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```

Comparisons and Ordering

```
(==)
            {a}
                    (Cmp a) \Rightarrow a \rightarrow a \rightarrow Bit
(!=)
            {a}
                    (Cmp a) => a -> a -> Bit
       : \{a,b\} (Cmp b) => (a \rightarrow b) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow Bit
            \{a,b\}\ (Cmp\ b) \Rightarrow (a \rightarrow b) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow Bit
(!==)
(<)
            \{a\}\ (Cmp\ a) => a -> a -> Bit
            \{a\}\ (Cmp\ a) => a -> a -> Bit
(<=)
            {a} (Cmp a) => a -> a -> Bit
(>=)
        : {a} (Cmp a) => a -> a -> Bit
min
         : {a} (Cmp a) => a -> a -> a
max
           {a} (Cmp a) => a -> a -> a
instance Cmp Bit
// No instance for functions.
instance (Cmp a, fin n) => Cmp [n]a
instance (Cmp a, Cmp b) => Cmp (a,b)
instance (Cmp a, Cmp b) => Cmp { x : a, y : b }
```

Signed Comparisons

```
(<$): {a} (SignedCmp a) => a -> a -> Bit
(>$): {a} (SignedCmp a) => a -> a -> Bit
(<=$): {a} (SignedCmp a) => a -> a -> Bit
(>=$): {a} (SignedCmp a) => a -> a -> Bit
(>=$): {a} (SignedCmp a) => a -> a -> Bit
// No instance for Bit
// No instance for functions.
instance (fin n, n >= 1) => SignedCmp [n]
instance (SignedCmp a, fin n) => SignedCmp [n]a
// (for [n]a, where a is other than Bit)
```

```
instance (SignedCmp a, SignedCmp b) => SignedCmp (a,b)
instance (SignedCmp a, SignedCmp b) => SignedCmp { x : a, y : b }
```

Arithmetic

```
(+)
      : {a} (Arith a) => a -> a -> a
(-)
      : {a} (Arith a) => a -> a -> a
(*)
     : {a} (Arith a) => a -> a -> a
(/)
      : {a} (Arith a) => a -> a -> a
(%)
     : {a} (Arith a) => a -> a -> a
     : {a} (Arith a) => a -> a -> a
     : {a} (Arith a) => a -> a -> a
(/\$)
(%$)
     : {a} (Arith a) => a -> a -> a
// No instance for `Bit`.
instance (fin n)
                          => Arith ([n] Bit)
instance (Arith a)
                          => Arith ( [n] a)
                    => Arith (a -> b)
instance (Arith b)
instance (Arith a, Arith b) => Arith (a,b)
instance (Arith a, Arith b) => Arith { x : a, y : b }
```

Note that because there is no instances for Arith Bit the top two instances do not actually overlap.

Boolean

```
False : Bit
True : Bit

zero : a
(&&) : a -> a -> a
(||) : a -> a -> a
(^) : a -> a -> a
(^) : a -> a
(^) : a -> a
(^) : Bit -> Bit -> Bit
(/\) : Bit -> Bit -> Bit
(\/) : Bit -> Bit -> Bit
```

Sequences

```
length : \{n,a,m\} (m \ge width n) = [n]a - [m]
```

```
: {parts,ench,a} (fin each) => [parts][each]a -> [parts * each]a
join
            : {parts,each,a} (fin each) => [parts * each]a -> [parts][each]a
split
            : {front,back,a} (fin front) => [front]a -> [back]a -> [front + back]a
(#)
splitAt
            : {front,back,a} (fin front) => [from + back] a -> ([front] a, [back] a)
            : \{n,a\} (fin n) \Rightarrow [n]a \rightarrow [n]a
reverse
transpose : \{n,m,a\} [n] [m] a \rightarrow [m] [n] a
(0)
             : \{n,a,m\}
                                        [n]a -> [m]
(00)
             : \{n,a,m,i\}
                                        [n]a \rightarrow [m][i] \rightarrow [m]a
             : \{n,a,m\} (fin n) => [n]a \rightarrow [m]
(!)
                                                          -> a
             : {n,a,m,i} (fin n) => [n]a \rightarrow [m][i] \rightarrow [m]a
(!!)
             : \{n,a,m\} (fin m) \Rightarrow [n]a \rightarrow [m] \rightarrow a \rightarrow [n]a
update
updateEnd : \{n,a,m\} (fin n, fin m) => [n]a \rightarrow [m] \rightarrow a \rightarrow [n]a
             : \{n,a,m,d\} (fin m, fin d) => [n]a \rightarrow [d][m] \rightarrow [d]a \rightarrow [n]a
updatesEnd : \{n,a,m,d\} (fin n, fin m, fin d) => [n]a -> [d][m] -> [d]a -> [n]a
// Abbreviations
groupBy n = split`{each = n}
tail n
           = splitAt`{front = 1}.1
take n
           = splitAt`{front = n}.0
           = splitAt`{front = n}.1
drop n
/* Also, `length` is not really needed:
   length: \{n,a,m\} (m \ge width n) = [n]a - [m]
   length _ = `n
```

Shift And Rotate

New types:

```
(<<) : {n,a,m} (fin n) => [n]a -> [m] -> [n]a
(>>) : {n,a,m} (fin n) => [n]a -> [m] -> [n]a
(<<<) : {n,a,m} (fin n) => [n]a -> [m] -> [n]a
(>>>) : {n,a,m} (fin n) => [n]a -> [m] -> [n]a
// Arithmetic shift only for bitvectors
(>>$) : {n, k} (fin n, n >= 1, fin k) => [n] -> [k] -> [n]
```

Random Values

```
random : {a} => [256] -> a
```

Debugging

undefined : {a} a

error : {n a} [n][8] -> a

trace : $\{n, a, b\}$ (fin n) => [n][8] -> a -> b -> b

traceVal : $\{n, a\}$ (fin n) => [n][8] -> a -> a