

Write the **negation** of each statement below. Simplify as much as is reasonable. That is, don't just write "it is false that..." followed by the statement.

1.  $\forall x \exists y \exists z (y \neq z \wedge x = y + z)$

2.  $\exists x \forall y (x < y \rightarrow x + 1 < y)$

3. There are integers  $x$  and  $y$  such that  $x^2 = 4y + 2$

4. For all integers  $a$  and  $b$ , if  $a \cdot b$  is odd, then  $a$  or  $b$  is odd.

5. For every integer  $x$  there is an integer  $y$  such that  $x < y$  and  $x^2 \geq y^2$ .

6. For every function  $f$  and every closed interval  $[a, b]$ , if  $f$  is continuous on  $[a, b]$  then there is a number  $c$  in the interval  $[a, b]$  such that  $f(c) \geq f(x)$  for all  $x$  in the interval.