TxForest: Composable Memory Transactions over Filestores

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Abstract

Keywords

1. Introduction

Databases are a long-standing, effective technology for storing structured and semi-structured data. Using a database has many benefits, including transactions and access to rich set of data manipulation languages and toolkits.

downsides: heavy legacy, relational model is not always adequate cheaper and simpler alternative: store data directly as a collection of files, directories and symbolic links in a traditional filesystem. examples of filesystems as databases

filesystems fall short for a number of reasons

Forest [1] made a solid step into solving this, by offering an integrated programming environment for specifying and managing filestores

Although promising, the old Forest suffered two essential short-comings:

- It did not offer the level of transparency of a typical DBMS.
 Users don't get to believe that they are working directly on the
 database (filesystem), they explicitly issue load/store calls, and
 instead manipulate in-memory representations and the filesystem
 independently, offline synchronization.
- It provided none of the transactional guarantees familiar from databases. transactions are nice: prevent concurrency and failure problems. successful transactions are guaranteed to run in serial order and failing transactions rollback as if they never occurred. rely on extra programmers' to avoid the hazards of concurrent updates. different hacks and tricks like creating lock files and storing data in temporary locations, that severely increase the complexity of the applications. writing concurrent programs is notoriously hard to get right. even more in the presence of laziness (original forest used the generally unsound Haskell lazy I/O)

transactional filesystem use cases:

a directory has a group of files that must be processed and deleted and having the aggregate result written to another file.

software upgrade (rollback),

concurrent file access (beautiful account example?)

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```
 [pads \mid \mathbf{data} \; Balance = Balance \; Int \mid ] \\ [forest \mid \\ \mathbf{type} \; Accounts = [a :: Account \mid a \leftarrow matches \; (GL "*")] \\ \mathbf{type} \; Account = \mathtt{File} \; Balance \\ \mid ]
```

Specific use cases: LHC Network logs Dan's scientific data

2. Examples

3. The Forest Language

the forest description types

a forest description defines a structured representation of a semi-structured filestore.

each Forest declaraction is interpreted as: an expected on-disk shape of a filesystem fragment a transactional variable an ordinary Haskell type for the in-memory representation that represents the content of a variable

two expression quotations: non-monadic (e) vs monadic $\langle |e| \rangle$

4. Forest Transactions

The Forest description language introduced in the previous section describes how to specify the expected shape of a filestore as an allegorical Haskell type, independently from the concrete programming artifacts that are used to manipulate such filestores. We now focus on the key goal of this paper: the design of the Transactional Forest interface.

As we shall see, TxForest (for short) offers an elegant and powerful abstraction to concurrently manipulate structured filestores. We first describe general-purpose transactional facilities (4.1). We then introduce transactional forest variables that allow programmers to interact with filestores (4.2). We briefly touch on how programmers can verify, at any time, if a filestore conforms to its specification (4.3), and finish by introducing analogous of standard file system operations over filestores (4.4).

4.1 Composable transactions

As an embedded domain-specific language in Haskell, the inspiration for TxForest is the widely popular *software transactional memory* (STM) Haskell library, that provides a small set of highly composable operations to define the key facilities of a transaction. We now explain the intuition of each one of these mechanisms, cast in the context of TxForest.

Running transactions In TxForest, one runs a transaction by calling an *atomic* function with type:¹

```
atomic :: FTM \ a \rightarrow IO \ a
```

It receives a forest memory transaction, of type $FTM\ a$, and produces an $IO\ a$ action that executes the transaction atomically with respect to all other concurrent transactions, returning a result of type a. In the pure functional language Haskell, FTM and IO are called monads. Different monads are typically used to characterize different classes of computational effects. IO is the primitive Haskell monad for performing irrevocable I/O actions, including reading/writing to files or to mutable references, managing threads, etc. For example, the Haskell prelude functions:

```
getChar :: IO Char

putChar :: Char \rightarrow IO ()
```

respectively read a character from the standard input and write a single character to the standard output.

Conversely, our FTM monad denotes computations that are tentative, in the sense that they happen inside the scope of a transaction and can always be rolled back. As we shall in the remainder of this section, these consist of STM-like transactional combinators, file system operations on Forest filestores, or arbitrary pure functions. Note that, being FTM and IO different types, the Haskell type system effectively prevents non-transactional actions to be run inside a transaction. This is a valuable guarantee, and one that is not commonly found in transactional libraries for mainstream programming languages without a very expressive type system.

Blocking transactions To allow a transaction to *block* on a resource, TxForest provides a single *retry* operation with type:

```
retry :: FTM \ a
```

Conceptually, retry cancels the current transaction, without emitting any errors, and schedules it to be retried at a later time. Since each transaction logs all the reads/writes that it performs on a filestore, an efficient implementation waits for another transaction to update the shared filestore fragments read by the blocked transaction before retrying.

Using *retry* we can define a pattern for conditional transactions that wait on a condition to be verified before performing an action:

```
wait :: FTM \ Bool \rightarrow FTM \ a \rightarrow FTM \ a
wait b \ c \ a = \mathbf{do} \ \{ b \leftarrow p; \mathbf{if} \ b \ \mathbf{then} \ retry \ \mathbf{else} \ a \}
```

All of the reads in a transaction are logged and when retry is called, it blocks until another transaction writes to a file from the read log before restarting the transaction from scratch.

Composing transactions Multiple transactions can be sequentially composed via the standard **do** notation. For example, we can write:

```
do \{x \leftarrow ftm1; fmt2 \ x\}
```

to run a transaction ftm1:FTM a and pass its result to a transaction $ftm2::a \rightarrow FTM$ b. Since the whole computation is itself a transaction, it will be performed indivisibly inside an atomic block.

We can also compose transactions as alternatives, using the orElse primitive:

```
orElse :: FTM \ a \rightarrow FTM \ a \rightarrow FTM \ a
```

This combinator performs a left-biased choice: if first runs transaction ftm1, tries fmt2 if ftm1 retries, and the whole action retries if ftm2 retries. It can be useful, for example, to read either one of two files depending on the current configuration of the file system.

Note that or Else provides an elegant mechanism to define nested transactions. At any point inside a larger transaction, we can tentatively perform a transaction ftm1, and rollback to the beginning (of the nested transaction) to try an alternative ftm2 in case fmt1 retries:

```
do \{...; or Else ftm1 ftm2; ...\}
```

Exceptions The last general-purpose feature of FTM transactions are *exceptions*. In Haskell, both built-in and user-defined exceptions are used to signal error conditions. We can *throw* and *catch* exceptions in the FTM monad in the same way as the IO monad:

```
throw:: Exception e \Rightarrow e \rightarrow FTM a catch:: Exception e \Rightarrow FTM a \rightarrow (e \rightarrow FTM a) \rightarrow FTM a
```

For instance, a TxForest user may define a new FileNotFound exception and write the following pseudo-code:

```
tryRead = \mathbf{do}

\{exists \leftarrow ...find \ file ...

\mathbf{;if} \ (not \ exists) \ \mathbf{then} \ throw \ FileNotFound \ \mathbf{else} \ return \ ()

\mathbf{;...} read \ file...
```

If the file in question is not found, then a *FileNotFound* exception is thrown, aborting the current *atomic* block (and hence the file is never read). Programmers can prevent the transaction from being aborted, and its effects discarded, by catching exceptions inside the transaction, e.g.:

```
catch \ tryRead \ (\lambda FileNotFound \rightarrow return ... \ default...) \ tryRead
```

4.2 Transactional variables

We have seen how to build transactions from smaller transactional blocks, but we still haven't seen concrete operations to manipulate *shared data*, a fundamental piece of any transactional mechanism. In vanilla Haskell STM, communication between threads is done via shared mutable memory cells called *transactional variables*. For a transaction to log all memory effects, transactional variables can only be explicitly created, read from or written to using specific transactional operations. Nevertheless, programmers are welcome to perform many arbitrary pure functional computations to manipulate their content; since these don't have side-effects, they don't ever need to be logged or rolled back.

In the context of TxForest, shared data is not stored in-memory but on the filestore. It is illuminating to quote [2]:

"We study internal concurrency between threads interacting through memory [...]; we do not consider here the questions of external interaction through storage systems or databases."

We consider precisely the question of external interaction with a file system. Two transactions may communicate, e.g., by reading from or writing to the same file or possibly a list of files within a directory. To facilitate this interaction, the TxForest compiler generates an instance of the TxForest type class (and corresponding types) for each Forest declaration:

```
class TxForest\ args\ ty\ rep\ |\ ty \to rep\ , ty \to args\ where new :: args \to FilePath \to FTM\ fs\ ty read :: ty \to FTM\ rep writeOrElse :: ty \to rep \to b \to (Manifest \to FTM\ fs\ b) \to FTM\ fs\ b
```

In this signature, ty is an opaque transactional variable type that uniquely identifies a user-declared Forest type. The representation type rep is a plain Haskell type that holds the content of a transactional variable.

The transactional forest programing style draws no distinction between data on the file system and in-memory. Anywhere inside a

¹ For the original STM interface, substitute FTM by STM [2].

transaction, users can declare a new transactional variable of type ty, with argument data pertaining to the forest declaration and rooted at the argument path in the file system. This operation does not have any effect on the file system, and just establishes the schema to which a filestore should conform.

Users can read the contents of a transactional variable to obtain an Haskell value of type rep. Consider reading the description in Figure ??:

```
do
  accs :: Accounts \leftarrow new () "/var/db/accounts"
  accs\_rep \leftarrow read \ accs
```

In the background, this is done by lazily traversing the directories, files and symbolic links mentioned in the forest description, stopping as soon as other transactional variables are encountered. The above snippet reads the accounts directory and generates a list of transactional variables, one per account. Developers can control the degree of laziness in a forest description by controlling the granularity of Forest declarations. For instance, if we have inlined each account in the description in Figure ??:

```
type Accounts = [a :: File Balance | a \leftarrow matches (GL "*")]
```

then read accs would also read the file content of each individual account inside the accounts directory.

Users can manipulate these structures as they would in regular Haskell programs, and eventually perform FS modifications by writing a new representation to a transactional variable. writes may fail if the provided data is not a faithful representation of the filestore for the specification under consideration.

WriteErrors have nothing to do with transactional errors and account for the inconsistencies that can arise when a programmer attempts to write an erroneous in-memory representation to the filestore. For example, attempting to write conflicting data to the same file or a text file to a specification of a directory structure.

The rep of a variable may contain other variables such as a directory containing a list of other Forest types.

Notice that we can have multiple variables (possibly with different specs) "connected" to the same fragment of a filesystem. This can cause WriteErrors, as noted above, and the values of the two will be interdependent. However, variables only depend on each other within a transaction, not across transactions (until a transaction is committed that is).

We have a sort of mismatch: Transactional variables for type declarations VS fileinfo for directories/files. Since forest always fills in default data for non-existing paths, the fileinfo actually determines whether a directory/file exists or not in the real FS. E.g. to delete a file we need to mark its fileinfo as invalid, and to create a file we need to define clean, valid fileinfo for it.

4.3 Validation

Validation helps programmers detect inconsistencies between the data they are trying to write to the filesystem and the constraints they have specified through Forest. In order to detect these sorts of errors, which we allow them to make should they care to, we provide a validate function, returning all such errors.

4.4 Standard filesystem operations

not a problem of expressiveness, for convenience

```
rm :: TxForest \ args \ ty \ rep \Rightarrow ty \rightarrow FTM \ ()
```

This command lets the programmer remove a filepath by writing invalid fileinfo and default data to it. In order to avoid a loss of information, the default data needs to be precisely the data that is generated by forest. If we are removing a directory, we need to make sure that its content is the empty list; a non-existing directory with content inside is not a valid snapshot of a FS, but a valid haskell value nonetheless. This is cumbersome to do manually for arbitrary specs that touch multiple files/directories, which is why we provide this primitive operation that generates the appropriate default data and performs the removal.

This command lets the programmer copy a forest specification. While copying a single file by hand is simple (read, copy the contents, update the fileinfo, write), copying a directory is significantly more cumbersome because we have to recursively copy each child variable and update its fileinfo accordingly. Therefore, we provide this primitive operation. It may fail because the data that we are trying to write may not be consistent with the specification for the target arguments and path. For example, a specification with a boolean argument that loads file x or y, with source argument True and target argument False.

Implementation

5.1 Transactional Forest

(this is important since we write to canonical paths, whose canonicalization may depend on concurrent writes...)

lock-free lazy acquire acquire ownership. only one tx can acquire an object at a time. global total order on variables, acquire variables in sorted order the analogous in txforest would be per-filepath locks, what does nto work out-of-the-box in the presence of symbolic links

the identity of a filepath is not unique (different paths point to the same physical address) nor stable (equivalence depends on on the current filesystem).

transactional semantics of STM: we log reads/writes to the filesystem instead of variables. global lock, no equality check on validation. load/store semantics of Forest with thunks, explicit laziness

transactional variables created by calling load on its spec with given arguments and root path; lazy loading, so no actual reads occur. Additionally to the representation data, each transactional variable remembers its creation-time arguments (they never change).

each transaction keeps a local filesystem version number, and a per-tvar log mapping fsversions to values, stored in a weaktable (fsversions are purgeable once a tx commits).

on writes: backup the current fslog, increment the fsversion, add an entry to the table for the (newfsversion,newvalue), run the store function for the new data and writing the modifications to the buffered FS; if there are errors, rollback to the backed-up FS and the previous fsversion.

the store function also changes the in-memory representation by recomputing the validation thunks (hidden to users) to match the new content.

write success theorem: if the current rep is in the image of load, then store succeeds

5.2 Incremental Transactional Forest

 $validate :: TxForest \ args \ ty \ rep \Rightarrow ty
ightarrow FTM \ ValidationErrors_{f problem}$ with 1st approach: ic loading: two variables over the same file; read spec1, write spec2, read spec1 (our simple cache mechanism fails to prevent recomputation) laziness problem with 1st approach: ic storing: read variable (child variables are lazy), write variable (will recursively store everything); instead of no-op! exploit DSL information to have incrementality

5.3 Log-structured Transactional Forest

problem with 2nd approach: tx1 reads a variable; tx2 reads the same variable

exploit (DSL info +) FS support to have incrementality read-only transactions require no synchronization

6. Evaluation

7. Related Work

transactional filesystems (user-space vs kernel-space) http://www. fuzzy.cz/en/articles/transactional-file-systems http://www.fsl.cs.sunysb.edu/docs/valor/valor_fast2009. pdf http://www.fsl.cs.sunysb.edu/docs/amino-tos06/amino.

pdf
libraries for transactional file operations: http://commons.

libraries for transactional file operations: http://commons.apache.org/proper/commons-transaction/file/index.html https://xadisk.java.net/

https://transactionalfilemgr.codeplex.com/

tx file-level operations (copy,create,delete,move,write) schema somehow equivalent to using the unstructured universal Forest representation

but what about data manipulation: transactional maps,etc?

8. Conclusions

transactional variables do not descend to the content of files. pads specs are read/written in bulk. e.g., append line to log file. extend pads.

References

- [1] K. Fisher, N. Foster, D. Walker, and K. Q. Zhu. Forest: A language and toolkit for programming with filestores. In *Proceedings of the 16th ACM SIGPLAN International Conference on Functional Programming*, ICFP '11, pages 292–306. ACM, 2011.
- [2] T. Harris, S. Marlow, S. Peyton-Jones, and M. Herlihy. Composable memory transactions. In *Proceedings of the Tenth ACM SIGPLAN Symposium on Principles and Practice of Parallel Programming*, PPoPP '05, pages 48–60, New York, NY, USA, 2005. ACM. ISBN 1-59593-080-9. URL http://doi.acm.org/10.1145/1065944.1065952.

Forest Semantics

$$F^*(r \, / \, u) = \left\{ \begin{array}{ll} F^*(r') & \text{if } F(F^*(r) \, / \, u) = (i, \text{Link } r') \\ F^*(\cdot) = \cdot & \text{otherwise} \end{array} \right.$$

$$r \in r'$$

$$\frac{1}{r \in \cdot} \quad \frac{r \in r'}{r / u \in r'}$$

$$F \searrow r \triangleq F|_{\{\forall r'. F^*(r') \in r\}}$$

$$F = F' = \forall r \in rs. F \searrow r = F' \searrow r$$

$$Err\ a = (M\ Bool, a)$$

s	$ \mathcal{R}[s] $	$\mathcal{C}[\![s]\!]$
Ms	$M\left(Err\left(\mathcal{R}[\![s]\!]\right)\right)$	$M\left(Err\left(\mathcal{R}\llbracket s\rrbracket\right)\right)$
$k_{ au_1}^{ au_2}$	$Err(au_2, au_1)$	(au_2, au_1)
e :: s	$ \mathcal{R}[s] $	$\mathcal{C}[s]$
$\langle x:s_1,s_2\rangle$	$Err\left(\mathcal{R}[s_1],\mathcal{R}[s_2]\right)$	$(\mathcal{C}[s_1],\mathcal{C}[s_2])$
$\{s \mid x \in e\}$	$Err \left[\mathcal{R} \llbracket s \rrbracket \right]$	$\left[C \llbracket s \rrbracket \right]$
P(e)	Err ()	()
s?	$Err\ (Maybe\ (\mathcal{R}[\![s]\!]))$	Maybe (C[s])

 $\mathcal{R}[\![\cdot]\!]$ is the internal in-memory representation type of a forest declaration; $\mathcal{C}[\![\cdot]\!]$ is the external type of content of a variables that users can inspect/modify

$$\begin{array}{l} err(a) = \text{do} \; \{ e \leftarrow \text{get} \; a; (a_{err}, v) \leftarrow e; \text{return} \; a_{err} \} \\ err(a_{err}, v) = \text{return} \; a_{err} \\ valid(v) = \text{do} \; \{ a_{err} \leftarrow err \; v; e_{err} \leftarrow \text{get} \; a_{err}; e_{err} \} \end{array}$$

 $v_1 \in \mathcal{O}_2$ v₂ denotes value equivalence modulo memory addresses, under the given environments. $e_1 \in \mathcal{O}_2$ e₂ denotes expression equivalence by evaluation modulo memory addresses, under the given environments.

 $v_1 \ominus_1 \circ \ominus_2 v_2$ denotes value equivalence (ignoring error information) modulo memory addresses, under the given environments.

 Θ ; ε ; r; $s \vdash \text{load } F \Rightarrow \Theta'$; v "Under heap Θ and environment ε , load the specification s for filesystem F at path r and yield a representation v.

$$s = M s_1$$

$$\begin{aligned} a \notin \mathsf{dom}(\Theta) & \quad a_{err} \notin \mathsf{dom}(\Theta) & \quad e = \varepsilon; r; \mathsf{M}\, s \vdash \mathsf{load}\, F \\ e_{err} &= \mathsf{do}\, \big\{\, e_1 \leftarrow \mathsf{get}\, \, a; v_1 \leftarrow e_1; valid\,\, v_1 \big\} \\ \Theta; \varepsilon; r; \mathsf{M}\, s \vdash \mathsf{load}\, F \Rightarrow \Theta[a_{err}: e_{err}, a: e]; (a_{err}, a) \end{aligned}$$

s = k

$$\frac{a_{err} \notin \mathsf{dom}(\Theta) \quad \Theta; \mathsf{load}_k(\varepsilon, F, r) \Rightarrow \Theta'; (b, v)}{\Theta; \varepsilon; r; k \vdash \mathsf{load} F \Rightarrow \Theta'[a_{err} : \mathsf{return} \ b]; (a_{err}, v)}$$

$$\begin{aligned} & \mathsf{load_{File}}(\varepsilon, F, r) \left\{ \begin{array}{ll} \mathsf{return} \; (\mathit{True}, (i, u)) & \text{if } F(r) = (i, \mathsf{File} \; u) \\ \mathsf{return} \; (\mathit{False}, (i_{\mathsf{invalid}}, \verb"")) & \text{otherwise} \end{array} \right. \\ & \mathsf{load_{Dir}}(\varepsilon, F, r) \left\{ \begin{array}{ll} \mathsf{return} \; (\mathit{True}, (i, us)) & \text{if } F(r) = (i, \mathsf{Dir} \; us) \\ \mathsf{return} \; (\mathit{False}, (i_{\mathsf{invalid}}, \{\,\})) & \text{otherwise} \end{array} \right. \end{aligned}$$

$$\texttt{load}_{\texttt{Dir}}(\varepsilon, F, r) \left\{ \begin{array}{ll} \texttt{return} \; (\mathit{True}, (i, us)) & \text{if } F(r) = (i, \texttt{Dir} \; us) \\ \texttt{return} \; (\mathit{False}, (i_{\texttt{invalid}}, \{\,\})) & \text{otherwise} \end{array} \right.$$

$$\texttt{load}_{\texttt{Link}}(\varepsilon, F, r) \left\{ \begin{array}{ll} \texttt{return} \; (\mathit{True}, (i, r')) & \quad \text{if } F(r) = (i, \texttt{Link} \; r') \\ \texttt{return} \; (\mathit{False}, (i_{\texttt{invalid}}, \cdot)) & \quad \text{otherwise} \end{array} \right.$$

 $s = e :: s_1$

$$\frac{\Theta; \llbracket r \mathrel{/} e \rrbracket_{Path}^{\varepsilon} \Rightarrow \Theta'; r' \quad \Theta; \varepsilon; r'; s \vdash \mathsf{load} \; F \Rightarrow \Theta''; v}{\Theta; \varepsilon; r; e :: s \vdash \mathsf{load} \; F \Rightarrow \Theta''; v}$$

$$s = \langle x : s_1, s_2 \rangle$$

$$\begin{array}{c} \Theta; \varepsilon; r; s_1 \vdash \mathsf{load} \ F \Rightarrow \Theta_1; v_1 \\ \Theta_1; \varepsilon[x \mapsto v_1]; r; s_2 \vdash \mathsf{load} \ F \Rightarrow \Theta_2; v_2 \\ e_{err} = \mathsf{do} \ \{b_1 \leftarrow valid(v_1); b_2 \leftarrow valid(v_2); \mathsf{return} \ (b_1 \land b_2)\} \\ \Theta; \varepsilon; r; \langle x: s_1, s_2 \rangle \vdash \mathsf{load} \ F \Rightarrow \Theta_2[a_{err}: e_{err}]; (a_{err}, (v_1, v_2)) \end{array}$$

```
s = \mathtt{P} \; e
                                                                                                                                              \frac{a_{err} \notin \mathsf{dom}(\Theta)}{\Theta; \varepsilon; r; \mathsf{P}\, e \vdash \mathsf{load}\, F \Rightarrow \Theta[a_{err} : \llbracket e \rrbracket_{Bool}^{\varepsilon}]; (a_{err}, ())}
               s = s_1?
                                                                                                                                                                                       r\notin \mathtt{dom}(F) \quad a_{err}\notin \mathtt{dom}(\Theta)
                                                                                                                         \Theta; \varepsilon; r; s? \vdash \text{load } F \Rightarrow \Theta[a_{err} : \text{return } True]; (a_{err}, Nothing)
                                                                                                                                \underline{r \in \mathsf{dom}(F) \quad a_{err} \notin \mathsf{dom}(\Theta') \quad \Theta; \varepsilon; r; s \vdash \mathsf{load} \ F \Rightarrow \Theta'; v
                                                                                                                                     \Theta; \varepsilon; r; s? \vdash load F \Rightarrow \Theta[a_{err} : valid(v)]; (a_{err}, Just \ v)
               s = \{s_1 \mid x \in e\}
                                                                                  \begin{array}{c} a_{err} \notin \operatorname{dom}(\Theta) \quad \Theta; \llbracket e \rrbracket_{\{\tau\}}^{\varepsilon} \Rightarrow \Theta'; \{t_1, \ldots, t_k\} \\ \Theta'; \forall \, i \in \{1, \ldots, k\}. \, \operatorname{do} \, \{v_i \leftarrow \varepsilon[x \mapsto t_i]; r; s \vdash \operatorname{load} \, F; \operatorname{return} \, \{t_i \mapsto v_i\}\} \Rightarrow \Theta''; vs \\ e_{err} = \forall \, i \in \{1, \ldots, k\}. \, \operatorname{do} \, \{b_i \leftarrow valid(vs(t_i)); \operatorname{return} \, (\bigwedge \, b_i)\} \\ \Theta; \varepsilon; r; \{s \mid x \in e\} \vdash \operatorname{load} \, F \Rightarrow \Theta''[a_{err} : e_{err}]; (a_{err}, vs) \end{array}
               \Theta; \varepsilon; r; s \vdash \mathsf{store} \ F \ v \Rightarrow \Theta'; (F', \phi') "Under heap \Theta and environment \varepsilon, store the representation v for the specification s on filesystem
F at path r and yield an updated filesystem F' and a validation function \phi'."
               s = M s_1
                                                                                                                                                                 \begin{array}{c} \Theta(a) = e \quad \Theta; e \Rightarrow \Theta'; (a_{err}, v) \\ \Theta'; \varepsilon; r; s \vdash \mathsf{store} \; F \; v \Rightarrow \Theta''; (F', \phi') \\ \Theta; \varepsilon; r; \mathsf{M} \; s \vdash \mathsf{store} \; F \; a \Rightarrow \Theta''; (F', \phi') \end{array}
             s = k
                                                                                                                                                   \frac{\Theta; \mathtt{store}_k(\varepsilon, F, r, (d, v)) \Rightarrow \Theta'; (F', \phi)}{\Theta; \varepsilon; r; k \vdash \mathtt{store} \; F \; (a_{err}, (d, v)) \Rightarrow \Theta'; (F', \phi)}
          \mathtt{store_{File}}(\varepsilon, F, r, (i, u)) \left\{ \begin{array}{l} \mathtt{return} \; (F[r := (i, \mathtt{File} \; u)], \lambda F'. \; F'(r) = (i, \mathtt{File} \; u)) \\ \mathtt{return} \; (F[r := \bot], \lambda F'. \; F'(r) \neq (\_, \mathtt{File} \; \_)) \\ \mathtt{return} \; (F, \lambda F'. \; F'(r) \neq (\_, \mathtt{File} \; \_)) \end{array} \right.
                                                                                                                                                                                                                                                                                                                              \begin{array}{l} \text{if } i \neq i_{\texttt{invalid}} \\ \text{if } i = i_{\texttt{invalid}} \land F(r) = (\_, \texttt{File} \_) \\ \text{if } i = i_{\texttt{invalid}} \land F(r) \neq (\_, \texttt{File} \_) \end{array}
\mathtt{store_{Dir}}(\varepsilon,F,r,(i,\{u_1,...,u_n\})) \left\{ \begin{array}{l} \mathtt{return} \; (F[r:=(i,\mathtt{Dir}\;\{u_1,...,u_n\})], \lambda F'.\; F'(r) = (i,\mathtt{Dir}\;\{u_1,...,u_n\})) \\ \mathtt{return} \; (F[r:=\bot], \lambda F'.\; F'(r) \neq (\_,\mathtt{Dir}\;\_)) \\ \mathtt{return} \; (F,\lambda F'.\; F'(r) \neq (\_,\mathtt{Dir}\;\_)) \end{array} \right.
                                                                                                                                                                                                                                                                                                                                                                                                                             if i \neq i_{invalid}
                                                                                                                                                                                                                                                                                                                                                                                                                              if i = i_{invalid} \wedge F(r) = (-, Di)
                                                                                                                                                                                                                                                                                                                                                                                                                              if i = i_{\text{invalid}} \wedge F(r) \neq (-, D)
       \mathtt{store}_{\mathtt{Link}}(\varepsilon, F, r, (i, r')) \left\{ \begin{array}{l} \mathtt{return} \; (F[r := (i, \mathtt{Link} \; r')], \lambda F'. \; F'(r) = (i, \mathtt{Link} \; r')) \\ \mathtt{return} \; (F[r := \bot], \lambda F'. \; F'(r) \neq (\_, \mathtt{Link} \; \_)) \\ \mathtt{return} \; (F, \lambda F'. \; F'(r) \neq (\_, \mathtt{Link} \; \_)) \end{array} \right.
                                                                                                                                                                                                                                                                                                                                       if i \neq i_{invalid}
                                                                                                                                                                                                                                                                                                                                       if i=i_{\text{invalid}} \land F(r)=(\_, \text{Link}\_) if i=i_{\text{invalid}} \land F(r) \neq (\_, \text{Link}\_)
            s = e :: s_1
                                                                                                                                                               \frac{\Theta; \llbracket e \rrbracket_{Path}^{\varepsilon} \Rightarrow \Theta'; r'}{\Theta'; \varepsilon; r'; s \vdash \mathtt{store} \; F \; v \Rightarrow \Theta''; (F', \phi')}{\Theta; \varepsilon; r; e :: s \vdash \mathtt{store} \; F \; v \Rightarrow \Theta''; (F', \phi')}
                s = \langle x : s_1, s_2 \rangle
                                                                                                                   \begin{split} \Theta; \varepsilon; r; s_1 \vdash \mathtt{store} \; F \; v_1 \Rightarrow \Theta_1; (F_1, \phi_1) \\ \Theta_1; \varepsilon[x \mapsto v_1]; r; s_2 \vdash \mathtt{store} \; F \; v_2 \Rightarrow \Theta_2; (F_2, \phi_2) \\ \phi = \lambda F'. \; \phi_1(F') \wedge \phi_2(F') \\ \Theta; \varepsilon; r; \langle x : s_1, s_2 \rangle \vdash \mathtt{store} \; F \; (a_{err}, (v_1, v_2)) \Rightarrow \Theta_2; (F_1 + F_2, \phi) \end{split}
             s={\tt P}\, {\stackrel{-}{e}}
                                                                                                                                                         \frac{\phi = \lambda F'. \ True}{\Theta; \varepsilon; r; \mathtt{P} \ e \vdash \mathtt{store} \ F \ (a_{err}, ()) \Rightarrow \Theta; (F, \phi)}
               s = s_1?
```

 $\frac{\phi = \lambda F'. \ r \notin \mathtt{dom}(F')}{\Theta; \varepsilon; r; s? \vdash \mathtt{store} \ F \ (a_{err}, Nothing) \Rightarrow \Theta; (F[r := \bot], \phi)}$

$$\frac{\Theta; \varepsilon; r; s \vdash \mathtt{store} \ F \ v \Rightarrow \Theta'; (F_1, \phi_1)}{\phi = \lambda F'. \ \phi_1(F') \land r \in \mathtt{dom}(F')}$$
$$\Theta; \varepsilon; r; s? \vdash \mathtt{store} \ F \ (a_{err}, \mathit{Just} \ v) \Rightarrow \Theta; (F_1, \phi)$$

$$s = \{s_1 \mid x \in e\}$$

$$\Theta; \llbracket e \rrbracket_{\{\tau\}}^{\varepsilon} \Rightarrow \Theta'; ts \quad vs = \{t_1 \mapsto v_1, ..., t_k \mapsto v_k\}$$

$$\phi = \lambda F'. \ ts = \{t_1, ..., t_k\} \land \bigwedge \phi_i(F')$$

$$\Theta'; \forall i \in \{1, ..., k\}. \ \text{do} \ \{(F_i, \phi_i) \leftarrow \varepsilon[x \mapsto v_i]; r; s \vdash \text{store} \ F \ v_i; \text{return} \ (F_1 + ... + F_k, \phi)\} \Rightarrow \Theta''; F' \ \phi'$$

$$\Theta; \varepsilon; r; \{s \mid x \in e\} \vdash \text{store} \ F \ (a_{err}, vs) \Rightarrow \Theta; (F', \phi')$$

Proposition 1 (Load Type Safety). If Θ ; ε ; r; $s \vdash \mathsf{load}\ F \Rightarrow \Theta'$; v' and $\mathcal{R}[\![s]\!] = \tau$ then $\vdash v : \tau$.

Theorem A.1 (LoadStore). If

$$\begin{array}{c} \Theta; \varepsilon; r; s \vdash \mathtt{load} \ F \Rightarrow \Theta'; v \\ \Theta''; \varepsilon; r; s \vdash \mathtt{store} \ F \ v' \Rightarrow \Theta'''; (F', \phi') \\ v \stackrel{err}{\Theta''} v' \end{array}$$

then F = F' and $\phi'(F')$.

Theorem A.2 (StoreLoad). If

$$\Theta$$
; ε ; r ; $s \vdash$ store F $v \Rightarrow \Theta'$; (F', ϕ')
 Θ' : ε ; r ; $s \vdash$ load $F \Rightarrow \Theta''$; v'

then
$$\phi'(F')$$
 iff $v \overset{err}{\sim} \overset{err}{\sim} \phi'' v'$

stronger than the original forest theorem: store validation only fails for impossible cases (when representation cannot be stored to the FS without loss)

weaker in that we don't track consistency of inner validation variables; equality of the values is modulo error information. in a real implementation we want to repair error information on storing, so that it is consistent with a subsequent load.

the error information is not stored back to the FS, so the validity predicate ignores it.

B. Forest Incremental Semantics

Note that:

- We have access to the old filelesystem, since filesystem deltas record the changes to be performed.
- We do not have access to the old environment, since variable deltas record the changes that already occurred.

$$\begin{split} &\delta_F ::= \operatorname{addFile}(r,u) \mid \operatorname{addDir}(r) \mid \operatorname{addLink}(r,r') \mid \operatorname{rem}(r) \mid \operatorname{chgAttrs}(r,i) \mid \delta_{F_1}; \delta_{F_2} \mid \emptyset \\ &\delta_v ::= \operatorname{M}_{\delta_a} \delta_{v_1} \mid \delta_{v_1} \otimes \delta_{v_2} \mid \{t_i \mapsto \delta_{\perp v_i}\} \mid \delta_{v_1}? \mid \emptyset \mid \Delta \\ &\delta_{\perp v} ::= \perp \mid \delta_v \\ \\ &\Delta_v ::= \emptyset \mid \Delta \\ &(\operatorname{addFile}(r',u)) \searrow_F r \triangleq & \text{if } F^*(r') \in F^*(r) \text{ then addFile}(r',u) \text{ else } \emptyset \\ &(\operatorname{addDir}(r')) \searrow_F r \triangleq & \text{if } F^*(r') \in F^*(r) \text{ then addDir}(r') \text{ else } \emptyset \\ &(\operatorname{addLink}(r',r'')) \searrow_F r \triangleq & \text{if } F^*(r') \in F^*(r) \text{ then addLink}(r',r'') \text{ else } \emptyset \\ &(\operatorname{rem}(r')) \searrow_F r \triangleq & \text{if } F^*(r') \in F^*(r) \text{ then rem}(r') \text{ else } \emptyset \\ &(\operatorname{chgAttrs}(r',i)) \searrow_F r \triangleq & \text{if } F^*(r') \in F^*(r) \text{ then chgAttrs}(r',i) \text{ else } \emptyset \\ &(\delta_{F_1};\delta_{F_2}) \searrow_F r \triangleq \delta_{F_1} \searrow_F r; \delta_{F_2} \searrow_{F_1} r \text{ where } F_1 = (\delta_{F_1} \searrow_F r) F \\ &\emptyset \searrow_F r \triangleq \emptyset \end{split}$$

$$\Theta; v \xrightarrow{\delta_v} \Theta'; v'$$

the value delta maps v to v'

monadic expressions only read from the store and perform new allocations; they can't modify existing addresses. For any expression application $e \Theta = (\Theta', v)$, we have $\Theta = \Theta \cap \Theta'$. errors are computed in the background

$$\frac{a' \not\in \operatorname{dom}(\Theta)}{\Theta; \delta_a; \Delta_e \vdash a: e \Rightarrow \Theta[a':e]; (a', \Delta)} \quad \frac{}{\Theta; \emptyset; \Delta_e \vdash a: e \Rightarrow \Theta[a:e]; (a, \Delta)} \quad \frac{}{\Theta; \emptyset; \emptyset \vdash a: e \Rightarrow \Theta; (a, \emptyset)}$$

 Θ ; ε ; Δ_{ε} ; r; $s \vdash \mathsf{load}_{\Delta} F \ v \ \delta_F \ \delta_v \Rightarrow \Theta'$; (v', Δ'_v) "Under heap Θ , environment ε and delta environment Δ_{ε} , incrementally load the specification s for the original filesystem F and original representation v, given filesystem changes δ_F and representation changes δ_v , to yield an updated representation v' with changes Δ'_v .

$$\frac{\Delta\varepsilon|_{F^{\prime}(c)} = \emptyset \quad \delta_{F} \searrow_{F} r = \emptyset}{\Theta; \varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \Theta \Rightarrow \Theta; (v, \emptyset)}$$

$$\frac{\Theta; \varepsilon; \Sigma_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \Theta \Rightarrow \Theta; (v, \emptyset)}{\Theta; \varepsilon; \Sigma_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta'; (v', \Delta)}$$

$$s = \operatorname{M} s_{1}$$

$$\frac{\Theta'(\varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta'; (v', \Delta_{v})}{\Theta; \varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta'; (v', \Delta_{v})} \quad v = v'$$

$$\frac{\Theta'(\varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta'; (v', \Delta_{v})}{\Theta; \varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta; (v', \Delta_{v})} \quad \theta'(\varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta; (v', \Delta_{v})}$$

$$\frac{\Theta; \delta_{\varepsilon}; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta; (v', \Delta_{v})}{\Theta; \delta_{\varepsilon}; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\varphi} \Rightarrow \Theta'; (v', \Delta_{v})} \quad \theta'(\varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}$$

$$\frac{S = e :: s_{1}}{\Theta; \varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})} \quad \theta'(\varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}$$

$$\frac{\Theta; \varepsilon; \Delta_{\varepsilon}; r; \varepsilon \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}{\Phi; \varepsilon; \Delta_{\varepsilon}; r; s \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}$$

$$\frac{\Phi; \varepsilon; \Delta_{\varepsilon}; r; \varepsilon \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}{\Phi; \varepsilon; \Delta_{\varepsilon}; r; \varepsilon \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}$$

$$\frac{\Phi_{\varepsilon}; \delta_{\varepsilon}; \epsilon; r; \varepsilon \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi'; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}{\Phi; \varepsilon; \Delta_{\varepsilon}; r; \varepsilon \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi; v' \Rightarrow \Phi'(\varepsilon; v', \Delta_{v})}$$

$$\frac{\Phi_{\varepsilon}; \delta_{\varepsilon}; r; v; r \vdash \operatorname{load}_{\Delta} F \ v \, \delta_{F} \ \delta_{\psi} \Rightarrow \Phi; v' \Rightarrow \Phi'; v' \Rightarrow \Phi'$$

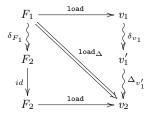
 Θ ; ε ; Δ_{ε} ; r; $s \vdash \mathtt{store}_{\Delta} F \ v \ \delta_{F} \ \delta_{v} \Rightarrow \Theta'$; (F', ϕ') "Under heap Θ , environment ε and delta environment Δ_{ε} , store the representation v for the specification s on filesystem F at path F, given filesystem changes δ_{F} and representation changes δ_{v} , and yield an updated filesystem F' and a filesystem validation function ϕ' ."

$$\begin{array}{c} \Delta_{||f(x)|} = \theta \cdot \delta_{f}^{-1} \nabla_{f}^{-1} = \theta \\ \theta : \varepsilon(r) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + r + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + r + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1} + \theta \\ \theta : \varepsilon(\lambda_{e}) \circ \delta_{f}^{-1} \circ \delta_{f}^{-1$$

Theorem B.1 (Incremental Load Soundness). If

$$\begin{split} \Theta; \varepsilon; r; s \vdash \mathsf{load} \ F_1 \Rightarrow \Theta_1; v_1 \\ \Theta_1; v_1 & \xrightarrow{\delta_{v_1}} \Theta_2; v_1' \\ \Theta_2; \varepsilon'; \Delta_\varepsilon; r; s \vdash \mathsf{load}_\Delta \ F_1 \ v_1' \ \delta_{F_1} \ \delta_{v_1} \Rightarrow \Theta_3; (v_2, \Delta_{v_1'}) \\ \Theta_1; \varepsilon'; r; s \vdash \mathsf{load} \ (\delta_{F_1} \ F_1) \Rightarrow \Theta_4; v_3 \end{split}$$

then $v_2 \overset{err}{\sim}_{\Theta_4} v_3$ and $valid(v_2) \overset{err}{\sim}_{\Theta_4} valid(v_3)$.



Lemma 1 (Incremental Load Stability). Θ ; ε ; Δ_{ε} ; r; M $s \vdash load_{\Delta} F$ a δ_{F} $(M_{\emptyset} \delta_{v}) \Rightarrow \Theta'$; (a, Δ_{a}) **Theorem B.2** (Incremental Store Soundness). *If*

$$\begin{split} \Theta; \varepsilon; r; s \vdash \mathtt{store} \; F \; v_1 \Rightarrow \Theta_1; (F_1, \phi_1) \\ \Theta_1; v_1 \xrightarrow{\delta_{v_1}} \Theta_2; v_2 \\ \Theta_2; \varepsilon'; \Delta_{\varepsilon}; r; s \vdash \mathtt{store}_{\Delta} \; F_1 \; v_2 \; \delta_{F_1} \; \delta_{v_1} \Rightarrow \Theta_3; (F_2, \phi_2) \\ \Theta_2; \varepsilon'; r; s \vdash \mathtt{store} \; (\delta_{F_1} \; F_1) \; v_2 \Rightarrow \Theta_4; (F_3, \phi_3) \end{split}$$

then $F_2 = F_3$ and $\phi_2(F_2) = \phi_3(F_3)$.

