

# 1 NfOrder: Orders in in absolute number fields

## 1.1 Introduction

Assume that  $K$  is an algebraic number field of degree  $d$ . Classically, an order  $\mathcal{O}$  of  $K$  is a subring  $\mathcal{O} \subseteq K$ , which is a free  $\mathbf{Z}$ -module of rank  $d = \text{degree}(K)$ . For computational reasons, an  $\mathcal{O}$  is always given together with a matrix  $A$  (the *basis matrix*), such that the elements  $\omega_1, \dots, \omega_d$  defined by

$$\begin{pmatrix} \omega_1 \\ \omega_2 \\ \vdots \\ \omega_d \end{pmatrix} = A \cdot \begin{pmatrix} 1 \\ \alpha \\ \vdots \\ \alpha^d \end{pmatrix}$$

are a  $\mathbf{Z}$ -basis of  $\mathcal{O}$ .

In HECKE orders in number fields are modelled by objects of type `NfOrder`.

## 1.2 Creation of objects of type NfOrder

```
EquationOrder(K::NfNumberField) -> NfOrder
    arg1::Bool = true
    I am a paramter::Bool = false
```

Assume that  $K$  represents the number field  $\mathbf{Q}(\alpha)$ . This function will produce the equation order  $\mathbf{Z}[\alpha]$  of  $\alpha$ , that is, the order of  $K$  with basis matrix  $\mathbf{1}_d$ .

I'm an example

```
julia> Qx, x = PolynomialRing(QQ,"x");
julia> f = x^19 + x^2 + 3*x + 11;
julia> K, a = NumberField(f, "a");
julia> O = EquationOrder(K);
```

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```
Order(a) -> b
```

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```
Order(arg1) -> tar
    parp
```

ich bin eine funktion. Die beschreibung kann so lang sein wie sie will. blablabla. dasdasd-ksadkasdksadkasdka sadk sakdk askdas .

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## 1.3 Creation of elements

```
O(x::nf_elem) -> NfOrderEllem
    check::Bool = true
```

Given an order `O`, try to coerce the number field element `x` into `O`

I'm the example

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