Depth Equations in Dolphin

1 Gamecube (SlowDepth)

$$(far - near) * \frac{z}{w} + far \tag{1}$$

2 Direct3D FastDepth

Depth equation:

$$(far - near) * \frac{z}{w} + near \tag{2}$$

Solution:

$$(far - near) * (\frac{z+w}{w}) + near \tag{3}$$

$$(far - near) * (\frac{z}{w} + \frac{w}{w}) + near \tag{4}$$

$$(far - near) * (\frac{z}{w} + 1) + near \tag{5}$$

$$(far - near) * \frac{z}{w} + (far - near) + near$$
 (6)

$$(far - near) * \frac{z}{w} + far \tag{7}$$

(z + w introduces rounding errors)

3 OpenGL FastDepth

Depth equation:

$$\frac{far - near}{2} * \frac{z}{w} + \frac{near + far}{2} \tag{8}$$

Solution:

$$\frac{far - near}{2} * \left(\frac{2 * z + w}{w}\right) + \frac{near + far}{2} \tag{9}$$

$$\frac{far - near}{2} * \left(2 * \frac{z}{w} + \frac{w}{w}\right) + \frac{near + far}{2} \tag{10}$$

$$\frac{far - near}{2} * (2 * \frac{z}{w} + 1) + \frac{near + far}{2}$$
 (11)

$$(far - near) * \frac{z}{w} + \frac{far - near}{2} + \frac{near + far}{2}$$
 (12)

$$(far - near) * \frac{z}{w} + \frac{far - near + near + far}{2}$$
 (13)

$$(far - near) * \frac{z}{w} + \frac{far + far}{2}$$
 (14)

$$(far - near) * \frac{z}{w} + far \tag{15}$$

(2*z+w introduces rounding errors)

4 OpenGL FastDepth (Clip Control)

Depth equation:

$$(far - near) * \frac{z}{w} + near$$
 (16)

Solution:

$$(near - far) * \frac{-z}{w} + far \tag{17}$$

$$(far - near) * \frac{z}{w} + far \tag{18}$$

(OpenGL allows far < near, no rounding errors)

5 Direct3D FastDepth (Depth Inversion)

Designed by Galop1n

Depth equation:

$$(far - near) * \frac{z}{w} + near \tag{19}$$

Solution:

$$((1 - near) - (1 - far)) * \frac{-z}{w} + (1 - far)$$
 (20)

$$((1-1) + (far - near)) * \frac{-z}{w} + (1 - far)$$
 (21)

$$(far - near) * \frac{-z}{w} + (1 - far) \tag{22}$$

Depth inversion:

$$1 - ((far - near) * \frac{-z}{w} + (1 - far))$$
 (23)

$$1 + (far - near) * \frac{z}{w} - 1 + far \tag{24}$$

$$(far - near) * \frac{z}{w} + far \tag{25}$$

(Direct3D doesn't allow far < near, no rounding errors)