Linear Regression

import library

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
import matplotlib.colors as colors
from mpl_toolkits.mplot3d import Axes3D
```

load point data for training and testing

```
In []:
    filename_data = 'assignment_07_data.csv'

    data = np.genfromtxt(filename_data, delimiter=',')
    number_data = data.shape[0]

    x = data[:, 0]
    y = data[:, 1]
    z = data[:, 2]

    print('number of data = ', number_data)
    print('data type of x = ', x.dtype)
    print('data type of y = ', y.dtype)
    print('data type of z = ', z.dtype)

number of data = 2500
    data type of x = float64
    data type of z = float64
    data type of z = float64
```

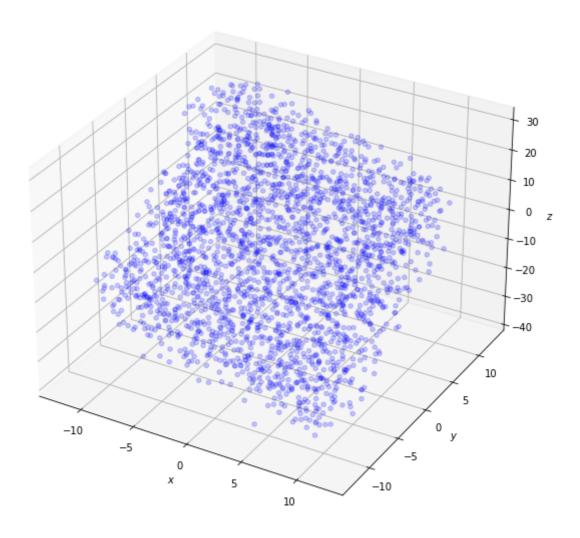
plot the data in the three dimensional space

```
In [ ]:
    fig = plt.figure(figsize=(12, 8))
    ax1 = plt.subplot(111, projection='3d')

ax1.set_xlabel('$x$')
    ax1.set_ylabel('$y$')
    ax1.set_zlabel('$z$')
    ax1.scatter(x, y, z, marker='o', color='blue', alpha=0.2)

plt.title('data points')
    plt.tight_layout()
    plt.show()
```

data points



compute the prediction function

- $\theta = (\theta_0, \theta_1, \theta_2) \in \mathbb{R}^3$
- $x,y \in \mathbb{R}$

compute the loss function

- $\bullet \ \ \theta = (\theta_0, \theta_1, \theta_2) \in \mathbb{R}^3$
- $ullet \ x,y,z\in \mathbb{R}$

```
In [ ]: def compute_residual(theta, x, y, z):
```

• useful functions: np.inner

compute the gradient for the model parameters heta

useful functions: np.matmul

gradient descent for the optimization

In []:

functions for presenting the results

def function_result_01():

```
plt.figure(figsize=(8,6))
            plt.title('loss')
            plt.plot(loss_iteration, '-', color='red')
            plt.xlabel('iteration')
            plt.ylabel('loss')
            plt.tight_layout()
            plt.show()
In [ ]:
        def function_result_02():
            plt.figure(figsize=(8,6))
            plt.title('model parameters')
            plt.plot(theta_iteration[:, 2], '-', color='blue', label=r'$\text{\text{\text{wtheta}}$_2$')
            plt.xlabel('iteration')
            plt.ylabel('model parameter')
            plt.legend()
            plt.tight_layout()
            plt.show()
```

```
In []:
    def function_result_03():
        xx = np.arange(-10, 10, 0.1)
        yy = np.arange(-10, 10, 0.1)

        (grid_x, grid_y) = np.meshgrid(xx,yy)
        zz = theta[0] + theta[1] * grid_x + theta[2] * grid_y

        fig = plt.figure(figsize=(8,8))
        ax = fig.add_subplot(111, projection='3d')
        plt.title('regression surface')

        ax = plt.axes(projection='3d')
```

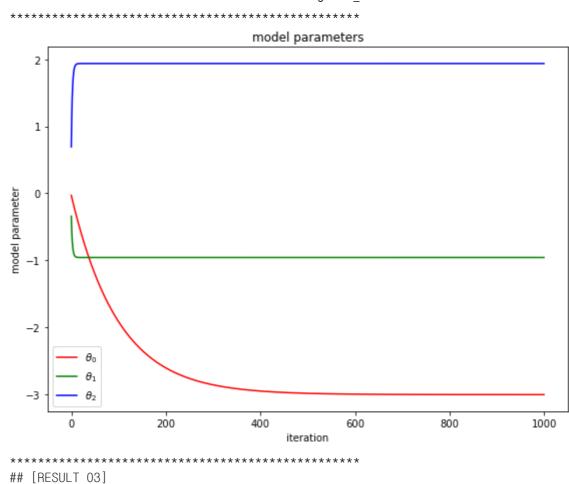
```
ax.set_xlabel(r'$x$')
ax.set_ylabel(r'$y$')
ax.set_zlabel(r'$z$')

ax.plot_surface(grid_x, grid_y, zz, rstride=1, cstride=1, cmap='viridis', edgecol
ax.scatter(x, y, z, marker='o', color='blue', alpha=0.5)

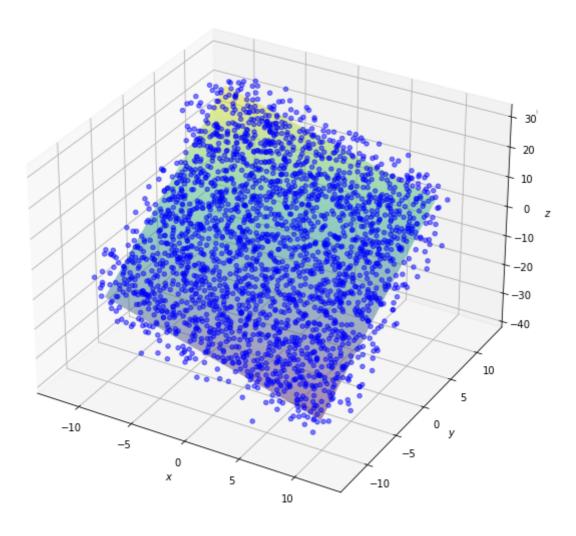
plt.tight_layout()
plt.show()
```

results

```
In [ ]:
       number_result = 3
       for i in range(number_result):
          title = '## [RESULT {:02d}]'.format(i+1)
          name_function = 'function_result_{:02d}()'.format(i+1)
          print(title)
          print('*********
          eval(name_function)
      ***********
      ## [RESULT 01]
                                      loss
        45
        40
        35
        30
      S 25
        20
        15
        10
                       200
                                 400
                                                      800
                                                                1000
                                           600
      ## [RESULT 02]
```



regression surface



In []:		