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```

### Comparisons and Ordering

```
(==)
           {a}
                   (Cmp a) \Rightarrow a \rightarrow a \rightarrow Bit
(!=)
           {a}
                   (Cmp a) \Rightarrow a \rightarrow a \rightarrow Bit
(===) : {a,b} (Cmp b) => (a -> b) -> (a -> b) -> a -> Bit
       : \{a,b\} (Cmp b) => (a \rightarrow b) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow Bit
(<)
           \{a\}\ (Cmp\ a) => a -> a -> Bit
(>)
        : {a} (Cmp a) => a -> a -> Bit
(<=)
       : {a} (Cmp a) => a -> a -> Bit
(>=)
           {a} (Cmp a) => a -> a -> Bit
        : {a} (Cmp a) => a -> a -> a
min
max
        : {a} (Cmp a) => a -> a -> a
instance Cmp Bit
// No instance for functions.
instance (Cmp a, fin n) => Cmp [n] a
instance (Cmp a, Cmp b) => Cmp (a,b)
instance (Cmp a, Cmp b) => Cmp { x : a, y : b }
```

#### Arithmetic

```
: {a} (Arith a) => a -> a -> a
(+)
(-)
       : {a} (Arith a) => a -> a -> a
(*)
       : {a} (Arith a) => a -> a -> a
(/)
       : {a} (Arith a) => a -> a -> a
(%)
       : {a} (Arith a) => a -> a -> a
       : {a} (Arith a) => a -> a -> a
// No instance for `Bit`.
instance (fin n)
                            => Arith ([n] Bit)
instance (Arith a)
                            => Arith ( [n] a)
instance (Arith b)
                            => Arith (a -> b)
```

```
instance (Arith a, Arith b) => Arith (a,b)
instance (Arith a, Arith b) => Arith { x : a, y : b }
```

Note that because there is no instances for Arith Bit the top two instances do not actually overlap.

#### Boolean

```
False : Bit
True : Bit

zero : a
(&&) : a -> a -> a
(||) : a -> a -> a
(^) : a -> a
(^) : a -> a
```

#### Sequences

```
: \{n,a,m\} (m \ge width n) = [n]a - [m]
length
           : {parts,ench,a} (fin each) => [parts][each]a -> [parts * each]a
join
            : {parts,each,a} (fin each) => [parts * each]a -> [parts][each]a
split
           : \{front,back,a\}\ (fin\ front) \Rightarrow [front]a \rightarrow [back]a \rightarrow [front + back]a
(#)
           : {front,back,a} (fin front) => [from + back] a -> ([front] a, [back] a)
splitAt
           : \{n,a\} (fin n) \Rightarrow [n]a \rightarrow [n]a
transpose : \{n,m,a\} [n] [m] a \rightarrow [m] [n] a
(0)
             : {n a m}
                                        [n]a -> [m]
(00)
             : {n a m i}
                                        [n]a \rightarrow [m][i] \rightarrow [m]a
(!)
             : \{n a m\}
                         (fin n) \Rightarrow [n]a \rightarrow [m]
                                                         -> a
             : {n a m i} (fin n) \Rightarrow [n]a \rightarrow [m][i] \rightarrow [m]a
(!!)
// Abbreviations
groupBy n = split`{each = n}
           = splitAt`{front = 1}.1
tail n
           = splitAt`{front = n}.0
take n
           = splitAt`{front = n}.1
drop n
/* Also, `length` is not really needed:
   length : \{n,a,m\} (m \ge width n) = [n]a - [m]
```

```
length _ = `n
*/
```

### Shift And Rotate

New types:

# Random Values

```
random : {a} => [256] -> a
```

# Debugging

undefined : {a} a

error : {n a} [n][8] -> a