$$=(x,y)\in\mathbb{R}^2$$

• label =
$$l \in \{0, 1\}$$

define the loss function for the logistic regression

```
\bullet \ \ \theta = (\theta_0, \theta_1, \theta_2) \in \mathbb{R}^3
```

$$ullet$$
 point $=(1,x,y)\in\mathbb{R}^3$

• label = $l \in \{0, 1\}$

define the gradient of the loss with respect to the model parameter $\boldsymbol{\theta}$

```
egin{aligned} & 	heta = (	heta_0, 	heta_1, 	heta_2) \in \mathbb{R}^3 \ & 	heta 	ext{ point} = (1, x, y) \in \mathbb{R}^3 \ & 	heta 	ext{ label} = l \in \{0, 1\} \end{aligned}
```

initialize the gradient descent algorithm

```
In []:
    num_iteration = 5000 # USE THIS VALUE for the number of gradient descent iterations
    learning_rate = 0.001 # USE THIS VALUE for the learning rate

theta = np.array((0, 0, 0))
    theta_iteration = np.zeros((num_iteration, theta.size))
    loss_iteration = np.zeros(num_iteration)

number_point_class_0 = len(point_x_class_0)
    number_point_class_1 = len(point_x_class_1)

point_class_0 = np.ones((number_point_class_0, 3))
    point_class_1 = np.ones((number_point_class_1, 3))

point_class_0[:, 1] = point_x_class_0
    point_class_0[:, 2] = point_y_class_0

point_class_1[:, 1] = point_x_class_1
```

```
point_class_1[:, 2] = point_y_class_1
          = np.zeros(number_point_class_0)
label_1 = np.ones(number_point_class_1)
point = np.concatenate((point_class_0, point_class_1), axis=0)
label = np.concatenate((label_0, label_1), axis=0)
print('shape of point_class_0 : ', point_class_0.shape)
print('shape of point_class_1 : ', point_class_1.shape)
print('shape of label_0 : ', label_0.shape)
print('shape of label_1 : ', label_1.shape)
print('shape of point : ', point.shape)
print('shape of label : ', label.shape)
shape of point_class_0: (300, 3)
shape of point_class_1: (300, 3)
shape of label_0: (300,)
shape of label_1: (300,)
shape of point : (600, 3)
shape of label: (600,)
```

run the gradient descent algorithm to optimize the loss function with respect to the model parameter

functions for presenting the results

```
In []: def function_result_01():
    input1 = np.array([0.1, 0.2, 0.3])
    input2 = np.array([[1, 2, 3], [1, -2, -3]])
    value = compute_linear_regression(input1, input2)
    print(value)
```

In []: | def function_result_02():

```
input1 = np.array([0.1, 0.2, 0.3])
             input2 = np.array([[1, 2, 3], [1, -2, -3]])
             value = compute_logistic_regression(input1, input2)
             print(value)
In [ ]:
         def function_result_03():
             input1 = np.array([0.1, 0.2, 0.3])
             input2 = np.array([[1, 2, 3], [1, -2, -3]])
             input3 = np.array([0, 1])
             value = compute_residual(input1, input2, input3)
             print(value)
In [ ]:
         def function_result_04():
             input1 = np.array([0.1, 0.2, 0.3])
             input2 = np.array([[1, 2, 3], [1, -2, -3]])
             input 3 = \text{np.array}([[0], [1]])
             value = compute_loss(input1, input2, input3)
             print(value)
In [ ]:
         def function_result_05():
             input1 = np.array([0.1, 0.2, 0.3])
             input2 = np.array([[1, 2, 3], [1, -2, -3]])
             input3 = np.array([[0], [1]])
             value = compute_gradient(input1, input2, input3)
             print(value)
In [ ]:
         def function_result_06():
             plt.figure(figsize=(8,6))
             plt.title('loss')
             plt.plot(loss_iteration, '-', color='red')
             plt.xlabel('iteration')
             plt.ylabel('loss')
             plt.tight_layout()
             plt.show()
In [ ]:
         def function_result_07():
             plt.figure(figsize=(8,6)) # USE THIS VALUE for the size of the figure
             plt.title('model parameter')
             plt.plot(theta_iteration[:, 0], '-', color='red', label=r'$\text{Wtheta_0$'}
```

```
plt.plot(theta_iteration[:, 1], '-', color='green', label=r'$\text{Wtheta_1$}')
plt.plot(theta_iteration[:, 2], '-', color='blue', label=r'$\text{Wtheta_2$}')

plt.xlabel('iteration')
plt.legend()

plt.tight_layout()
plt.show()
```

plot the linear regression values over the 2dimensional Euclidean space and superimpose the training data

```
In [ ]:
        def function_result_08():
           X = np.arange(-20, 35, 0.1) # USE THIS VALUE for the range of x values in the con
           Y = np.arange(-20, 35, 0.1) # USE THIS VALUE for the range of y values in the con-
            [XX, YY] = np.meshgrid(X, Y)
            # complete the blanks
           xravel = XX.ravel(); yravel = YY.ravel()
           F = compute_linear_regression(theta_optimal, (np.array([np.ones(xravel.size), xra
           FF = F.reshape(XX.shape)
           plt.figure(figsize=(8,8))
           plt.title('linear regression values')
           cntrf = plt.contourf(XX, YY, FF, cmap=plt.get_cmap('RdBu_r'), levels = 90)
           plt.colorbar(cntrf)
           plt.plot(point_x_class_0, point_y_class_0, '.', color='blue', label='class 0')
           plt.plot(point_x_class_1, point_y_class_1, '.', color='red', label='class 1')
           plt.contour(XX, YY, FF, levels=[0], colors = "black")
           plt.axis('equal')
           plt.legend()
           plt.tight_layout()
           plt.show()
```

plot the logistic regression values over the 2dimensional Euclidean space

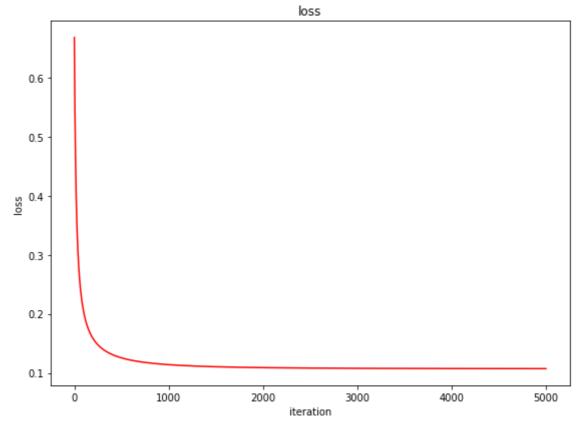
```
In [ ]: def function_result_09():
    X = np.arange(-20, 35, 0.1) # USE THIS VALUE for the range of x values in the construction
    Y = np.arange(-20, 35, 0.1) # USE THIS VALUE for the range of y values in the construction
    [XX, YY] = np.meshgrid(X, Y)
```

```
# complete the blanks
#
xravel = XX.ravel(); yravel = YY.ravel()
F = compute_logistic_regression(theta_optimal, (np.array([np.ones(xravel.size), x
FF = F.reshape(XX.shape)
plt.figure(figsize=(8,8))
plt.title('logistic regression values')
cntrf = plt.contourf(XX, YY, FF, cmap=plt.get_cmap('RdBu_r'), levels = 100)
plt.colorbar(cntrf)
plt.plot(point_x_class_0, point_y_class_0, '.', color='blue', label='class 0')
plt.plot(point_x_class_1, point_y_class_1, '.', color='red', label='class 1')
# plt.contour(XX, YY, FF, levels=[0], colors = "black")
plt.axis('equal')
plt.legend()
plt.tight_layout()
plt.show()
```

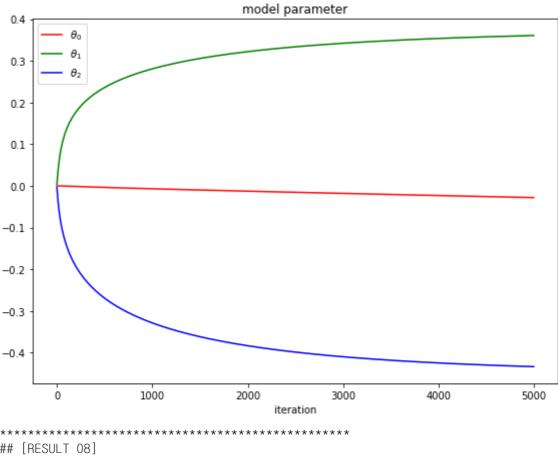
results

```
In [ ]:
     number_result = 9
     for i in range(number_result):
       title = '## [RESULT {:02d}]'.format(i+1)
       name_function = 'function_result_{:02d}()'.format(i+1)
       print(title)
       eval(name_function)
    ***********
    ## [RESULT 01]
    [1.4 - 1.2]
    ***********
    ## [RESULT 02]
    ***********
    [0.80218389 0.23147522]
    ## [RESULT 03]
    **************
    [1.62041741 1.46328247]
    ***********
    ## [RESULT 04]
```





[RESULT 07]



[RESULT 08]

